Splee: A Declarative Information-Based Language for Multiagent Interaction Protocols

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ABSTRACT
The Blindingly Simple Protocol Language (BSPL) is a novel information-based approach for specifying interaction protocols that can be enacted by agents in a fully decentralized manner via asynchronous messaging. We introduce Splee, an extension of BSPL. The extensions fall into two broad categories: multicast and roles. In Splee, a role binding is information that is dynamically generated during protocol enactment, potentially as the content (payload) of communication between two agents. Multicast communication is the idea that a message is sent to a set of agents. The two categories of extensions are interconnected via novel features such as set roles (the idea that a role binding can be a set of agents) and subroles (the idea that agents playing a role must be a subset of agents playing another role). We give the formal semantics of Splee and give small model characterizations of the safety and liveness of Splee protocols. We also introduce the pragmatic idea of query attachments for messages. Query attachments take advantage of Splee’s information-orientation, and can help restrict the information (parameter bindings) communicated in a message.

1. INTRODUCTION
A protocol is a first-class abstraction for specifying multiagent systems [4, 19, 31]. Work in multiagent protocols addresses two important concerns: the (normative) meanings of the operations performed by the participants and the ordering and occurrence constraints on the operations, which we refer to together as operational constraints. To see the distinction between meanings and operational constraints, consider the familiar setting of buyer-seller interactions. An operational constraint in this setting would be that a quote for an item cannot be sent by a seller unless a request for quotes for that item has been received from the buyer. The meaning of the quote message in this setting would be that it commits the seller to delivering the item to the buyer if the buyer pays the quoted price. In decentralized settings, the operations would correspond to communicative acts realized via asynchronous messaging between agents.

Meaning-based protocols, especially commitment protocols [22, 35, 39, 42], have been extensively studied in multiagent systems. In contrast to previous approaches, we are concerned primarily with the specification of operational protocols, that is, protocols that specify operational constraints. Below, we use the term protocol to mean operational protocols. An important challenge is designing protocol languages that can capture common interaction patterns and support the decentralized enactment of those patterns by asynchronous messaging between agents. We address interaction patterns involving subtleties of roles and multicast communication that have not been systematically addressed in protocol languages that support decentralized enactments.

We take the Blindingly Simple Protocol Language (BSPL) [36, 37, 38] as our point of departure. In contrast to other protocol languages (discussed in Section 6), BSPL is a formal, declarative, and information-based approach for specifying protocols. It naturally supports correct decentralized enactments of protocols via asynchronous messaging between agents. Although BSPL represents an important innovation in interaction protocol languages, it lacks the expressiveness for specifying certain common interaction patterns. One, in a BSPL protocol, roles are not information parameters. The effect is that BSPL does not support dynamic role bindings. Further, in a BSPL protocol, a role may not be played by more than one agent. Two, BSPL supports only point-to-point communication between agents; it does not support multicast, where an agent may send the same message instance to a set of agents.

To highlight the need for more sophisticated models, let us consider auctions as an illustrative application. In any enactment (instance) of an auction protocol, multiple agents may play bidder (not supported in BSPL), specifically, the winner must be selected dynamically from among the bidders (not supported in BSPL). Further, the winner is the bidder who has bid the highest (not supported in BSPL). Integrity requires that in a particular (single-item) auction enactment, the same item information is multicast to all bidders (not supported in BSPL). Analogous challenges would arise in specifying the Contract Net [18] (more than one agent may play contractor) as well as protocols for insurance claims, where the claims adjuster is determined on the fly from among multiple inspectors [10].

This paper seeks to overcome the shortcomings of BSPL by proposing an extended language that we dub Splee. The following are the main novel ideas in Splee.

Roles as information parameters. Role bindings are dynamically produced during protocol enactment.
Set roles. A role is adopted by a set of agents.

Subroles. One role may be a subrole of another, indicating that any agent who plays the first also plays the second.

Multicast. An agent may send a message to the set of agents playing a role.

Mapping keys. A protocol’s key consisting of two or more parameters may be mapped into a key of one parameter. This mapping facilitates natural specification and composition.

Query attachments. A query restricts the binding generated for a parameter to specific values.

Our contributions are the syntax of Splee along with characterizations of important correctness properties, namely, liveness and safety, for Splee protocols. Notably, for a BSPL protocol, these properties may be determined from its specification alone. However, this is not necessarily so for Splee, as role bindings are dynamic and effectively require consideration of infinitely many universes of discourse. To overcome this challenge, we propose a “small model” characterization of these properties.

2. BACKGROUND: BSPL

BSPL is declarative: it has no control-flow abstractions. A BSPL protocol is a bag of protocols, which bottom out in messages. Instead of specifying control flow, in BSPL, one specifies information flow. Specifically, a BSPL protocol (and messages, since they are protocols as well) has information parameters and causality explicitly specified in terms of information flow (via messaging) between agents. In other words, the messages an agent may send at any point in an enactment depend on the parameter bindings known to that agent at that point. Notably, an agent can receive any message at any point. Two, BSPL supports integrity constraints via explicit key parameters that functionally determine other parameters and capture the idea that in any protocol enactment, an agent may not send or receive conflicting information. Causality and integrity form the bases for safety and liveness [38], which are important correctness properties pertaining to decentralized enactments of BSPL protocols.

2.1 Illustrating BSPL

Listing 1 illustrates BSPL’s main concepts.

