Abstract—Recently, physical layer security has been recognized as a new design paradigm to provide security in wireless networks. In contrast to the existing conventional cryptographic methods, physical layer security exploits the dynamics of fading channels to enhance security of wireless communications. This paper studies optimization frameworks for a multicasting network in which a transmitter broadcasts the same information to a group of legitimate users in the presence of multiple eavesdroppers. In particular, the following optimization problems are investigated for a multicasting secrecy network: a) power minimization and b) secrecy rate maximization. First, the power minimization problem is solved for different numbers of legitimate users and eavesdroppers. Next, the secrecy rate maximization problem is investigated with the help of private jammers to improve the achievable secrecy rates through game theoretic approach. These jammers charge the transmitter for their jamming services based on the amount of the interference caused to the eavesdroppers. For a fixed interference price scenario, a closed-form solution for the optimal interference requirement to maximize the revenue of the transmitter is derived. This rate maximization problem for a non-fixed interference price scenario is formulated as a Stackelberg game where the jammers and transmitter are the leaders and follower, respectively. For the proposed game, a Stackelberg equilibrium is derived to maximize the revenues of both the transmitter and the private jammers. To support the derived theoretical results, simulation results are provided with different numbers of legitimate users and eavesdroppers. In addition, these results show that physical layer security based jamming schemes could be incorporated in emerging and future wireless networks to enhance the quality of secure communications.

Index Terms—Physical layer security, multicasting network, convex optimization, game theory.

I. INTRODUCTION

In traditional wireless networks, security is achieved in the upper layers based on conventional cryptographic methods. However, the broadcasting nature of wireless communications introduces different challenges in terms of key exchange and distribution. Recently, physical layer based secure communications has received considerable attention due to its suitability for dynamic network configurations and distributed processing techniques [1]–[3]. In addition, this approach implements security in the physical layer as a complement to the cryptographic methods by exploiting channel state information (CSI) of legitimate parties as well as eavesdroppers.

The ideas of physical layer security were first investigated in [4] and [5] based on information theoretic concepts by defining the secrecy capacity of wiretap channels. Recently, multiantenna secrecy channels have received considerable attention in the research community since the use of multiple antennas yield spatial diversity and additional degrees of freedom [6]–[14]. In [6], the secrecy capacity of multiple-antenna wiretap channels was presented with average power constraint, whereas the same secrecy capacity was established in [7] as the saddle point solution to a min-max problem. A transmit covariance matrix design was considered in [8] to maximize the ergodic secrecy rate with a power constraint for a multiple-input single-output (MISO) wiretap channel model, whereas an optimal transmit design through the semidefinite programming approach is proposed in [9] for the same channel model as in [8]. In [10], full rank solutions have been derived for the multiple-input multiple-output (MIMO) wiretap channel with an average power constraint and an alternative solution based on Taylor series has been proposed for the same problem in [11].

Cooperative jamming is a well known approach to further improve secrecy rates, where the jamming signals are introduced at the eavesdropper with the help of relays or jamming nodes [15]–[20]. This scheme degrades the eavesdropper’s capability of retrieving the information intended for the legitimate users. The achievable rates and an efficient cooperative jamming protocol have been presented for the general Gaussian multiple access and two-way wiretap channels in [16]. In [15], different cooperative jamming strategies have been developed for two-hop relay networks to confuse eavesdroppers with the assumption of global CSI. Opportunistic relaying for secret communications has been presented in [17] through cooperative jamming and relay chatting, whereas full-duplex jamming and optimal cooperative jamming for relays have been proposed in [18] and [19], respectively. On the other hand, jamming signals can be embedded in the transmitted signal from the legitimate transmitter to confuse the eavesdroppers, a strategy known as artificial noise (AN) technique in the literature [21]–[24]. In [22], a more general framework of AN methods has been presented for multi-antenna nodes. An AN scheme based on spatial selection has been proposed for MISO multi-eavesdropper secrecy rate maximization in [24] and a quality of service based beamforming scheme is has been proposed in [21] to employ AN.

Recently, game theoretic techniques have been incorporated into the study of secure wireless communications for decision
making and resource allocation, e.g., [25]–[31]. In [25], a novel cooperative paradigm has been proposed to improve the secrecy of primary users with the help of the secondary users in cognitive radio networks through a Stackelberg game approach. Secure games have been formulated for a secret communication network with an unfriendly jammer through a non-cooperative zero-sum continuous game in [26]. Physical layer security has been also investigated in a two way untrusted relay system through a Stackelberg game in [27]. In [28], a game theoretic framework has been developed for multi-hop networks in the presence of eavesdroppers. Transmission strategies have been proposed for MIMO secret communication networks in the presence of a multi-antenna eavesdropper through game theoretic approaches in [29], whereas a secrecy game for a Gaussian MISO interference channel has been investigated in [30].

In this paper, we consider a secure multicasting network as shown in Figure 1 where a transmitter broadcasts the same information to multiple legitimate users. To the best of the authors’ knowledge, there are only few works investigated multicasting secrecy network with multiple eavesdroppers in the literature. In [32], multicasting secrecy rate maximization was investigated for MISO channels with multiple eavesdroppers equipped with multiple antennas based on convex approximation techniques, whereas performance analysis has been derived for a secure multicasting network consisting of a single-antenna transmitter with multiple multi-antenna receivers as well as multiple multi-antenna eavesdroppers in [33]. In [34], a multicarrier based physical layer security scheme has been investigated for multicasting systems and a waveform design has been proposed for secure single-input single-output multicasting transmission in [35]. Recently, different capacities have been derived for secure multicasting in stochastic MIMO networks, whereas a joint beamforming and user selection scheme has been proposed for MISO wiretap channels with multiple single-antenna eavesdroppers in [36]. However, secure multicasting communications with cooperative jamming has not been considered in these works. In this paper, we propose different secrecy rate optimization frameworks with cooperative jamming, where a game theoretic approach is used to derive the optimal strategies between the legitimate transmitter and the jammers. The contributions of this paper are summarized as follows:

1) **Power minimization:** We consider a beamforming design for a secure communication network consisting of a legitimate user and an eavesdropper, where our goal is to minimize the transmit power with a secrecy rate constraint. This problem can be easily formulated as a second order cone programming (SOCP). Furthermore, we derive a closed-form optimal solution based on the dual problem and Karush-Kuhn-Tucker (KKT) conditions. The derived optimal solution is validated through a comparison with the SOCP results via simulations. Next, the power minimization problem is considered for a scenario with multiple legitimate users and multiple eavesdroppers. This problem is not convex in terms of the beamformer at the transmitter. However, we formulate this problem as a semidefinite programming by introducing a new variable and also using semidefinite relaxation.

2) **Game theory based secrecy rate maximization:** In the above power minimization schemes, the legitimate transmitter requires a certain amount of transmit power to satisfy the required secrecy rates. However, it is not always possible to realize the predefined secrecy rates, either because the available transmit power is limited or because it might be expensive to use the required amount of power. To overcome these issues, external jammers can be employed to introduce interference to the eavesdroppers, which will improve the achievable secrecy rate at the legitimate users. Therefore, we consider a multicasting secrecy network with multiple legitimate users and multiple eavesdroppers as shown in Figure 2 in which private jammers introduce interference to the eavesdroppers. Particularly, these private jammers charge the transmitter for their jamming service based on the amount of interference caused at the eavesdroppers. On the other hand, the legitimate users also pay the transmitter according to their achieved secrecy rates, which provides a profit to the transmitter and compensates for the charges of the private jammers. Based on the revenues at both transmitter and the private jammers, we formulate this problem as a Stackelberg game in which the private jammers and the transmitter are the *leaders* and the *follower*, respectively. For the proposed game, we derive a Stackelberg equilibrium solution with different numbers of legitimate users and eavesdroppers, which maximizes the revenues of the transmitter as well as the private jammers.

The remainder of the paper is organized as follows. The system model is described in Section II. Section III presents the power minimization problem with different numbers of legitimate users and eavesdroppers. The Stackelberg game is introduced in Section IV, whereas Stackelberg equilibrium solutions are derived for the proposed game in Section V for different scenarios. Section VI provides simulation results to support the theoretical results. Finally, Section VII concludes the paper.

**A. Notation**

We use upper case boldface letters for matrices and lower case boldface letters for vectors. $(\cdot)^T$ denotes conjugate transpose. $\text{Tr}(\cdot)$ and $\mathbb{E}\{\cdot\}$ stand for the trace of a matrix and the expectation for random variables. $A \succeq 0$ indicates that $A$ is a positive semidefinite matrix. $I$ denotes the identity matrix of appropriate size. $\| \cdot \|_2$ represents the Euclidean norm of a matrix. $[x]^+$ denotes $\max\{x, 0\}$.

**II. System Model**

We consider a multicasting secrecy network with $K$ legitimate users and $L$ eavesdroppers as shown in Figure 1, where a transmitter broadcasts the same information to all the legitimate users in the presence of multiple eavesdroppers. It is assumed that the transmitter is equipped with $N_T$ transmit antennas, whereas the legitimate users and the eavesdroppers have a single receive antenna. The channel coefficients between the legitimate transmitter and the $k^{th}$ legitimate user as
as follows:

\[ \text{loss + additive white Gaussian noise, the achievable secrecy rate at the } \]

The noise eavesdroppers are also legitimate members of the network, but requirements for the multicasting network being considered here, in which potential eavesdroppers are also legitimate members of the network, but do not have the permission to receive a particular multicast content being protected. This assumption has been widely used in the literature [2], [15], [19], [21], [37]–[42]. The noise power at the \( k \)-th legitimate user and the eavesdroppers is assumed to be \( \sigma_k^2 \) and \( \sigma_e^2 \), respectively. The received signals at the \( k \)-th legitimate user and \( l \)-th eavesdropper can be written as follows:

\[
y_k = h_k^H w s + n_k, \quad y_l = g_l^H w s + n_l, (1)
\]

where \( s (\mathbb{E}[s^2] = 1) \), and \( w \in \mathbb{C}^{N_T \times 1} \) are the signal intended to the legitimate users and the beamformer at the legitimate transmitter, respectively. \( n_k \) and \( n_l \) denote the noise at the \( k \)-th legitimate user and \( l \)-th eavesdropper, respectively. Assuming additive white Gaussian noise, the achievable secrecy rate at the \( k \)-th legitimate user is given by [7]

\[
R_k = \log \left( 1 + \frac{w^H h_k h_k^H w}{\sigma_k^2} \right) - \max_{1 \leq l \leq L} \log \left( 1 + \frac{w^H g_l g_l^H w}{\sigma_e^2} \right).
\]

III. SECRECY RATE OPTIMIZATIONS

In this section, we consider the power minimization problem for a multicasting secrecy network in which the transmitter provides the required secrecy rates for all the legitimate users in the presence of multiple active eavesdroppers. This problem can be formulated as an optimization framework in which the total transmit power is minimized to satisfy the secrecy rate constraints.

A. Power Minimization

First, the power minimization problem is investigated with a single legitimate user and an eavesdropper. For this problem, a closed-form optimal solution can be derived based on the dual problem and KKT conditions. For the scenario of multiple legitimate users in the presence of multiple eavesdroppers, it is formulated into a semidefinite programming framework through semidefinite relaxation.

Single Legitimate User and Single Eavesdropper

With a single legitimate user and a single eavesdropper, the power minimization problem can be formulated with the secrecy rate constraint as follows:

\[
\min_w \|w\|_2^2 \\
\text{s.t. } \log \left( 1 + \frac{w^H h_1 h_1^H w}{\sigma_1^2} \right) - \log \left( 1 + \frac{w^H g_1 g_1^H w}{\sigma_e^2} \right) \geq \bar{R}_s, (2)
\]

where \( h_1 \) and \( g_1 \) are the channels between the legitimate transmitter and the legitimate user as well as the eavesdropper, respectively. In addition, \( \bar{R}_s \) is the required secrecy rate of the legitimate user. The problem in (2) can be formulated into a SOCP problem. However, we derive a closed-form optimal solution based on the dual problem and KKT conditions. In the simulation section, we validate this closed-form solution by comparing it with SOCP results.

Lemma 1: The optimal solution of (2) is given by

\[
w^* = \sqrt{p^*} \tilde{w}^*, \quad \tilde{w}^* = \frac{w_1}{\|w_1\|_2}, \quad w_1 = v_{\max} \left( \tilde{h}_1 \tilde{h}_1^H - 2 \bar{R}_s \tilde{g}_1 \tilde{g}_1^H \right)^{1/2},
\]

where \( \tilde{h}_1 = h_1 / \sigma_1 \), \( \tilde{g}_1 = g_1 / \sigma_e \), and \( \lambda_{\max}(\cdot) \) denote the maximum eigenvalue and the eigenvector corresponding to the maximum eigenvalue, respectively.

Proof: Please refer to Appendix A.

Multiple Legitimate Users and Multiple Eavesdroppers

The power minimization problem with multiple legitimate users and multiple eavesdroppers can be formulated as

\[
\min_w \|w\|_2^2 \\
\text{s.t. } \log \left( 1 + \frac{w^H h_k h_k^H w}{\sigma_k^2} \right) - \max_{1 \leq l \leq L} \log \left( 1 + \frac{w^H g_l g_l^H w}{\sigma_e^2} \right) \geq \bar{R}_k, \\
k = 1, \cdots, K, \quad l = 1, \cdots, L, (4)
\]

where \( \bar{R}_k \) is the target secrecy rate of the \( k \)-th legitimate user. This problem is not convex in terms of the transmit beamformer. However, by introducing a new semidefinite matrix \( W = \text{ww}^H \) and relaxing the rank-one constraint, the above problem can be formulated into a semidefinite programming (semidefinite relaxation) as follows:

\[
\min_{W \succeq 0} \text{Tr}\{W\} \\
\text{s.t. } 1 + \text{Tr}\{\tilde{h}_k \tilde{h}_l^H W\} - 2 \bar{R}_k \text{Tr}\{\tilde{g}_l \tilde{g}_l^H W\} \geq 2 \bar{R}_l, \\
k = 1, \cdots, K, \quad l = 1, \cdots, L, (5)
\]

where \( \tilde{h}_k = h_k / \sigma_k \) and \( \tilde{g}_l = g_l / \sigma_e \). If the solution of the above problem is rank-one, then it will be the optimal solution of the original problem in (4). In case of a non-rank-one solution, randomization techniques can be used to construct a rank-one solution from the non-rank-one solution of (5) [43], [44].

IV. GAME THEORY BASED SECRECY RATE OPTIMIZATION

In order to satisfy the target secrecy rates, the transmitter requires a certain amount of transmit power. However, it
is not always possible to provide the target secrecy rates due to limited transmit power or because it might require a significant amount of transmit power which will be infeasible in terms of hardware implementations at the transmitter. On the other hand, in multicasting networks, it is difficult to achieve the target secrecy rates at different legitimate users with a single beamformer. To overcome these issues, cooperative jamming would be a solution, which will enhance the secrecy performance at the legitimate users. Here, we consider a multicasting secrecy network in which a set of private (friendly) jammers are employed to provide jamming services as shown in Figure 2. These private jammers introduce interference to the eavesdroppers who overhear the multicasting transmission from the transmitter. In addition, these jammers ensure that there is no interference leakage to the legitimate users, which could be achieved by appropriately designing the beamformers at the jammers and employing a dedicated jammer near to each eavesdropper. Since, a dedicated jammer is closely located to the corresponding eavesdropper, each eavesdropper receives interference only from the corresponding private jammer\(^1\). These private jammers charge the transmitter for their dedicated jamming service based on the amount of interference caused to each eavesdropper. To compensate these interference prices, the legitimate transmitter also introduces charges to the legitimate users for its enhanced secured service based on the achieved secrecy rates. For this scenario, we consider secrecy rate maximization with multiple legitimate users, multiple eavesdroppers and multiple corresponding jammers. We formulate this problem as a Stackelberg game and then investigate the Stackelberg equilibrium for the proposed game. A Stackelberg game consists of two set of players, namely, leaders and followers, where both of them try to maximize their revenues or profits. The leaders make a move first and then followers will move according to the leaders’ strategy. The leaders (private jammers) announce a set of unit interference prices for each eavesdropper. Then, the follower (transmitter) decides on the interference requirements at the eavesdroppers according to the interference prices.

\(^1\)Here, it is assumed that the jammers have the perfect CSI of the corresponding eavesdroppers. This is a reasonable assumption, since the eavesdroppers might be also part of the system [15], [19], [21].

### A. Stackelberg Game

The interference received at the \(l\)th eavesdropper from the corresponding private jammer can be written as follows:

\[
I_l = p_l |g_{jl}|^2,
\]

where \(|g_{jl}|^2\) is the power gain between the corresponding private jammer and the \(l\)th eavesdropper and the power allocation at the \(l\)th private jammer is represented by \(p_l\). Here, we are only interested in the power allocation policy at the jammer, where the beamformer at the jammer is appropriately designed with no interference leakage to the legitimate users and hence interference is introduced only to the corresponding eavesdropper.

The private jammers’ objective is to maximize their revenue by selling interference to the transmitter. The revenue of the \(l\)th private jammer can be written as follows:

\[
\phi_l(\mu_l, p_l) = \mu_l p_l |g_{jl}|^2,
\]

where \(\mu_l\) is the unit interference price charged by the corresponding jammer to cause interference at the \(l\)th eavesdropper. Depending on the interference requirement at the \(l\)th eavesdropper, the interference price should be determined by the corresponding jammer to maximize its revenue. The prices for interference at each eavesdropper can be obtained by solving the following optimization problem:

\[
\text{Problem (A): } \max_{\mu_l \geq 0} \sum_{l=1}^{L} \phi_l(\mu_l, p_l), \tag{8}
\]

where \(\mu = [\mu_1 \cdots \mu_L]\) represents the interference prices for all the eavesdroppers.