- The listing declares Request Quote as the name of the protocol; two roles (both public, in this case): M (merchant) and C (customer); and three parameters (all public, in this case): ID, item, and price. Parameter ID is annotated key, meaning that ID functionally determines the other parameters. All parameters are adorned "out", meaning that their bindings are generated by enacting the protocol, i.e., enacting the messages declared in it. The public parameters of a protocol serve as its interface and facilitate composition.

- Request Quote declares two message schemas (the order of their listing is irrelevant). By convention, any key parameter of the protocol is a key parameter for any message in which it appears, though a message may have additional key parameters. Thus, request is directed from customer to merchant and its key is ID.

- The message request has two parameters ID and item, each annotated "out", meaning that a customer can generate bindings for them when it sends an instance of request. In quote, ID and item are "in", meaning that a merchant may send an instance of quote with some bindings for ID and item, only if it has received an instance of request with those bindings.

- Bindings for ID identify enactments of Request Quote. That is, distinct tuples of bindings as allowed by the key constraints correspond to distinct enactments. A complete enactment of Request Quote corresponds to a tuple of bindings for all its public parameters.

Listing 1: A simple quote protocol in BSPL.

<table>
<thead>
<tr>
<th>Request Quote</th>
</tr>
</thead>
<tbody>
<tr>
<td>roles M, C // Merchant, Customer</td>
</tr>
<tr>
<td>parameters out ID key, out item, out price</td>
</tr>
<tr>
<td>C \rightarrow M: request [out ID, out item]</td>
</tr>
<tr>
<td>M \rightarrow C: quote [in ID, in item, out price]</td>
</tr>
</tbody>
</table>

Singh [38] formalizes liveness and safety for BSPL and gives verification techniques. A protocol is live iff every enactment can complete and there is at least one enactment. Request Quote is live (there is only one enactment). A protocol that cannot be enacted is not live.

A protocol is safe iff it is not possible to produce conflicting bindings for a parameter for a given key binding in any enactment. A trivial safety violation would be if a customer sent request with ID “1” and item “flower,” and then sent ID “1” and item “phone.” This violation is trivial because it can be avoided by the customer based solely on its local knowledge. (Resending (“1”, “flower”) though would not be a violation.) A message is viable iff sending it does not cause any local violation. Safety is characterized as there being no violation assuming each message emission is viable. Request Quote is safe. Request Quote Unsafe in Listing 2, which modifies Request Quote by adding message desire from C to M (indicating the price the customer desires the item for), is unsafe. Both merchant and customer can concurrently produce bindings for price; that is, a nonlocal conflict exists.

Listing 2: An unsafe protocol in BSPL.

<table>
<thead>
<tr>
<th>Request Quote Unsafe</th>
</tr>
</thead>
<tbody>
<tr>
<td>C \rightarrow M: desire [in ID, in item, out price]</td>
</tr>
</tbody>
</table>

In BSPL, roles are not parameters: they are adopted externally, not during enactment. In effect, Request Quote defines a multiagent system of two agents, whose names might as well be M and C.

We use auctions as our running example. A seller requests that an auctioneer put up an item for auction. The auctioneer sends a call for bids including item and starting amount (samt) to a set of bidders. One or more bidders may submit bids. The auctioneer announces the highest bidder as the winner.

The BSPL Call for Bids in Listing 3 is inadequate because B can be played by at most one agent in any enactment.
2.2 Decentralization

BSPL realizes LoST (Local State Transfer) [37], which is a decentralized architecture style for multiagent systems. We summarize the basic requirements of LoST. Agents interact via asynchronous messaging; in particular, there is no global repository of state (shared-nothing setting). Each agent has a local (public) state that consists of the messages it has sent and received. Further, agents are autonomous, meaning that they may or may not send messages. An agent can send any message for which it has the requisite information.

LoST requires that no assumptions be made about message delivery order. LoST requires being able to work over lossy infrastructures that support message retransmission. In such a loosely coupled architectural setting, LoST imposes the correctness requirement that agents should have a consistent view of their interactions. Safety for BSPL, as described above, in effect, captures the consistency requirements. Liveness ensures that consistency is not maintained trivially, that is, by not acting at all.

3. SPLEE SYNTAX AND MOTIVATION

The formal syntax of Splee is given next. A superscript of + indicates one or more repetitions, and [ and ] delimit expressions, which are optional when without a superscript.

L1. A protocol declaration consists of a name, public parameters, optional private parameters, and references to constituent protocols or messages. Public parameters are adorned. Both public and private parameters may have one or more optional qualifiers. The public parameters marked key form this declaration’s key. In Splee, roles are parameters; qualifier role indicates if a parameter is a role.

\[ \text{Protocol} \rightarrow \text{Name} \{ \text{Public} [\text{Private}] \text{Reference}^+ \} \]

L2. Public parameters are adorned with information flow constraints and qualifiers.

\[ \text{Public} \rightarrow \text{public} [\text{Adorned} [\text{Qualifier}]]^+ \]

L3. Private parameters are not adorned as they are not part of a protocol’s interface.

\[ \text{Private} \rightarrow \text{private} [\text{Name} \text{Qualifier}]^+ \]

L4. A reference to a protocol (from a declaration) may consist of the name of the protocol appended by as many parameters as it declares.

\[ \text{Reference} \rightarrow \text{Name} (\text{Adorned}^+) \]

L5. A reference may be a message schema, and consists of exactly one name, sending role and receiving roles, and one or more parameters. The receiving role is adorned.