At the same time, the transmitter should maximize its utility by introducing a price for secret communication established between the transmitter and the corresponding legitimate users. The revenue function at the transmitter can be written as

\[
\psi_L(p, \mu) = \sum_{k=1}^{K} \lambda_k R_k - \sum_{l=1}^{L} \mu_l p_l |g_{jl}|^2, \tag{9}
\]

where \(\lambda_k\) and \(R_k\) are the unit price for the secrecy rate and the achievable secrecy rate at the \(k\)th user, respectively. In addition, it is assumed that the unit price for the secrecy rate for each user is fixed to a certain value. Hence, the transmitter should determine the beamforming vector and decide the interference requirements at different eavesdroppers to maximize its revenue. However, we are only interested in determining the interference requirements at each eavesdropper for a given beamformer at the transmitter. This problem can be formulated as follows:

\[
\text{Problem (B): } \max_{p \geq 0} \psi_L(p, \mu), \tag{10}
\]

where \(p = [p_1 \cdots p_L]\) represents the power allocation policy at all jammers.

\textbf{Problem (A) and Problem (B) form a Stackelberg game, in which the jammers (leaders) announce the interference prices at each eavesdropper and then the transmitter (follower) determines the required amount of interference to each eavesdropper. The solution of this game can be obtained by investigating the Stackelberg equilibrium, at which the}
transmitter and the jammers come to an agreement on the interference requirements and the interference price at each eavesdropper. The deviation of either the transmitter or the jammers from this equilibrium will introduce loss in their revenues.

B. Stackelberg Equilibrium

The Stackelberg equilibrium for the proposed game is defined as follows:

Problem (B), whereas \( \mu^* \) contains the best prices for Problem (A). The solutions \( p^* \) and \( \mu^* \) define the Stackelberg equilibrium point if the following conditions are satisfied for any set of \( p \) and \( \mu \):

\[
\psi_L(p^*, \mu^*) \geq \psi_L(p, \mu^*), \quad \phi_l(p^*_l, \mu^*_l) \geq \phi_l(p^*_l, \mu_l), \forall l.
\]

V. STACKELBERG EQUILIBRIUM SOLUTION

In this section, we derive Stackelberg equilibrium solutions for the proposed game described in the previous section with different numbers of legitimate users and eavesdroppers. First, the best response of the transmitter is derived in terms of power allocation at the jammers for fixed interference prices. Then, the optimal interference prices are obtained to maximize the revenue of the jammers. In order to obtain the Stackelberg equilibrium points, the best responses of the follower (transmitter) and the leaders (jammers) should be obtained by solving Problem (B) and Problem (A), respectively. Since, the leaders (jammers) derive the optimal interference prices decided by the interference requirements from the legitimate transmitter, the best response function of the follower should be derived first in terms of the interference requirements. For the proposed game, Stackelberg equilibrium can be derived by obtaining \( p^* \) from Problem (B) first and then by obtaining the best interference prices \( \mu^* \) from Problem (A). In the following subsections, we solve the proposed Stackelberg game with different numbers of legitimate users and eavesdroppers.

A. Single Legitimate User and Single Eavesdropper

In this subsection, the proposed game is considered with a single legitimate user and an eavesdropper. First, the optimal interference requirement (best response) at the transmitter is obtained to maximize its revenue for the fixed interference price at the jammer. Then, a Stackelberg equilibrium is derived for this game where both legitimate transmitter and the jammer attain an equilibrium by achieving their maximum revenues.

Fixed Interference Price

Here, the optimal interference requirement is obtained for a fixed interference price at the jammer. For a given beamformer at the transmitter, the achievable secrecy rate of the legitimate user in the presence of an eavesdropper is defined as

\[
R_{SL-SE} = \log(1 + \beta_0) - \log \left( 1 + \frac{\beta_1}{\sigma^2 + p_1 \alpha_1} \right), \quad \beta_0 = \frac{w^H h_i h_i^H w}{\sigma^2}, \beta_1 = w^H g_j g_j^H w, \quad \alpha_1 = |g_{j1}|^2.
\]

Hence, the optimal interference requirement at the eavesdropper can be obtained by solving the following optimization problem:

\[
\max_{p_1 \geq 0} \lambda_1 R_{SL-SE} - \mu_1 p_1 \alpha_1,
\]

where \( p_1 \) is the power allocation policy at the corresponding jammer. This problem is convex and the corresponding proof has been provided in the next subsection. Hence, the optimal power allocation can be obtained through standard interior point methods [45]. However, we derive the closed-form solution for the power allocation \( p_1 \) to realize the Stackelberg equilibrium in the following subsection.

Stackelberg Game

In this subsection, we derive the Stackelberg equilibrium with a legitimate user and an eavesdropper. To obtain this equilibrium, the best response (i.e., \( p^*_1 \)) of the follower (transmitter) is derived for a given interference price \( \mu_1 \), since the leader (jammer) derives its best response from the interference requirement decided by the follower (transmitter). Note that a closed-form solution for the best response should be obtained to derive the Stackelberg equilibrium of the proposed game. The best response of the follower can be obtained by solving the following problem:

\[
\max_{p_1 \geq 0} \psi_{SL-SE}(p_1, \mu_1),
\]

where \( \psi_{SL-SE}(p_1, \mu_1) \) is the revenue function for the transmitter and is defined in (15) at the top of the next page. \( \lambda_1 \) and \( \mu_1 \) are the unit prices for the secrecy rate at the legitimate user and the cost for the interference introduced at the eavesdropper.

The optimal interference requirement for a given \( w \) and \( \mu_1 \) can be obtained by solving the following problem:

\[
\max_{p_1 \geq 0} \lambda_1 \left[ \log(1 + \beta_0) - \log \left( 1 + \frac{\beta_1}{\sigma^2 + p_1 \alpha_1} \right) \right] - \mu_1 p_1 \alpha_1.
\]

where

\[
\beta_0 = \frac{w^H h_i h_i^H w}{\sigma^2}, \quad \beta_1 = w^H g_j g_j^H w \quad \text{and} \quad \alpha_1 = |g_{j1}|^2.
\]

Lemma 2: The optimal interference requirement from the jammer with a given interference price \( \mu_1 \) is given by

\[
p_1^* = \frac{1}{\alpha_1} \left[ \sqrt{\frac{\beta_0^2}{4} + \frac{\lambda_1 \beta_1}{\mu_1}} - \frac{2(\sigma^2 + \beta_1)}{2} \right]
\]

Proof: Please refer to Appendix B.

Corollary 1: With a given \( w \) and \( \mu_1 \), the interference price \( \mu_1 \) is bounded as follows:

\[
\mu_1 \leq \frac{\lambda_1 \beta_1}{\sigma^2 (\sigma^2 + \beta_1)}.
\]

Since \( p_1 \geq 0 \),

\[
\sqrt{\frac{\beta_0^2}{4} + \frac{\lambda_1 \beta_1}{\mu_1}} \geq \frac{2(\sigma^2 + \beta_1)}{2} \Rightarrow \mu_1 \leq \frac{\lambda_1 \beta_1}{\sigma^2 (\sigma^2 + \beta_1)}.
\]

We have thus obtained the optimal interference requirement at the eavesdropper to maximize the revenue of the legitimate transmitter. The jammer should announce the optimal unit
interference price $\mu_1$ to maximize its revenue by selling the interference to the transmitter. The optimal unit interference price can be obtained by solving the following optimization problem:

$$\max_{\mu_1 \geq 0} \phi_1(p_1^*, \mu_1) = \mu_1 p_1^* \alpha_1$$  \hfill (21)

**Lemma 3**: The optimal unit interference price $\mu_1$ is given as follows:

$$\mu_1^* = \frac{c_2}{2c_1} \left( \frac{c_0}{\sqrt{c_0^2 - c_1}} - 1 \right),$$  \hfill (22)

where

$$c_0 = \frac{(2\sigma_e^2 + \beta_1)}{2\alpha_1}, \quad c_1 = \frac{\beta_e^2}{4\alpha_1^2} \text{ and } c_2 = \frac{\lambda_1 \beta_1}{\alpha_1^2}. \hfill (23)$$

**Proof**: Please refer to Appendix C. 

Hence, a Stackelberg equilibrium for the proposed game with a single legitimate user and an eavesdropper is $(p_1^*, \mu_1^*)$. The deviation from this equilibrium point will cause loss to both the follower (legitimate transmitter) and leader (jammer). Hence, both of them will operate at this Stackelberg equilibrium to maximize their revenues.

**Proposition 1**: There is a unique Nash equilibrium for the proposed game and the derived Stackelberg equilibrium solution achieves this unique Nash equilibrium.

**Proof**: As mentioned before, the revenue function of the legitimate transmitter is a concave function of the power allocation policy at the jammer. Hence, the optimal and unique jammer power allocation policy has been derived for a given interference price. Similarly, the revenue function of the jammer is also a concave function in terms of the interference price which results in an optimal and unique interference price. Since, both solutions are unique and optimal, this equilibrium achieves a unique Nash equilibrium for the proposed game. 

B. Multiple Legitimate Users and Single Eavesdropper

In this subsection, we extend the proposed game to the scenario with multiple legitimate users and a single eavesdropper. As in the previous subsection, first, the optimal interference requirement is obtained for a fixed interference price and then, a Stackelberg equilibrium is derived for the proposed game.

**Fixed Interference Price**

The achievable secrecy rate of the $i$th user can be defined as

$$R_{SL-SE}^{(i)} = \log(1 + \beta_i) - \log \left( 1 + \frac{\beta_e}{\sigma_e^2 + p_i \alpha_1} \right).$$  \hfill (24)

where

$$\beta_i = \frac{w_i^H h_i h_i^H w}{\sigma_e^2}, \quad \beta_e = w_i^H g_i^H g_i^H w \quad \alpha_1 = |g_1|^2.$$  \hfill (25)

The optimal power allocation policy at the jammer for a fixed interference price can be formulated as

$$\max_{\mu_1 \geq 0} \sum_{i=1}^{K} \lambda_i R_{SL-ME}^{(i)} - \mu_1 p_2^* \alpha_1.$$  \hfill (26)

**Lemma 4**: The optimal power allocation policy at the jammer to maximize the revenue at the legitimate transmitter is given by

$$p_2^* = \frac{1}{\alpha_1} \left( \sqrt{\frac{\beta_e^2}{4} + \frac{\beta_e}{\mu_1} \left( \sum_{i=1}^{K} \lambda_i \right)} - \frac{\lambda_1 \beta_1}{\alpha_1^2} \right).$$  \hfill (27)

**Proof**: The proof is similar to that of Lemma 2.

**Stackelberg Game**

In order to derive the Stackelberg equilibrium with multiple legitimate users and an eavesdropper, the best response of the jammer should be obtained by solving the following problem:

$$\max_{p_2, \mu_2} \phi_2(p_2, \mu_2) = \mu_2 p_2^* \alpha_1$$  \hfill (28)

**Lemma 5**: The optimal unit interference price $\mu_2$ is given as follows:

$$\mu_2^* = \frac{c_2}{2c_1} \left( \frac{c_0}{\sqrt{c_0^2 - c_1}} - 1 \right),$$  \hfill (29)

where

$$c_0 = \frac{(2\sigma_e^2 + \beta_e)}{2\alpha_1}, \quad c_1 = \frac{\beta_e^2}{4\alpha_1^2} \text{ and } c_2 = \frac{\beta_e}{\alpha_1^2} \sum_{i=1}^{K} \lambda_i.$$  \hfill (30)

**Proof**: The proof is similar to that of Lemma 3.

Hence, the Stackelberg equilibrium of the proposed game with multiple legitimate users and single eavesdropper is defined as $(p_2^*, \mu_2^*)$.

C. Single Legitimate User and Multiple Eavesdroppers

Here, the proposed game is investigated with a single legitimate user and multiple eavesdroppers. This problem is different from the above problems due to the fact that there are the multiple active eavesdroppers. As in the previous subsection, first the fixed-interference scenario is solved, followed by the derivation of the Stackelberg equilibrium of the proposed game.

**Fixed Interference Prices**

The achievable secrecy rate with multiple eavesdroppers can be defined as

$$R_{SL-ME} = \log(1 + \beta_0) - \max_{1 \leq i \leq L} \log \left( 1 + \frac{\beta_i}{\sigma_e^2 + p_i \alpha_1} \right).$$  \hfill (31)

where

$$\beta_0 = \frac{w_i^H h_i h_i^H w}{\sigma_e^2}, \quad \beta_i = w_i^H g_i^H g_i^H w \quad \alpha_1 = |g_1|^2.$$  \hfill (32)

Note that all the eavesdroppers may not necessarily influence the achievable secrecy rate at the legitimate user. The eavesdropper with the highest achieved rate will determine the
achieved secrecy rate of the legitimate user. By introducing jamming to this eavesdropper, the secrecy rate can be improved by reducing the achievable rate at the corresponding eavesdropper. After this jamming, another eavesdropper might now have the highest achievable rate which will deteriorate the achievable secrecy rate of the legitimate user. Hence, it is important to jam this eavesdropper in order to match the achieved rate of the previous eavesdropper. Therefore, only a set of eavesdroppers require the interference from the jammers and the rest of them do not need any interference from the jammers, since their impact on the secrecy rate is not dominant. Here, we divide these eavesdroppers into two sets, namely, super-active and non-super active eavesdroppers. The eavesdroppers who receive interference from the jammers and determine the achievable secrecy rate of the legitimate user are called super-active eavesdroppers and the rest of them are defined as non-super active eavesdroppers. In order to improve the revenue of the legitimate transmitter, the optimal interference requirements problem can be formulated as follows:

\[
\max_{\mathbf{p} \geq 0, \ t_i, \ t_0} \lambda_1 R_{SL-ME} = \sum_{i \in \mathbb{K}} \mu_i p_i \alpha_i, \tag{33}
\]

where vector \( \mathbf{p} = \{p_i \mid i \in \mathbb{K}\} \) represents the power allocations of private jammers in the set \( \mathbb{K} \) consisting of all super-active eavesdroppers. The optimal interference requirements from private jammers corresponding to the super-active eavesdroppers can be obtained by formulating the problem as follows:

\[
\max_{\mathbf{p} \geq 0, \ t_i, \ t_0} \lambda_1 \left[ \log(1 + \beta_i) - t_0 \right] - \sum_{i \in \mathbb{K}} \mu_i p_i \alpha_i \\
\text{s.t. } \log \left(1 + \frac{\beta_i}{\sigma_e^2 + p_i \alpha_i} \right) \leq t_i, \ i \in \mathbb{K} \\
\max \{t_i \mid i \in \mathbb{K}\} = t_0, \ t_i \geq 0, \ i \in \mathbb{K}. \tag{34}
\]

The problem in (34) is convex in \( \mathbf{p} \) and can be easily solved by interior point methods. However, one issue might arise how to obtain the super-active eavesdroppers’ set \( \mathbb{K} \) from all available active eavesdroppers. This can be addressed by solving the following optimization problem:

\[
\max_{\mathbf{p} \geq 0, \ t_i, \ t_0} \lambda_1 \left[ \log(1 + \beta_i) - t_0 \right] - \sum_{i = 1}^{L} \mu_i p_i \alpha_i \\
\text{s.t. } \log \left(1 + \frac{\beta_i}{\sigma_e^2 + p_i \alpha_i} \right) \leq t_i, \ \forall \ i \\
\max \{t_i, \ldots, t_L\} = t_0, \ t_i \geq 0, \ \forall \ i, \tag{35}
\]

where the super-active eavesdroppers’ set \( \mathbb{K} \) is removed and all the available eavesdroppers have been incorporated into the optimization problem.

**Proposition 2:** At the optimal solution of (35), the achieved rates of the super-active eavesdroppers (i.e., \( t_i, \ i \in \mathbb{K} \)) will be equal and power allocations \( p_i s \) of non-super-active eavesdroppers (i.e., \( i \notin \mathbb{K} \)) will be all zeros.

**Proof:** Assume that \( t_i, \ i \in \mathbb{K} \) are not equal. Let consider the minimum \( t_i = t_{\min} < t_0 \) from all \( t_i, \ i = 1, \ldots, L, \) and the corresponding \( p_i \) will be higher than that of \( t_{\min} = t_0. \) Hence, the revenue of the transmitter (cost function of (35)) with \( t_i = t_{\min} \) will be less than that with \( t_i = t_0. \) Thus, the achieved rates of the super-active eavesdroppers (i.e., \( t_i, i \in \mathbb{K} \)) will be equal at the optimal solution and the power allocations strategy corresponding to the non-super-active eavesdroppers (i.e., \( i \notin \mathbb{K} \)) will be zeros.

Therefore, the optimal interference requirements from the private jammers with fixed interference prices can be obtained by solving the convex problem in (35).

**Stackelberg Game**

As in the previous subsections, this problem is formulated as a Stackelberg game and the Stackelberg equilibrium is defined for the proposed game. The best response of the transmitter for a given set of interference prices can be determined by solving the following problem:

\[
\max_{\mathbf{p} \geq 0} \lambda_1 R_{SL-ME} - \sum_{i \in \mathbb{K}} \mu_i p_i \alpha_i, \tag{36}
\]

where \( \mathbf{p} \) represents power allocations of the private jammers in the set \( \mathbb{K} \) which is the set consisting of all the super-active eavesdroppers. This problem can be formulated into a convex problem as in (35) and the optimal power allocation strategy can be obtained. However, it is necessary to find a closed-form solution to derive a Stackelberg equilibrium for the proposed game.