\[ \text{Reference} \rightarrow \text{Name} \rightarrow \text{Adorned} : \text{Name[Adorned]}^+ \]

L6. Adorned \rightarrow Adornment Name

L7. Qualifiers indicate if a parameter is a key, a singleton role (role but not set), a nonsingleton role (role and set), if an agent playing a role is a member of a set of agents playing another role (subrole), and whether a parameter has a map constraint. The order of the qualifiers is irrelevant.

```
Listing 3: A call for bids in BSPL.
BSPL Call for Bids {
roles S, A, B //Seller, Auctioneer, Bidders
parameters out aID key, out item, out samt
S \rightarrow A: request [out aID, out item]
A \rightarrow B: call [in aID, in item, out samt]
}
```

```
Listing 4: An attempt to support multiple bidders by treating roles as information parameters.
Multiple Bidders {
public out aID key, out item, out samt, out S role key, out A role key
private B role key
S \rightarrow out A: request [out aID, out item]
A \rightarrow out B: call [in aID, in S, in item, out samt]
}
```

```
Listing 5: A call for bids in BSPL.
BSPL Call for Bids {
roles S, A, B //Seller, Auctioneer, Bidders
parameters out aID key, out item, out samt
S \rightarrow A: request [out aID, out item]
A \rightarrow B: call [in aID, in item, out samt]
}
```

We gradually work our way up to a desirable specification of an auction protocol. Below, we use \( X \rightarrow Y \) to mean that the set of parameters \( X \) functionally determines each parameter in the set \( Y \) [23]. We highlight five innovations below.

First innovation: roles as information. Supporting multiple bidders implies being able to bind multiple agents (i.e., their identifiers) with the role \( B \), in essence, treating \( B \) as a parameter. Multiple Bidders in Listing 4 treats all roles as parameters. Bindings for \( A \) and \( S \) are generated by enacting Multiple Bidders; moreover, they are both key parameters of the protocol (in addition to \( \text{aID} \)). Role \( B \) is a private role parameter of the protocol. The sender is not adorned because its binding must be fixed when the message is sent. Notice the presence of “in” \( S \) in \( \text{call} \): since \( \{S, A, \text{aid}\} \rightarrow \{\text{item}\} \), it cannot be omitted.

The reason Multiple Bidders supports multiple bidders is that \( B \) is a key parameter for \( \text{call} \) (following the convention that a message parameter that is a key parameter for the protocol is a key parameter for the message). Or, given an enactment of Multiple Bidders—by specifying for \( A, S \), and \( \text{aID} \)—there can be many bindings for \( B \), and therefore many call messages (one to each bidder).

```
Listing 4: An attempt to support multiple bidders by treating roles as information parameters.
Multiple Bidders {
public out aID key, out item, out samt, out S role key, out A role key
private B role key
S \rightarrow out A: request [out aID, out item]
A \rightarrow out B: call [in aID, in S, in item, out samt]
}
```

Second innovation: key mapping functions that preserve functional dependencies. We represent a mapping function as an injective function \( \text{map} : \mathbb{S}^{\text{func}} \rightarrow \text{String} \) that has the property that if \( X \rightarrow Y \), then \( \{\text{map}(X)\} \rightarrow Y \). String concatenation and perfect hashes are examples of mapping functions. Listing 5 uses key mapping to transform \( \{A, S, \text{aID}\} \rightarrow \{\text{nil}\} \). That is, \( \{\text{nil}\} \rightarrow \{A, S, \text{aID}, \text{item}\} \). Key mapping facilitates specification and composition, and may help obscure the bindings involved (e.g., to hide the seller’s identity from bidders). Notice that in Listing 5, \( S \) and \( A \) are no longer annotated as key parameters because \( \text{nilD} \) suffices.

```
Listing 5: Applying a dependency-preserving key map.
Key Mapping {
public out nID key map(S, A, nID), out item, out samt, out S role, out A role
private B role key
S \rightarrow out A: request [out aID, out item, out nID]
A \rightarrow out B: call [in nID, in item, out samt]
}
```

Third and fourth innovation: set roles and multicast. Listing 5 has an important shortcoming: the auctioneer can send different bindings for \( \text{samt} \) to different bidders, which would be wrong in a (single-item) auction enactment. Different bindings are possible because \( B \) is a key parameter in \( \text{call} \);
that is, \(\{nID, B\} \to \{\text{samt}\}\). Recall that we made \(B\) key for the express purpose of supporting multiple bidders. So how can we have multiple bidders but prevent different \(\text{samt}\) bindings from being communicated to them? The solution is to treat the binding of \(B\) as a set of agents, as in Listing 6. In effect, because \(B\) is no longer key, \(\{nID\} \to \{\text{samt, B}\}\).

Listing 6: \textit{call} is a multicast message; \(B\) is set, meaning that it can take a set of more than one agent as its binding.

\[
\text{Multicast} \{
\begin{align*}
\text{public} & \text{ out nID key map}(S, A, aID), \text{ out item, out samt, out S role, out A role} \quad & \\
\text{private} & B \text{ role set} \quad & \\
S & \to \text{ out A: request} \text{ [out aID, out item, out nID]} \quad & \\
A & \to \text{ out B: call} \text{ [in nID, in item, out samt]} \\
\end{align*}
\]

\textit{Fifth and sixth innovations:} role binding selection, in which an agent performs a role binding and communicates it to other agents, and \textit{subroles}. Listing 7 introduces bidding and selection of a winner. Any agent playing an individual bidder (I) is indicated to belong to the set of agents playing \(B\). Such agents may send instances of \textit{bid} with an amount \(\text{bamt}\), which may be different for each bidder. The auctioneer selects the winner (\(W\)) in \textit{wins}; an agent playing \(W\) must also be a member of \(B\). Recall that in the actor model of computation, an actor may send another actor a third actor’s name [25]. In contrast, in Splee, an agent may not only send an agent’s name to another but may also send a role binding, in essence changing the type of the agent.