**Lemma 6:** The optimal power allocation policy at the \( i^{th} \) jammer is given by

\[
p_i^* = \frac{1}{\alpha_i} \left( \frac{\beta_i}{\gamma_0} - \sigma_e^2 \right)^+, \tag{37}
\]

where

\[
\beta_i = w^H g_i g_i^H w, \tag{38}
\]

\[
\gamma_0 = \sum_{i=1}^{K} \mu_i \beta_i + \sqrt{\sum_{i=1}^{K} \mu_i \beta_i \left( 4\lambda_1 + \sum_{i=1}^{K} \mu_i \beta_i \right)} \tag{39}
\]

**Proof:** Please refer to Appendix D.

The optimal interference requirement has been derived to maximize the transmitter’s revenue for a given set of interference prices. However, the jammers should announce their optimal interference prices to maximize their revenues. The optimal interference price can be obtained by solving the following problem:

\[
\max_{\mu \geq 0} \sum_{i=1}^{L} \phi_i(p_i^*, \mu_i) = \sum_{i=1}^{L} \mu_i p_i^* \alpha_i. \tag{40}
\]

By substituting the optimal power allocations \( p_i^* s \) in (37) in terms of the interference prices \( \mu_i s, \) the above optimization problem can be rewritten as

\[
\max_{\mu \geq 0} \frac{2\lambda_1 \sum_{i=1}^{K} \mu_i \beta_i}{\sum_{i=1}^{K} \mu_i \beta_i + \sqrt{\sum_{i=1}^{K} \mu_i \beta_i \left( 4\lambda_1 + \sum_{i=1}^{K} \mu_i \beta_i \right)}} = \sigma_e^2 \sum_{i=1}^{K} \mu_i. \tag{41}
\]

It is very difficult to find a closed form solution for the optimal interference prices \( \mu_i s \) and the problem in (40) might be solved
using existing numerical methods. However, we can find a closed-form solution, if we assume that each private jammer announces the same interference prices (i.e., \( \mu_1 = \mu_2 = \cdots = \mu_L = \mu_0 \)). For this uniform interference price scenario, the optimization problem in (40) can be modified as

\[
\max_{\mu_0 \geq 0} \frac{2 \lambda_t \mu_0 \sum_{i=1}^{K} \beta_i + \sqrt{\mu_0 \sum_{i=1}^{K} \beta_i \left( 4 \lambda_t + \mu_0 \sum_{i=1}^{K} \beta_i \right)}}{K \sigma_e^2 \mu_0} - K \sigma_e^2 \mu_0
\]

(41)

**Lemma 7:** The optimal interference price \( \mu_0^* \) in (41) is given by

\[
\mu_0^* = \frac{0.5 \left[ -4 \lambda_t K \sigma_e^2 \eta_1 + 2 \lambda_t \sqrt{K \sigma_e^2 \eta_2 + 4 K^2 \sigma_e^4 \eta_2^2} \right]}{K \sigma_e^2 \eta_2}
\]

where

\[
\eta_1 = \left( 1 + \frac{K \sigma_e^2}{\bar{c}_2} \right), \quad \eta_2 = (\bar{c}_2 + K \sigma_e^2), \quad \bar{c}_2 = \sum_{i=1}^{K} \beta_i.
\]

(42)

**Proof:** Please refer to Appendix E.

The Stackelberg equilibrium of the proposed uniform price game with a single legitimate user and multiple eavesdroppers is given by \( (p_i^*, \mu_0^*) \). By using this equilibrium solution, both the legitimate transmitter and the jammers achieve their maximum revenues.

**D. Multiple Legitimate Users and Multiple Eavesdroppers**

In this subsection, the proposed game is extended to the scenario with multiple legitimate users and multiple eavesdroppers. As in the previous subsections, the fixed interference price scenario and Stackelberg game are investigated.

**Fixed Interference Prices**

The achievable secrecy rate of the \( i \)-th user can be defined as

\[
R_{ML-ME}^{(i)} = \log \left( 1 + \beta_0^{(i)} \right) - \max_{1 \leq L \leq K} \log \left( 1 + \frac{\beta_i}{\sigma_e^2 + p_i \alpha_i} \right),
\]

(44)

where

\[
\beta_0^{(i)} = \frac{w^H h_i h_i^H w}{\sigma_e^2}, \quad \beta_i = w^H g_i^H g_i w.
\]

(45)

As mentioned in the previous subsection, all the eavesdroppers might not be active due to the different achieved rates. By considering only super-active eavesdroppers, the optimal interference requirements can be obtained by solving the following problem:

\[
\max_{\mu_0 \geq 0} \sum_{i=1}^{K} \lambda_i R_{SL-ME}^{(i)} = \sum_{i \in \mathcal{K}} \mu_i p_i \alpha_i,
\]

(46)

where the vector \( p \) represents power allocations of private jammers in the set \( \mathcal{K} \) which is the set consisting of all the active eavesdroppers. As in the previous subsection, the optimal interference requirements can be obtained by considering both super-active and non-super-active eavesdroppers through the following problem:

\[
\max_{p \geq 0, \ t_i, \ t_0} \sum_{i=1}^{K} \lambda_i \left[ \log \left( 1 + \beta_0^{(i)} \right) - t_i \right] - \sum_{i=1}^{L} \mu_i p_i \alpha_i
\]

s.t.

\[
\log \left( 1 + \frac{\beta_i}{\sigma_e^2 + p_i \alpha_i} \right) \leq t_i, \ \forall \ i
\]

\[
\max \{ t_1, \cdots, t_L \} = t_0, \ \forall \ i, \ t_i \geq 0, \ \forall \ i
\]

(47)

At the optimal solution of (47), the achieved rates of the super-active eavesdroppers will be equal and power allocations corresponding to the non-super-active eavesdroppers will be zeros, where the corresponding proof is similar to that of Proposition 2.

**Stackelberg Game**

Here, we solve the Stackelberg game for the scenario with multiple legitimate users and multiple eavesdroppers. The derivation of the Stackelberg equilibrium is similar to that of the scenario with a single legitimate user and multiple eavesdroppers. The best response of the legitimate transmitter can be obtained by solving the following problem:

\[
\max_{p \geq 0} \sum_{i=1}^{K} \lambda_i R_{ML-ME}^{(i)} = \sum_{i \in \mathcal{K}} \mu_i p_i \alpha_i,
\]

(48)

where the vector \( p \) consists of all the power allocations of the jammers corresponding to the super-active eavesdroppers.

**Lemma 8:** The optimal power allocation strategy at the \( i \)-th jammer is given by

\[
p_{ML-ME}^* = \frac{1}{\alpha_i} \frac{\beta_i}{\gamma_1 - \sigma_e^2}^+, \quad \gamma_1 = \frac{\sum_{i=1}^{K} \mu_i \beta_i + \sqrt{\sum_{i=1}^{K} \mu_i \beta_i \left( 4 \sum_{i=1}^{K} \lambda_i + \sum_{i=1}^{K} \lambda_i \beta_i \right)}}{2 \sum_{i=1}^{K} \lambda_i}
\]

(49)

**Proof:** The proof is similar to that of Lemma 6.

For this interference requirement, the jammers should determine their optimal interference prices to maximize their revenues which can be obtained by solving the following problem:

\[
\max_{\mu_0 \geq 0, \ t_i, \ t_0} \sum_{i=1}^{K} \lambda_i R_{SL-ME}^{(i)} = \sum_{i \in \mathcal{K}} \mu_i p_i \alpha_i.
\]

(50)

However, it is difficult to find the closed-form optimal solution for the problem in (50) with different interference prices \( \mu_i \)s at each jammer. In the case of the uniform interference price (i.e., \( \mu_1 = \mu_2 = \cdots = \mu_L = \mu_0 \)), the problem in (50) can be modified as follows:

\[
\max_{\mu_0 \geq 0, \ t_i, \ t_0} \sum_{i=1}^{K} \lambda_i \left[ \log \left( 1 + \frac{\beta_i}{\sigma_e^2 + p_i \alpha_i} \right) - t_i \right] - \sum_{i=1}^{L} \mu_i p_i \alpha_i
\]

\[
- K \sigma_e^2 \mu_0
\]

(51)

where

\[
\beta_i = \frac{2 \mu_0 \bar{c}_3 \bar{c}_2}{\mu_0 \bar{c}_2 + \sqrt{\mu_0 \bar{c}_2 \left( 4 \bar{c}_3 + \mu_0 \bar{c}_2 \right)}} - K \sigma_e^2 \mu_0
\]

(52)

\[
\bar{c}_2 = \sum_{i=1}^{K} \beta_i, \quad \bar{c}_3 = \sum_{i=1}^{K} \lambda_i.
\]

**Lemma 9:** The optimal interference price \( \mu_0^* \) is given by

\[
\mu_0^* = \frac{0.5 \left[ -4 K \sigma_e^2 \eta_1 + 2 \bar{c}_3 \sqrt{K \sigma_e^2 \eta_2 + 4 K^2 \sigma_e^4 \eta_2^2} \right]}{K \sigma_e^2 \eta_2}
\]

(53)
where
\[ \eta_1 = 1 + \frac{K \sigma^2}{c_2}, \quad \eta_2 = c_2 + K \sigma^2. \] (54)

Proof: The proof is similar to that of Lemma 7. □

Hence, a Stackelberg equilibrium of the proposed game with multiple legitimate users and multiple users is defined by \( (p_1^{* \text{ML-ME}}, \forall i, p_i^{* \text{ML-ME}}) \) which provides the maximum revenues for both the legitimate transmitter and the private jammers.

VI. SIMULATION RESULTS

In this section, we provide simulation results to support the theoretical results derived in the previous sections. In order to evaluate the performance of the proposed schemes, we consider a multicasting secrecy network in which the transmitter broadcasts the same information to all the legitimate users in the presence of multiple eavesdroppers. In addition, private jammers are employed to confuse the eavesdroppers by introducing interference in order to improve the secrecy rates at the legitimate users. The legitimate transmitter is equipped with three antennas, whereas the legitimate users and the eavesdroppers have a single-antenna. The unit secrecy rate price has been set to 5 (i.e., \( \lambda_1 = 5 \)). In this secrecy network, all channels have been generated using zero-mean circularly symmetric independent and identically distributed complex Gaussian random variables. The noise power at all the terminals has been assumed to be 0.1.

A. Power Minimization

In this subsection, we provide simulation results to support the closed-form results derived in (3) for the scenario with a single legitimate user and an eavesdropper. As mentioned before, the original power minimization problem can be formulated into a convex optimization (SOCP) framework. However, we derived a closed-form solution in (3). We have obtained the required transmit power and the corresponding beamformer based on the closed-form solution as well as the convex optimization framework for different sets of channels as provided in Table 1 where the target secrecy rate has been set to 3.5. As seen in Table 1, both results are the same which validates the accuracy of the closed-form solution in (3). Due to space limitation, the performance for the corresponding beamformers as well as the simulation results for the case with multiple legitimate users and multiple eavesdroppers are not provided here.

<table>
<thead>
<tr>
<th>Channels</th>
<th>Required Transmit Power</th>
</tr>
</thead>
<tbody>
<tr>
<td>Channel 1</td>
<td>Closed Form</td>
</tr>
<tr>
<td>Channel 2</td>
<td>Closed Form</td>
</tr>
<tr>
<td>Channel 3</td>
<td>Closed Form</td>
</tr>
<tr>
<td>Channel 4</td>
<td>Closed Form</td>
</tr>
<tr>
<td>Channel 5</td>
<td>Closed Form</td>
</tr>
</tbody>
</table>

Table 1: The required transmit power for the closed-form and convex optimization based solutions.

Fig. 3: The revenue of the legitimate transmitter against power allocation at the private jammer for different channels with fixed interference price (i.e., \( \mu_1 = 1 \)).

B. Fixed Interference Prices

In this subsection, we evaluate the performance of the proposed schemes with private jammers, where the legitimate transmitter is charged with fixed interference prices. The simulation results are provided with different numbers of legitimate users and eavesdroppers.

Single Legitimate User and Single Eavesdropper

A secrecy network with a single legitimate user and an eavesdropper is considered in which a private jammer introduces interference to the eavesdropper by charging the legitimate transmitter with a price of one (i.e., \( \mu_1 = 1 \)) for unit interference. First, we validate the concavity of the revenue function of the legitimate transmitter (\( f(p_1) \) in (60)) in terms of the power allocation \( p_1 \) at the private jammer and then simulation results based optimal power allocations are obtained to support the theoretical derivations. Figure 3 shows the revenue function of the legitimate transmitter for different sets of channels for fixed interference price. As seen in Figure 3, the revenue functions are concave for different sets of channels, which validates the proof of the convexity of \( f(p_1) \) provided in Appendix B. On the other hand, Table 2 presents the optimal power allocation policy at the private jammer, the achieved secrecy rate and the corresponding revenue of the legitimate transmitter obtained through theoretical and simulation results. As seen in Table 2, the theoretical and simulation results are identical, which demonstrates the accuracy of the derivations in (18). In addition, the optimal power allocations at the jammer corresponding to the maximum revenue at transmitter in Figure 3 is the same as the theoretical results in Table 2 for the five channels considered in this simulation. Hence, these results confirm the optimality of the derived results for the scenario of the single legitimate user and the single eavesdropper.

Single Legitimate User and Multiple Eavesdroppers

Here, we consider a multicasting secrecy network with a single legitimate user and two eavesdroppers. The price used
not presented those results here due to space limitations. We have the transmitter for Channel 1 in Figure 4; however, the rest of channels. Note that we have only presented the revenue of the transmitter for five sets of channels. As seen in Table 3, the theoretical and simulation results are indistinguishable, which validates the derivation of the closed-form power allocations at the private jammers. This confirms the optimality of the results obtained in Table 3 for different sets of channels. In (37). On the other hand, the maximum revenue from Figure 4 is the same as that of Channel 1 in Table 3 with the same secrecy network as in the fixed interference price. The unit price for the achieved secrecy rate at the legitimate user is 5 ($\lambda_1 = 5$).

by the jammers to charge the legitimate transmitter is 1 and 3 (i.e., $\mu_1 = 1$, $\mu_2 = 3$), respectively, for unit interference. Similar to the previous simulations, first, we validate the convexity of the revenue function of the legitimate transmitter in (35) in terms of power allocations (i.e., $p_1$ and $p_2$) at the private jammers for different sets of channels. Then, the correctness of the derived theoretical results is supported through numerical results. Figure 4 depicts the revenue functions of the legitimate transmitter for Channel 1 provided in Table 3 which confirms the convexity of the revenue function in terms of power allocation policy at the jammers. In addition, Table 3 provides the theoretical and simulation based optimal power allocations at the private jammers which maximize the revenue of the transmitter for five sets of channels. As seen in Table 3, the theoretical and simulation results are indistinguishable, which validates the derivation of the closed-form power allocations in (37). On the other hand, the maximum revenue from Figure 4 is the same as that of Channel 1 in Table 3 with the same power allocations at the private jammers. This confirms the optimality of the results obtained in Table 3 for different sets of channels. Note that we have only presented the revenue of the transmitter for Channel 1 in Figure 4; however, the rest of the channels in Table 3 provide the similar results. We have not presented those results here due to space limitations.

### C. Stackelberg Game

In this subsection, we validate the equilibrium of the proposed Stackelberg games for different numbers of legitimate users and eavesdroppers.

#### Single Legitimate User and Single Eavesdropper

To support the derived Stackelberg equilibrium, a secrecy network with a single legitimate user and an eavesdropper is considered. First, for different set of channels, the revenue function of the jammer is evaluated with different interference prices as shown in Figure 5. These results confirm that the jammer revenue function is concave with respect to the interference price (i.e., $\mu_1$) and support the proof provided in Appendix C. The choices for the optimal interference prices and the maximum revenues of the jammers are provided in Table 4, which verifies the accuracy of the analytical results. The Stackelberg equilibria ($\mu_1^*, \mu_2^*$) for the proposed game are also presented in Table 4. These validate the derived unique Stackelberg equilibrium of the game through simulation results, where both the transmitter and the private jammer will come to an agreement to maximize their revenues.

#### Single Legitimate User and Multiple Eavesdroppers

In order to validate the proposed Stackelberg equilibrium, the same secrecy network as in the fixed interference price is considered with a single legitimate user and multiple

<table>
<thead>
<tr>
<th>Channels</th>
<th>Power Allocation: Jammer 1</th>
<th>Power Allocation: Jammer 2</th>
<th>Achieved Secrecy Rate</th>
<th>Revenue: Legitimate Transmitter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Channel 1</td>
<td>Derivation 1.1809</td>
<td>Simulation 1.2000</td>
<td>Derivation 1.6445</td>
<td>Simulation 1.6458</td>
</tr>
<tr>
<td>Channel 2</td>
<td>Derivation 1.5019</td>
<td>Simulation 1.5000</td>
<td>Derivation 2.0534</td>
<td>Simulation 2.0531</td>
</tr>
<tr>
<td>Channel 3</td>
<td>Derivation 3.5984</td>
<td>Simulation 3.6000</td>
<td>Derivation 2.0505</td>
<td>Simulation 2.0507</td>
</tr>
<tr>
<td>Channel 4</td>
<td>Derivation 0.9452</td>
<td>Simulation 1.0000</td>
<td>Derivation 1.9921</td>
<td>Simulation 2.0041</td>
</tr>
<tr>
<td>Channel 5</td>
<td>Derivation 2.4107</td>
<td>Simulation 2.4000</td>
<td>Derivation 1.8168</td>
<td>Simulation 1.8152</td>
</tr>
</tbody>
</table>

**TABLE 2:** The optimal power allocation policy of the private jammers with fixed interference prices $\mu_1 = 1$, achievable secrecy rates and revenues of legitimate transmitter for single legitimate transmitter and single eavesdropper. The unit price for the achieved secrecy rate at the legitimate user is 5 ($\lambda_1 = 5$).

<table>
<thead>
<tr>
<th>Channels</th>
<th>Power Allocation: Jammer 1</th>
<th>Power Allocation: Jammer 2</th>
<th>Achieved Secrecy Rate</th>
<th>Revenue: Legitimate Transmitter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Channel 1</td>
<td>Derivation 0.3324</td>
<td>Simulation 0.3324</td>
<td>Derivation 0.7457</td>
<td>Simulation 0.7458</td>
</tr>
<tr>
<td>Channel 2</td>
<td>Derivation 0.1264</td>
<td>Simulation 0.1264</td>
<td>Derivation 0.5729</td>
<td>Simulation 0.5430</td>
</tr>
<tr>
<td>Channel 4</td>
<td>Derivation 1.1613</td>
<td>Simulation 1.1614</td>
<td>Derivation 1.0441</td>
<td>Simulation 1.0442</td>
</tr>
<tr>
<td>Channel 5</td>
<td>Derivation 0.2778</td>
<td>Simulation 0.2778</td>
<td>Derivation 2.0209</td>
<td>Simulation 2.0211</td>
</tr>
</tbody>
</table>

**TABLE 3:** The optimal power allocation policy of the private jammers with fixed interference prices $\mu_1 = 1$ and $\mu_2 = 3$, achievable secrecy rates and revenues of legitimate transmitter. The unit price for the achieved secrecy rate at the legitimate user is 5 ($\lambda_1 = 5$).
improve the achievable secrecy rates. These private jammers considered for a multicasting secrecy network with jammers to eavesdroppers. First, we evaluate the revenue function of the legitimate transmitter \( f(\gamma_0) \) in (76) in terms of \( \gamma_0 \) for different sets of channels. Figure 6 plots the revenues of the legitimate transmitter versus \( \gamma_0 \) with fixed interference prices (i.e., \( \mu_1 = 1, \mu_2 = 3 \)) for different sets of channels. This confirms the derivation of the convexity of \( f(\gamma_0) \) (Appendix D) in terms of \( \gamma_0 \). In addition, the achievable maximum revenues are the same as the derived solutions represented in Table 5. Next, we evaluate the achievable revenues of the jammers with different interference prices where it is assumed that the all the jammers introduce the same interference price (i.e., \( \mu_1 = \mu_2 = \mu_0 \)). Figure 7 plots the revenues of the jammers versus the interference price \( \mu_0 \) for different sets of channels which proves the convexity of the revenue of the jammers in the interference price \( \mu_0 \) (Appendix E). Table 5 provides the theoretical and simulation based optimal interference prices (i.e., \( \mu_0^* \)'s) and corresponding revenues of the jammers for the proposed Stackelberg game with different sets of channels, where the theoretical results are the same as the simulated results. In addition, Stackelberg equilibria of the proposed game are also provided in Table 5. The deviation of the legitimate transmitter and jammers from this equilibrium solution will introduce a loss in their corresponding revenues as evidenced by the Figures 6 and 7.