Listing 7: Bidding and selecting winner. For brevity, we omit the qualifier role when \(\text{subrole}\) is present.

\[
\text{Winner} \{
\begin{align*}
\text{public} & \text{ out nID key map}(S, A, aID), \text{ out item, out samt, out S role, out A role, out W subrole B, out want} \quad & \\
\text{private} & B \text{ role set}, I \text{ key subrole } B / / \text{Individual bidder} \quad & \\
S & \to \text{ out A: request} \text{ [out aID, out item, out nID]} \quad & \\
A & \to \text{ out B: call} \text{ [in nID, in item, out samt]} \quad & \\
I & \to \text{ in A: bid} \text{ [in nID, in item, out bamt]} \quad & \\
A & \to \text{ in B: wins} \text{ [in nID, out W, out want]} \\
\end{align*}
\]

Splee protocols are subject to certain well-formedness criteria. Only role parameters may be set; if a role \(X\) is \textit{subrole} of role \(Y\), then both \(X\) and \(Y\) are \textit{role} and \(Y\) is \textit{set}; the sender and receiver roles in any message declaration are both \textit{role}, the sender is not a \textit{set}, and receiver is not adorned "nil"; and at least one public parameter is declared key. Further, because nonkey parameters have no meaning when separated from their key, the key (or its mapped form) with which the binding of a parameter is produced must be used in any reference where the parameter is used.

\section{4. SEMANTICS}

We formalize the above intuitions, enhancing Singh’s [38] semantics. The significant difference in our treatment arises from the following fact. For a BSPL protocol, the relevant \textit{universe of discourse} consists of roles and messages in the protocol. In contrast, for a Splee protocol, there are infinitely many universes of discourse, each including a finite set of agents and the roles each agent plays in the protocol.

We give a brief overview of the formalization before laying out its details. First, we formalize the structure of a protocol. We explain how a message schema is itself an elementary protocol. We then relate a message instance to its schema. This enables us to define the history of an agent as a set of message instances. Then we define a viable message for a history as one that satisfies causality, integrity, role, and map constraints. A multiagent enactment is modeled by a history vector whose components are histories of individual agents. Viable history vectors are those that satisfy the physical constraint that a message must have been sent before it is received. To capture enactments for specific roles, message schemas, agents, and the roles they play, we introduce the idea of a universe of discourse (UoD). This enables us to define the universe of enactments of a UoD. This enables us to define enactments (instances) of a protocol, the enactment of a message schema being the base case.

For convenience, we fix the symbols by which we refer to finite lists (mostly, treated as sets) of public parameters (\(\bar{p}\)), public key parameters (\(\bar{k}\)), private parameters (\(\bar{q}\)), private key parameters (\(\bar{l}\)), public roles (\(\bar{x}\)), public \(\text{samt}\) (\(\bar{s}\)), and qualified \(\text{samt}\) (\(\bar{r}\)). Usually, we do not care whether the role takes a singleton set, we simply write \(r\). Also, where we do not reference a \(\text{samt}\) key, the key (or its mapped form) with which the binding of a parameter is produced must be used in any reference where the parameter is used.

Definition 1 states that a Splee protocol (via any of its parameters) may reference another protocol (via its public parameters). The references bottom out at message schemas.

**Definition 1:** A protocol \(P = \langle n, \bar{p}, \bar{k}, \bar{q}, \bar{l}, \bar{x}, \bar{y}, \bar{z}, \bar{c}, \bar{F}\rangle\) is a tuple, where \(n\) is a name; \(\bar{p}, \bar{k}, \bar{q}, \bar{l}, \bar{x}, \bar{y}, \bar{z}\), and \(\bar{c}\) are as above; and \(\bar{F}\) is a finite set of \(f\) references, \(\{F_1, \ldots, F_r\}\). For \(\forall i \leq 1 \leq f \Rightarrow F_i = \langle n_i, \bar{p}_i, \bar{k}_i, \bar{q}_i, \bar{l}_i, \bar{x}_i, \bar{y}_i, \bar{z}_i, \bar{c}_i, \bar{F}\rangle\), and \(\langle n_i, \bar{p}_i, \bar{k}_i, \bar{q}_i, \bar{l}_i, \bar{x}_i, \bar{y}_i, \bar{z}_i, \bar{c}_i, \bar{F}\rangle\) is the public projection of a protocol \(P_i\) (with parameters renamed). The public projection of a protocol \(P = \langle n, \bar{p}, \bar{k}, \bar{q}, \bar{l}, \bar{x}, \bar{y}, \bar{z}, \bar{c}, \bar{F}\rangle\), is given by the tuple \(\langle n, \bar{p}, \bar{k}\rangle\).