### VII. CONCLUSIONS

In this paper, we have proposed different optimization techniques for a multicasting secrecy network. For the scenario with a single legitimate user and a single eavesdropper, a closed-form solution has been derived for the power minimization problem based on the corresponding dual problem, whereas it was formulated as a semidefinite programming in the case with multiple legitimate users and multiple eavesdroppers. On the other hand, optimization problems have been considered for a multicasting secrecy network with jammers to improve the achievable secrecy rates. These private jammers

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**TABLE 4:** The optimal interference prices and revenues of the private jammer as well as Stackelberg equilibrium for different sets of channels. The unit price for the achieved secrecy rate at the legitimate user is 5 (\( \lambda_1 = 5 \)).

<table>
<thead>
<tr>
<th>Channels</th>
<th>Interference Price (( \mu_1 ))</th>
<th>Revenue of Jammer:</th>
<th>Stackelberg Equilibrium:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Derivation</td>
<td>Simulation</td>
<td>Derivation</td>
</tr>
<tr>
<td>Channel 1</td>
<td>4.4313</td>
<td>4.4000</td>
<td>0.5554</td>
</tr>
<tr>
<td>Channel 2</td>
<td>8.5462</td>
<td>8.5000</td>
<td>2.2242</td>
</tr>
<tr>
<td>Channel 3</td>
<td>5.6251</td>
<td>5.6000</td>
<td>3.6714</td>
</tr>
<tr>
<td>Channel 4</td>
<td>8.5640</td>
<td>8.6000</td>
<td>2.1736</td>
</tr>
<tr>
<td>Channel 5</td>
<td>7.8066</td>
<td>7.8000</td>
<td>2.8496</td>
</tr>
</tbody>
</table>

**TABLE 5:** The optimal interference prices and revenues of the private jammers as well as Stackelberg equilibrium for different sets of channels. The unit price for the achieved secrecy rate at the legitimate user is 5 (\( \lambda_1 = 5 \)).

<table>
<thead>
<tr>
<th>Channels</th>
<th>Interference Price:</th>
<th>Revenue of Jammers:</th>
<th>Stackelberg Equilibrium:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Derivation</td>
<td>Simulation</td>
<td>Derivation</td>
</tr>
<tr>
<td>Channel 1</td>
<td>4.0721</td>
<td>4.1000</td>
<td>1.5381</td>
</tr>
<tr>
<td>Channel 2</td>
<td>2.1647</td>
<td>2.2000</td>
<td>0.5372</td>
</tr>
<tr>
<td>Channel 3</td>
<td>2.6639</td>
<td>2.7000</td>
<td>0.7088</td>
</tr>
<tr>
<td>Channel 4</td>
<td>3.1023</td>
<td>3.1000</td>
<td>0.8887</td>
</tr>
<tr>
<td>Channel 5</td>
<td>4.0322</td>
<td>4.0000</td>
<td>1.4932</td>
</tr>
</tbody>
</table>

**Fig. 5:** The revenue of the jammer with a single legitimate user and a single eavesdropper for different sets of channels.

**Fig. 6:** The revenue of the transmitter in terms of \( \gamma_0 \) with fixed interference prices for different sets of channels.
introduce charges for their jamming service. For the fixed interference prices, we have derived the optimal interference requirements for different numbers of legitimate users and eavesdroppers. For non-fixed interference prices, we have formulated the optimization problem into a Stackelberg game in which jammers and the transmitter are the leaders and follower, respectively. A Stackelberg equilibrium has been developed for the proposed game with different number of legitimate users and eavesdroppers. To validate the derived theoretical results, simulation results have been provided for different scenarios.

APPENDIX A: PROOF OF LEMMA 1

The original power minimization problem in (2) can be written without loss of generality as
\[
\min_{p, \tilde{w}} \quad p\tilde{w}^H\tilde{w}
\]
\[
s.t. \quad \frac{\tilde{w}^H(1+p\tilde{h}_1\tilde{h}_1^H)\tilde{w}}{\tilde{w}^H(1+p\tilde{g}_1\tilde{g}_1^H)\tilde{w}} \geq 2^{R_s}, \quad \tilde{w}^H\tilde{w} = 1, \quad p \geq 0, (55)
\]
where \( \tilde{h}_1 = \frac{h}{\sigma_1^2} \) and \( \tilde{g}_1 = \frac{g}{\sigma_1^2} \). In order to obtain the optimal solution of (55) (i.e., \( \tilde{w}^*, p^* \)), we derive the corresponding dual problem. The Lagrangian of (2) can be defined as
\[
L(w, \lambda) = w^H w + \lambda \left[ 2^{R_s} (1 + w^H \tilde{g}_1 \tilde{g}_1^H w) - (1 + w^H \tilde{h}_1 \tilde{h}_1^H w) \right],
\]
where \( \lambda \) is the Lagrange multiplier associated with the secrecy rate constraint. The corresponding dual problem can be defined as
\[
\max \lambda \geq 0 \quad \frac{\partial R_s}{\partial \lambda} - 1, \quad s.t. \quad Z \triangleq I - \lambda \left( \tilde{h}_1 \tilde{h}_1^H - 2^{R_s} \tilde{g}_1 \tilde{g}_1^H \right) \succeq 0, (56)
\]
The constraint in (56) means that the matrix \( Z \) should have at least one zero eigenvalue. On the other hand, \( \lambda \) can take the maximum to satisfy the positive semidefinite constraint in (56) as
\[
\lambda^* = \frac{1}{\lambda_{\max}} \left( \tilde{h}_1 \tilde{h}_1^H - 2^{R_s} \tilde{g}_1 \tilde{g}_1^H \right), \quad (57)
\]
where \( \lambda_{\max} \) denotes the maximum eigenvalue of its argument. The original problem in (2) can be formulated as a convex problem. Hence, strong duality holds between the original problem in (2) and the corresponding dual problem in (56). The required minimum power to achieve the secrecy rate constraint is
\[
p^* = \lambda^*_2 \left( 2^{R_s} - 1 \right). \quad (58)
\]
On the other hand, the optimal \( w \) should be in the null space of \( Z \):
\[
w = v_{\max} \left( \tilde{h}_1 \tilde{h}_1^H - 2^{R_s} \tilde{g}_1 \tilde{g}_1^H \right), \quad \tilde{w}^* = \frac{w}{\|w\|_2}, (59)
\]
where \( v_{\max} \) denotes the the eigenvector corresponding to the maximum eigenvalue. Hence the optimal solution of (2) can be expressed as in (3). This completes the proof for Lemma 1.

APPENDIX B: PROOF OF LEMMA 2

We first show that the problem in (16) is a convex problem by showing that the following function is concave in \( p_1 \):
\[
f(p_1) = \lambda_1 \left[ \log(1 + \beta_0) - \log \left( 1 + \frac{\beta_1}{\sigma_1^2 + p_1 \alpha_1} \right) \right] - \mu_1 p_1 \alpha_1. \quad (60)
\]
The concavity of this function can be shown by finding the second derivative with respect to \( p_1 \) as follows:
\[
\frac{\partial^2 f(p_1)}{\partial p_1} = - \lambda_1 \alpha_1 \beta_1 \left( 2 \alpha_2^2 p_1 + 2 \alpha_1 \alpha_2^2 + \beta_1 \alpha_1 \right) - \mu_1 \alpha_1. \quad (61)
\]
Since \( \frac{\partial^2 f(p_1)}{\partial p_1^2} < 0, f(p_1) \) is a concave function in terms of \( p_1 \). Hence the optimal solution should satisfy the KKT conditions as follows [45]:
\[
\frac{\partial f(p_1)}{\partial p_1} = \frac{\lambda_1 \alpha_1 \beta_1}{(\sigma_1^2 + p_1 \alpha_1 + \beta_1)(\sigma_1^2 + p_1 \alpha_1)} - \mu_1 \alpha_1 = 0. \quad (63)
\]
By arranging the terms of (63), we obtain the following:
\[
\alpha_1^2 p_1^2 + (2 \sigma_1^2 + \beta_1) \alpha_1 p_1 + \beta_1 \sigma_1^2 + \sigma_1^2 - \frac{\lambda_1 \beta_1}{\mu_1} = 0 \quad (64)
\]
By solving this equation, the optimal power allocation policy \( p_1 \) at the jammer is obtained as \( p_1 \geq 0, \)
\[
p_1^* = \left. \frac{1}{\alpha_1} \left[ \sqrt{\frac{\beta_1^2}{4} + \frac{\lambda_1 \beta_1}{\mu_1} - \frac{(2 \sigma_1^2 + \beta_1)^2}{2}} \right] \right|^{+}. \quad (65)
\]
This completes the proof of Lemma 2.