We treat a message schema with name \(m\), parameters \(\bar{p}\), sender role (\(s \in \bar{p}\)), singleton receiver role (\(r \in \bar{p}\)), key parameters \(\bar{k}\), and constraints \(\bar{c}\) as an atomic protocol with exactly two public roles (sender and receiver) and no references: \(\langle m, \bar{p}, \bar{k}, \bar{q}, \bar{l}, \bar{x}, \bar{y}, \bar{z}, \bar{c}, \bar{F}\rangle\). If the receiver is qualified set, then we write it as \(\langle m, \bar{p}, \bar{k}, \bar{q}, \bar{l}, \bar{x}, \bar{y}, \bar{z}, \bar{c}, \bar{F}\rangle\). For brevity, we write them as "\(\bar{m} : p(k, s \rightarrow r)\bar{c}\)" and "\(\bar{m} : p(k, s \rightarrow r)\bar{c}\)\)\). Usually, \(\bar{k}\) and \(\bar{c}\) are understood from the protocol in which the schema is referenced. Specifically, \(\bar{k}\) equals the intersection of \(p\) with the key parameters of the protocol declaration and \(\bar{c}\) contains any subrole constraints that pertain to either \(s\) or \(r\) and relevant map constraints.

Below, let roles(\(P\)) = \(\bar{x} \cup \bar{y} \cup \bigcup_i \text{roles}(F_i)\); params(\(P\)) = \(\bar{p} \cup \bigcup_i \text{params}(F_i)\); msgs(\(P\)) = \(\bigcup_i \text{msgs}(F_i)\) and msgs("\(\bar{m} : p(k, s \rightarrow r)\bar{c}\)\)\) = \(\{m\}\). Definition 2 assumes that message instances are unique up to the key, as in their schema.

**Definition 2:** A message instance \(m[\bar{p}, \bar{v}]\) associates a message schema "\(\bar{m} : p(k, s \rightarrow r)\bar{c}\)\) with a list of values, where \(\bar{v} = [\bar{p}, \bar{v}]\), \(\bar{v} \downarrow_s\) is a singleton set of agents, and \(\bar{v} \downarrow_r\) is a set of
agents, and \( \vec{v} \downarrow = \vec{\text{nil}} \) if \( p \not\in \vec{p}X \). If the schema specified \( \rightarrow \), then \( \vec{v} \downarrow \) would be a singleton set as well. For convenience, we may make more schema elements explicit, e.g., by writing \( m[p, \vec{r}, \vec{c}] \) or \( m[p, s, r, \vec{k}, \vec{c}, \vec{v}] \), as necessary.

Definition 3 captures the idea of a history of an agent as a sequence (equivalent to a set in our approach) of all and only the message instances emitted or received by the agent. Thus, \( H^\alpha \) captures the local view of agent \( \alpha \) during a protocol enactment. A history may be infinite in general. However, we assume each enactment in which a tuple of parameter bindings is generated is finite. Notice that the emission of a message instance that has more than one receiver corresponds to the emission of a set of physical message tokens of identical contents, one to each receiver. We assume infrastructure supports sending such message tokens.

Definition 3: A history of an agent \( \alpha \), written \( H^\alpha \), is given by a sequence of zero or more message instances \( m_1 \circ m_2 \circ \ldots \) (\( \circ \) means sequence). Each \( m_i \) is of the form \( m[p, s, r, \vec{v}] \) and either \( \alpha \in \vec{v} \downarrow \) or \( \alpha \in \vec{v} \downarrow \).

Definition 4 captures the idea that what an agent knows at a history is exactly given by what the agent has seen so far in terms of incoming and outgoing messages. Here, 2(i) ensures that the message instance under consideration does not violate the uniqueness of the bindings; 2(ii) ensures that the agent knows the binding for each \( \vec{r}^{in} \) parameter and not for any "out" or \( \vec{r}^{nil} \) parameter; 2(iii) ensures that the instance satisfies map constraints; and 2(iv) ensures that the subrole constraints are satisfied.

Definition 4: A message instance \( m[p, s, r, \vec{k}, \vec{c}, \vec{v}] \) is viable at \( H^\alpha \) iff (1) \( \alpha \in \vec{v} \downarrow \) (reception) or (2) \( \alpha \in \vec{v} \downarrow \) (emission) and (i) \( (\forall m_i \, [m_i(p), v_i] \in H^\alpha \) if \( \vec{k} \subseteq \vec{p} \) and \( v_i \downarrow \vec{v} \downarrow \vec{k} \) then \( v_i \downarrow \vec{v} \downarrow \vec{k} \) (emission), \( H^\alpha \) and \( p \in \vec{p} \) and \( \vec{k} \subseteq \vec{p} \). (ii) \( (\forall p \in \vec{p} : p \in \vec{p} \downarrow \alpha \in \vec{v} \downarrow \vec{p} \) if \( (\exists m_i \, [p_i, v_i] \in H^\alpha \) and \( \vec{k} \subseteq \vec{p} \)). (iii) every map constraint in \( \vec{c} \) is satisfied in \( \vec{v} \), and (iv) (for every constraint \( s \) subrole \( g \) in \( \vec{c} \), \( (\exists m_i \, [p_i, v_i] \in H^\alpha \) such that \( \alpha \in v_i \downarrow \downarrow \), and (for every constraint \( r \) subrole \( g \) in \( \vec{c} \), \( (\exists m_i \, [p_i, v_i] \in H^\alpha \) such that \( v_i \downarrow \downarrow \subseteq v_i \downarrow \)).

Definition 5 captures that a history vector for a protocol is a vector of histories of agents that together are causally sound: a message instance is received only if it has been emitted [30].

Definition 5: A history vector for a finite set of agents \( \mathcal{A} \) is \( H^\mathcal{A} = \{ H^\alpha \} \) such that \( (\forall \alpha \in \mathcal{A} : H^\alpha \) is a component in the vector and \( (\forall m[p, s, r] \in H^\alpha : \alpha \in \vec{v} \downarrow \downarrow \) if \( \alpha \in \vec{v} \downarrow \downarrow \), \( \beta \in \vec{p} \downarrow \downarrow \), then \( m[p, s, r, \vec{v}] \in H^\beta \)).

A history vector records the progression of a protocol enactment. Under the above causality restriction, a vector that includes a reception must have progressed from a vector that includes the corresponding emission. Further, we avoid the FIFO assumption about message delivery. The viability of the messages emitted by any agent ensures that the progression is epistemically correct with respect to each agent.

Definition 6: A history vector for a finite set of agents \( \mathcal{A} \), \( H^\mathcal{A} = \{ H^\alpha \} \), is viable iff (1) each of its component histories is empty or (2) it arises from the progression of a viable history vector through the emission or the reception of a viable message instance by one of its agents, i.e., \( (\exists m_i : H^\alpha = H^\alpha \circ m_i \) and \( \{ H^\alpha \} \) is viable).

Definition 7 introduces a universe of discourse (UoD). Definition 8 defines viable history vectors relative to a UoD.

The heart of our formal semantics is the intension of a protocol, defined relative to a UoD, and given by the set of viable history vectors, each corresponding to its successful enactment. Given a UoD, Definition 8 specifies a universe of enactments, based on which we express the intension of a protocol. We restrict attention to viable vectors because those are the only ones that can be realized under our assumptions. We include private parameters in the intension to support compositionality. In the last stage, we project the intension to the public parameters.

Definition 7: A UoD is a tuple \( (\mathcal{R}, \mathcal{M}, \mathcal{A}, \mathcal{X}) \) where \( \mathcal{R} \) is a set of roles; \( \mathcal{M} \) is a set of message names; each message specifies its parameters along with its sender and receiver from \( \mathcal{R} \); \( \mathcal{A} \) is a finite set of agents; and \( \mathcal{X} \subseteq \mathcal{R} \times \mathcal{A} \). Tuple \( (\rho, a) \in \mathcal{X} \) means that agent \( a \) plays role \( \rho \).

Definition 8: A viable history vector for a UoD \( \mathcal{U} \) is a viable history vector \( \{ H^1, \ldots, H^m \} \) such that (1) exactly \( j \) distinct agents appear in \( \mathcal{X} \) and each such agent has a history in the vector, and (2) each message instance in any history in the vector instantiates a schema in \( \mathcal{M} \). The universe of enactments for that UoD, \( \mathcal{U}_{\mathcal{R}, \mathcal{M}, \mathcal{A}, \mathcal{X}} \) is the set of viable history vectors for that UoD.

Definition 9 states that the intension of a message schema is given by the set of viable history vectors on which that schema is instantiated, i.e., an instance of the schema occurs in both its sender and each receiver’s histories.

Definition 9: The intension of a message schema is given by: \( \mathcal{U} \) is a viable history vector by \( \{ H | H \in \mathcal{U}_{\mathcal{R}, \mathcal{M}, \mathcal{A}, \mathcal{X}} \) and \( (\exists a, \vec{v}; i : H^i = m[p, s, r, \vec{v}] \) and \( \alpha \in \vec{v} \downarrow \downarrow \) and \( (\forall j \in i \in \vec{v} \downarrow \downarrow ) \).

As for BSPL, a Splee protocol completes when all its public parameters are bound. A (composite) protocol completes if one or more of subsets of its references completes. Informally, each such subset contributes all the viable interleavings of the enactments of its members, i.e., the intersection of their intensions. Definition 10 captures the cover as an adequate subset of references of a protocol, and states that the intension of a protocol equals the union of the contributions of each of its covers.

Definition 10: Let \( \mathcal{P} = (n, p, k, i, l, x, y, z, \vec{c}, F) \) be a protocol. Let \( \text{cover}(\mathcal{P}, \mathcal{G}) \equiv G \subseteq F \rightleftharpoons (\forall p \in \vec{p} : \exists G_i \in \mathcal{G} : G_i = \langle n, p, k_i \rangle ) \) and \( \text{P}' \)’s intension, \( \mathcal{U}_{\mathcal{P}, \mathcal{M}, \mathcal{A}, \mathcal{X}} = \bigcup_{\text{cover}(\mathcal{P}, \mathcal{G})} \mathcal{U}_{\mathcal{P} = \mathcal{G}, \mathcal{R}, \mathcal{M}, \mathcal{A}, \mathcal{X}} \). Define 11 define the notion of a UoD of a protocol as involving only \( \mathcal{P}' \)’s roles and messages (including its references recursively). A protocol UoD would vary with the set of agents and the roles they play in the protocol.

Definition 11: A UoD of a protocol \( \mathcal{P} \), written \( \text{UoD}(\mathcal{P}) \), is a UoD \( \langle \mathcal{R}, \mathcal{M}, \mathcal{A}, \mathcal{X} \rangle \) where \( \mathcal{R} = \text{roles}(\mathcal{P}) \) and \( \mathcal{M} = \text{msgs}(\mathcal{P}) \). By allUoD(\mathcal{P}), we refer to the set of all UoD(\mathcal{P}).