APPENDIX C: PROOF OF LEMMA 3

The problem in (21) can be proven to be a convex problem by showing the following function is concave in the interference price \( \mu_1 \) for \( p_1^*(\geq 0) \) in (18):
\[
f(\mu_1) = \mu_1 \left( \sqrt{\frac{c_1 + c_2}{\mu_1}} - \mu_0 \right), \quad (66)
\]
where \( \mu_0, c_1 \) and \( c_2 \) are defined in (23). This function can be shown to be concave by finding its second derivative with respect to \( \mu_1 \) as follows:
\[
\frac{\partial^2 f(\mu_1)}{\partial \mu_1^2} = - \frac{c_2}{4 \mu_1^2} \left( c_1 + c_2 \right)^{\frac{1}{2}} - \frac{c_0}{4 \mu_1^2} \quad (68)
\]
Hence the second derivative of $f(\mu_1)$ with respect to $\mu_1$ is negative (i.e., $\frac{\partial^2 f(\mu_1)}{\partial \mu_1^2} < 0$), and $f(\mu_1)$ is a concave function in $\mu_1$. In addition, the optimal interference price $\mu_1^*$ should satisfy the KKT conditions as follows [45]:

$$\frac{\partial f(\mu_1)}{\partial \mu_1} = \left( c_1 + c_2 \frac{\beta_1}{\mu_1} \right)^2 - c_2 \frac{c_2}{2 \mu_1^2} \left( c_1 + c_2 \frac{\beta_1}{\mu_1} \right)^{-\frac{1}{2}} - c_0 = 0 \quad (69)$$

By rearranging the (69), we obtain the following:

$$4c_1(\gamma_1^2 - \gamma_2) \mu_1^2 + 4c_2(\gamma_2 - \gamma_1) \mu_1 - c_2 = 0. \quad (70)$$

By solving the above equation, the optimal interference price $\mu_1^*$ to maximize the jammer’s revenue is obtained as $\mu_1 > 0$,

$$\mu_1^* = \frac{c_2}{2c_1} \left( \frac{c_0}{\sqrt{\gamma_2 - \gamma_1}^2} - 1 \right). \quad (71)$$

This completes the proof of Lemma 3.

**APPENDIX D: PROOF OF LEMMA 6**

With the optimal power allocation in (34), the achieved rates of the super-active eavesdroppers (i.e., $i \in K$) will be equal as stated in Proposition 2. Hence, the power allocation at the $i^{th}$ private jammer can be written as

$$\frac{\beta_i}{\sigma_i^2 + p_i \alpha_i} = \gamma_0, \Rightarrow p_i = \frac{1}{\alpha_i} \left( \frac{\beta_i}{\gamma_0} - \sigma_i^2 \right)^+. \quad (75)$$

The original optimization problem in (34) can be formulated in terms of $\gamma_0$ as follows:

$$\max_{\gamma_0 \geq 0} \lambda_1 [\log(1 + \beta_0) - \log(1 + \gamma_0)] - \frac{1}{\gamma_0} K \sum_{i=1}^{K} \mu_i \beta_i + \frac{1}{2} \sum_{i=1}^{K} \mu_i \beta_i \quad \triangleq f(\gamma_0) \quad (76)$$

The optimal $\gamma_0^*$ should satisfy the KKT conditions and therefore we obtain the following:

$$\frac{\partial f(\gamma_0)}{\partial \gamma_0} = -\frac{\lambda_1}{1 + \gamma_0} + \frac{\tau}{\gamma_0^2}, \quad \frac{\partial^2 f(\gamma_0)}{\partial \gamma_0^2} = \frac{\lambda_1}{(1 + \gamma_0)^2} - \frac{2\tau}{\gamma_0^3}, \quad (77)$$

where $\tau = \sum_{i=1}^{K} \mu_i \beta_i$. The function $f(\gamma_0)$ is concave if the following condition is satisfied:

$$\frac{\gamma_0^2}{(1 + \gamma_0)^2} \leq \frac{2\tau}{\lambda_1}. \quad (78)$$

Hence, the optimal $\gamma_0^*$ can be obtained if $\lambda_1$ is large enough to satisfy the above condition. This means that the legitimate transmitter should charge the legitimate user a reasonable price to make a profit by introducing interference to the eavesdroppers with the help of the private jammers. However, the optimal $\gamma_0^*$ should satisfy the KKT conditions $\frac{\partial f(\gamma_0)}{\partial \gamma_0} = 0$. The optimal $\gamma_0^*$ can be obtained by solving the following equation:

$$\lambda_1 \gamma_0^2 - \gamma_0 \sum_{i=1}^{K} \mu_i \beta_i - \sum_{i=1}^{K} \mu_i \beta_i = 0. \quad (79)$$

and $\gamma_0 > 0$,

$$\gamma_0^* = \frac{\sum_{i=1}^{K} \mu_i \beta_i + \sqrt{\sum_{i=1}^{K} \mu_i \beta_i^2 (4\lambda_0 + \sum_{i=1}^{K} \mu_i \beta_i)}}{2\lambda_1}. \quad (80)$$

Hence the optimal power allocation policy of the $i^{th}$ can be written as

$$p_i^* = \frac{1}{\alpha_i} \left( \frac{\beta_i}{\gamma_0^*} - \sigma_i^2 \right)^+. \quad (81)$$

This completes the proof of Lemma 6. 

**APPENDIX E: PROOF OF LEMMA 7**

We first show that the revenue function of the jammers in (41) is concave in terms of $\mu_0$ for $p_i > 0$ in (37) and then we derive the optimal interference price $\mu_0^*$. The revenue function of the jammers is defined as

$$f(\mu_0) = \frac{2\lambda_1 \mu_0 \beta_1}{\mu_0 \beta_1 + \sqrt{\mu_0 \beta_1 (4\lambda_0 + \mu_0 \beta_1)}} - K\sigma^2 \mu_0, \quad (82)$$

where $\beta_1 = \sum_{i=1}^{K} \beta_i$. The concavity of $f(\mu_0)$ can be proven by finding the second derivative with respect to $\mu_0$ as in (72), which is at the top of the next page. In order to prove that the function in (82) is concave, we need to show that the second derivative (i.e., $\frac{\partial^2 f(\mu_0)}{\partial \mu_0^2}$) is negative. This has been proved in (73) and (74) which are at the top of the next page. This confirms that the revenue function of the jammers is concave in $\mu_0$ and the optimal $\mu_0^*$ should satisfy the KKT conditions $\frac{\partial f(\mu_0)}{\partial \mu_0} = 0$ [45]:

$$\frac{2\lambda_1 \beta_1}{\mu_0 \beta_1 + q} - \frac{2\lambda_1 \beta_1}{\mu_0 \beta_1 + q} = 0, \quad (83)$$

$$\mu_0^* = 0.5 \left[ -4\lambda_1 K \sigma^2 \eta_1 + 2\lambda_1 \sqrt{K \sigma^2 \eta_1 + 4K^2 \sigma^2 + 4K^2 \sigma^4 \eta_1^2} \right] \frac{K \sigma^2 \eta_1}{K \sigma^2 + 4K^2 \sigma^4 \eta_1^2}. \quad (84)$$

This completes the proof of Lemma 7.
\[ \frac{\partial^2 f(\mu_0)}{\partial \mu_0^2} = \frac{-2\lambda_1 \bar{c}_1}{\mu_0 \bar{c}_1 + q} - \frac{2\lambda_1 \bar{c}_1 \mu_0}{\mu_0 \bar{c}_1 + q} + q, \quad \mu_0 \geq 0, \quad q = \sqrt{\mu_0 \bar{c}_1 (4\lambda_1 + \mu_0 \bar{c}_1)}, \quad \bar{c}_1 = \sum_{i=1}^{K} \beta_i \]

where \( q = \sqrt{\mu_0 \bar{c}_1 (4\lambda_1 + \mu_0 \bar{c}_1)} \), \( \bar{c}_1 = \sum_{i=1}^{K} \beta_i \), and \( \mu_0 \geq 0 \).

By substituting \( q = \sqrt{\mu_0 \bar{c}_1 (4\lambda_1 + \mu_0 \bar{c}_1)} \), we have

\[ \frac{\partial^2 f(\mu_0)}{\partial \mu_0^2} = \frac{-12\lambda_1^2 \bar{c}_1^2 \mu_0 (q + \bar{c}_1 \mu_0 + 2\lambda_1) - 8\lambda_1^3 \bar{c}_1^3 \mu_0 \bar{c}_1 \mu_0 + q}{q^3 (\bar{c}_1 \mu_0 + q)^3} < 0 \]

(74)
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