4.1 Naive Properties

Safety means that for any key value, we cannot produce a history vector that generates more than one binding for any parameter. Liveness means that we cannot produce a history vector that deadlocks. Definitions 12 and 13 characterize these properties weakly meaning they require only the existence of an appropriate UoD (i.e., an appropriate set of agents and their roles bindings).

Definition 12: A protocol \( \mathcal{P} \) is weakly safe if \( (\forall U : U \in \text{allUoD}(\mathcal{P}) \) and each history vector in \( \mathcal{P} U \neq \emptyset \) is safe). A
history vector is safe iff all key uniqueness constraints apply across all histories in the vector.

Definition 13: A protocol $P$ is weakly live iff ($\forall U : U \in allUoD(P)$ and each history vector in $U_U$ can be extended through a finite number of message emissions and receptions to a history vector in $U_U$ that is complete).

Ideally, we would prefer strong characterizations where satisfaction did not depend upon a UoD. Definition 14 gives to a history vector in $P$ through a finite number of message emissions and receptions to a history vector in $U_U$ that is complete).

However, the strong versions would be too strong: clearly, there exists a UoD for any protocol in which it is not live. For example, the auction protocol in Listing 7 is not live if no agent plays auctioneer.

Because for any protocol $P$, allUoD($P$) is an infinite set, we employ model abstraction techniques to make the problem of verifying safety and liveness for the protocol tractable. Next, we describe a method for statically verifying Spree protocols for liveness and safety.

4.2 Distinct UoDs

In general, an agent may adopt more than one role in a protocol. Liveness and safety of a protocol should not rely upon the same agent adopting two or more roles. In a protocol, if any two roles were meant to be adopted by one agent, then the protocol is ill-conceived (we should simply merge the two roles into one). A distinct UoD is one where each role is played by a distinct agent except when the roles are connected by a subrole relationship. Formally, for any UoD of a protocol, we can generate a distinct UoD by substituting new agent identifiers for every agent that plays multiple roles in the original UoD, none of which are connected by a subrole relationship. For example, if agent $a$ plays both roles $\rho_1$ and $\rho_2$, we generate new agent identifiers $a_{\rho_1}$ and $a_{\rho_2}$ for the distinct UoD and substitute them for the original agent by binding them to the roles in their place: $a_{\rho_1}$ with $\rho_1$ and $a_{\rho_2}$ with $\rho_2$.

4.3 Canonical UoDs

Informally, our strategy is the following. For modularity, we consider only distinct UoDs for a protocol. Later we show how to handle the case where agents play multiple roles.

The first step is to reduce arbitrary (distinct) UoDs to UoDs with a canonical structure. We define a large UoD for $P$ as one where every role is played by some agent and if the protocol has set roles, then at least one of the roles is played by three or more agents. A canonical UoD for $P$ is one where every role is played by some agent and every set role is played by exactly two agents. The intuition behind every set role played by two agents (not fewer) in a canonical UoD is that if correctness relied upon fewer than two agents acting as a set role, then it would be pointless to declare it a set role. Since agent identities are not important, we can generate a unique canonical UoD for a protocol where for any nonset role $\rho$, its agent identifier is $a_\rho$ and for set role $\rho'$, its agent identifiers are $a_{\rho'}$ and $a_{\rho'}$.

Theorem 1: A protocol $P$ is safe in a large UoD for $P$ iff $P$ is safe in the canonical UoD for $P$.

Proof. In the forward direction, we set up an inductive ar-

...
distinct, then there is an agent \(a\) that plays two roles \(\rho\) and \(\rho'\) that were played by distinct agents in \(U'\). Combining histories can only reduce conflicts; so if there were no conflicts in any history vector of \(P\) in \(U'\), then there are no conflicts in any history of \(P\) in \(U\).

**Theorem 4:** Assume \(P\) is safe in a UoD \(U\). \(P\) is live in \(U\) iff it is live in \(U\)'s distinct UoD \(U'\).

**Proof.** In the forward direction, the projection to multiple histories (as described above) will preserve information flow. Hence liveness will be preserved. In the converse direction, if \(U\) is distinct we are done. If \(U\) is not distinct, then there is an agent \(a\) that plays two roles \(\rho\) and \(\rho'\) that were played by distinct agents in \(U'\). If \(P\) is live in \(U'\) but not live in \(U\), that means upon combining the agents into one in \(U\), some nonlocal choice that was causing the conflict is now manifesting as a local choice in the combined history. However, according to our assumption, \(P\) is safe in the UoD; therefore there cannot be such a nonlocal choice. Hence, our assumption that \(P\) is not live in \(U\) must be false.

### 4.4 Reducing Splee to BSPL

In BSPL, the UoD for a protocol that contains \(R\) roles and \(M\) messages is given by \((R, M)\) [38]. Notably, a BSPL-UoD does not refer to agents, which makes static checking of liveness and safety possible for BSPL protocols. For Splee, we have mapped the problem of checking liveness and safety for arbitrary UoDs to distinct “small-model” canonical UoDs. However, we cannot yet perform static checking for Splee protocols because their canonical UoDs refer to agents. We now give a method for mapping a protocol’s canonical UoD to a BSPL-UoD. Recall that the canonical model has one agent for every nonset role and two agents for every set role. Let \(U\) be \(P\)’s canonical model. For a Splee protocol \(P\), we construct a BSPL protocol \(B\) that is identical to \(P\) except that each occurrence of a set role in \(P\) is substituted by two new roles in \(P\). The idea is that each of the new roles identifies an agent playing the original role in \(U\). For a message in \(P\), where the set role occurs, this means we replace it by two copies of the message (with distinct names) in \(B\), one for each of the new roles. The BSPL-UoD of \(B\) contains only the roles and messages that occur in \(B\). We refer to this construction as Splee-to-BSPL mapping.

**Theorem 5:** A protocol \(P\) is live (alogously, safe) in a canonical UoD iff its Splee-to-BSPL mapping \(B\) is live (alogously, safe).

**Proof.** By the construction above, which gets rid of agents but in doing so introduces a role for each agent and suitably modifies the messages as well so that they refer to the new roles. Hence, the set of viable history vectors in both UoDs is identical.

With this step (Theorem 5), we have given a method for statically verifying the liveness and safety of a Splee protocol in large UoDs by mapping it to a BSPL verification problem. Verification for strictly smaller UoDs (e.g., one where a set role is adopted by only one agent) can be performed by reduction to BSPL verification problems, as described above. However, smaller UoDs are oddities in the sense that set roles would have only singleton bindings or nonset roles would have no bindings.

### 5. QUERY ATTACHMENTS

Listing 7 does not constrain how the winner is determined—

in our auction, the binding for \(W\) must be the highest bidder and the binding for \(\text{wamt}\) must be its bid. This constraint could be captured as a norm specification, e.g., the auctioneer commits to choosing the bindings as described [13]. That is, at the Splee level, the auctioneer may announce anyone as the winner; however, at the meaning-level, the auctioneer’s commitment could be violated. Such a formulation would expand agent autonomy but diminish error checking.

Alternatively, to enhance error checking, we can constrain the bindings of "\(\text{out}\)" parameters via query attachments.

Since each message schema corresponds to a database relation, the parameters could be bound based upon the result of queries on message instances an agent has recorded in its (local) database [37]—any other bindings would be illegal. The queries can be written in a language compiles easily into SQL or another practical language. In Listing 8, \(\text{wamt}\) is constrained to be maximum \(\text{bamt}\) and \(W\) is constrained to the bidder who bid \(\text{wamt}\) in the SQL-like query attachment.

Listing 8: Building upon Listing 7, an auction protocol in Splee; winner is determined via a query attachment.

<table>
<thead>
<tr>
<th>Auction</th>
<th>.../* All of Winner (Listing 7) up to and including schema bids*/</th>
</tr>
</thead>
<tbody>
<tr>
<td>A → B:</td>
<td>(\text{wamt} ) in (\text{bids}) up to and including schema (\text{bids})</td>
</tr>
<tr>
<td>(\text{A})</td>
<td>: (\text{select this.wamt = ifnull (max(bamt), 'No bid') , this.W = ifnull ( max(wamt) , 'No bid') } )</td>
</tr>
<tr>
<td></td>
<td>from (\text{bid}) where (\text{nID} = \text{this.nID})</td>
</tr>
</tbody>
</table>

This tension between autonomy and error checking is the tension between regulation and regimentation [28], with error checking representing a higher degree of regimentation. The degree of regimentation is a design choice for protocol designers. In some situations, a designer may find it appropriate to introduce Splee query attachments so that certain kinds of errors are ruled out and desirable implementations are more easily constructed.

Notice that \(\text{win}\) can be sent when no bids have been received. In such a case, the query binds both \(W\) and \(\text{wamt}\) to the value No bid. Query attachments are not a way to control the flow of message instances. Instead, they should be regarded as a way to narrow the set of possible bindings for message instances an agent is allowed to emit. Intuitively, query attachments affect the viability of messages (Definition 4) in the same way that map constraints do. However, a formalization of attachments is out of our present scope.

### 6. CONCLUSION

Splee is a generalization of BSPL in the direction of dynamic role bindings and multicast. A fundamental enhancement is to make roles themselves information parameters that take agents as values. We introduced associated enhancements such as set roles and subroles, without which specifying important interaction patterns such as auctions would be impossible. We emphasize that although auctions have been specified and implemented in various multiagent languages and approaches e.g., [20, 33, 35], those are not protocol languages that support decentralized enactment. Finally, we introduced the idea of query attachments in order to constrain generated parameter bindings to specific values. The benefit of attachments is to simplify and make explicit the computation that agent developers would oth-
Meaning-based protocols. For example, a price
realize that the same operations may feature in multiple
meanings are distinct concerns. To see this, we need only
typically do not address decentralization, as Splee does.
[20], and AOSE methodologies such as Prometheus [34]—
[2, 21], process algebras [3], organization-oriented languages
have to implement multicast correctly in each agent. Mod-
multicast support in protocol languages, developers would
have to either hard code them in each agent or rely
on some external discovery mechanism. In the absence of
multicast support in protocol languages, developers would
to have implement multicast correctly in each agent. Mod-
eling applications via protocols is the essence of Interaction-
Oriented Software Engineering (IOSE) [14].

In programming frameworks such as JaCaMo [8], agents
communicate via a shared CArtAgo environment. Splee by
contrast is shared nothing; it conceptually avoids entities
such as an environment. In decentralized settings with one
CArtAgo component per agent with asynchronous messaging,
one would need Splee to specify how those components
interoperate. Supporting Splee in frameworks such as Ja-
CaMo, potentially by incorporating a middleware in the
form of protocol adapters [37], would considerably enhance
the capabilities of the frameworks.

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