Two-Timeslot Two-Way Full-Duplex Relaying for 5G Wireless Communication Networks

Zhengquan Zhang, Zheng Ma, Member, IEEE, Ming Xiao, Senior Member, IEEE, George K. Karagiannidis, Fellow, IEEE, Zhiguo Ding, Senior Member, IEEE, and Pingzhi Fan, Fellow, IEEE

Abstract—We propose a novel two-timeslot two-way full-duplex (FD) relaying scheme, in which the access link and the backhaul link are divided in the time domain, and we study the average end-to-end rate and the outage performance. According to the user equipment capability and services, we investigate two scenarios: three-node I- and four-node Y-relaying channels. Among various relaying protocols, the well-known amplify-and-forward and decode-and-forward are considered. Closed-form expressions for the average end-to-end rate and the outage probability, under the effect of residual self-interference and inter-user interference, are presented. The results show that the proposed two-timeslot two-way FD relaying scheme can achieve higher rate and better outage performance than the half-duplex one, when residual self-interference is below a certain level. Therefore, this relaying scheme presents a reasonable tradeoff between performance and complexity, and so, it could be efficiently used in the fifth-generation wireless networks.

Index Terms—Full-duplex, two-way relaying, time division multiplexing, residual self-interference, Y-relaying channel.

I. INTRODUCTION

RELAYING, which enables wireless networks to work in a cooperative manner, is an efficient way to improve spectrum efficiency and extend coverage. Half-duplex (HD) relaying has already been adopted as one of the key features in long term evolution-advanced (LTE-A) systems [1]. Field tests show that it can improve the coverage in the holes and the data rate in poorly covered areas of a donor eNodeB (DeNB) [2], [3]. In order to satisfy the increasing data rate demands, the research in fifth generation (5G) wireless networks is on-going, both in academia and industry. In the 5G era, wireless networks should offer up to tens of Gbps data rate to support a variety of emerging services [4], [5], which stimulates researchers to constantly explore innovative techniques, with higher spectrum efficiency.

Recently, full-duplex (FD) radio was proposed as a promising technique for the 5G networks, because it can double the spectrum efficiency, by achieving simultaneous transmission and reception on the same carrier frequency [6]–[9]. Furthermore, in order to satisfy the 5G requirements, relaying schemes with high spectrum efficiency, such as two-way, and full-duplex etc., have been recently attracted considerable attention.

A. Related Literature

Fig. 1 summarizes existing three-node relay transmission schemes, which differ in the number of time slots required to achieve the bidirectional data exchange.

- Four-timeslot HD relaying [10], [11]. As shown in Fig. 1(a), this scheme needs four time slots to achieve the bidirectional data transmission between the user equipment (UE) and the donor base station (BS) via the relay. In the first time slot, the UE transmits uplink data...
to the relay, while the relay forwards the received data to the BS in the second time slot. Similarly, in the third time slot, the BS transmits downlink data to the relay, while the relay forwards the received data to the UE in the fourth time slot. Among all the relay transmission schemes, this scheme presents the lowest complexity, but its spectrum efficiency is the lowest one.

- **Three-timeslot HD relaying [12], [13].** Fig. 1(b) shows that bidirectional data transmission between the UE and the BS via the relay, can be achieved in three time slots. In the first time slot, the UE transmits uplink data to the relay, while the BS transmits downlink data to the relay in the second time slot. In the third time slot, the relay broadcasts a combination of the received data to the UE and the BS. In general, network coding [14], [15] is used to combine the received two data flows at the relay. Therefore, the destination node receives not only the desired data from the source node but also its own previous transmitted data. The destination node subtracts back-propagating interference (BI)\(^1\) [16] prior to decoding.

- **Two-timeslot HD relaying [16]–[19].** The two time slots bidirectional data transmission, between the UE and the BS via the relay, is demonstrated in Fig. 1(c). This scheme consists of the multiple access (MAC) and broadcast (BC) stages. At the MAC stage, the UE and the BS simultaneously transmit their own data to the relay on the same carrier frequency, while the relay broadcasts a combination of the received data to the UE and the BS at the BC stage. Similarly, both the UE and the BS need to suppress the back-propagating interference in two-timeslot HD relaying.

- **One-way FD relaying (Protocol 1) [20]–[24].** In this scheme, unidirectional data transmission between the UE and the BS via the FD relay is achieved in one time slot, as shown in Fig. 1(d). In order to exchange the bidirectional data between the UE and the BS, it still needs two time slots. In the first time slot, the UE transmits uplink to the BS via the relay, while the BS transmits downlink data to the UE via the relay in the second time slot. In this scheme, only the relay operates in FD mode, and suffers from residual self-interference\(^2\) [20]. When the amplify-and-forward (AF) protocol is adopted, it is also called as full-duplex repeater [25], [26], which has widely been used in cellular networks. Unlike the BS with whole baseband and radio remote units, a full-duplex repeater consists of a radio receiver and a transmitter, which can enable the signal to cover longer distances without degradation, through retransmitting the received weak signal at a higher power.

- **FD relaying (Protocol 2) [27].** As shown in Fig. 1(e), two time slots are used to achieve the bidirectional data exchange between the UE and the BS via the relay. In the first time slot, the UE transmits the uplink data to the relay. In the second time slot, the relay receives the downlink data from the BS, then broadcasts a combination of the received data to the UE and the BS. In this scheme, the relay and the BS operate in FD mode, thus they suffer from residual self-interference generated by the co-channel transmission and imperfect interference cancellation. In addition, both the UE and the BS need to cancel the back-propagating interference as well.

- **Two-way FD relaying (Protocol 3) [27]–[29].** Fig. 1(f) demonstrates the bidirectional data exchange between the UE and the BS via the relay in one time slot. The relay simultaneously receives two data flows from the UE and BS on the same carrier frequency, then broadcasts their combination to the UE and the BS. Compared with the above relaying schemes, two-way FD relaying (Protocol 3) can achieve highest spectrum efficiency, but it also presents the maximum processing complexity. This is because the UE, the relay, and the BS need to suppress residual self-interference, created by the co-channel transmission and imperfect interference cancellation, and the back-propagating interference needs to be cancelled at both the UE and the BS.

**B. Motivation and Contribution**

Even though there are several available relaying schemes, which are described above, it seems that they are not optimal for the future needs of wireless networks. For one-way FD relaying (Protocol 1), the BS operates in HD mode, and thus, does not fully take the advantages of FD; In FD (Protocol 2), the relay performs signal combining and the UE perfectly cancel the back-propagating interference; the relay needs two sets of FD transceivers to achieve simultaneous bidirectional data exchange between the UE and the BS in two-way FD (Protocol 3) and also performs signal combining. Besides, in this scheme, both UE and BS are required to perfectly cancel the back-propagating interference. In addition, the BS cannot dynamically adjust the time resources to optimize the performance for some scenarios, such as the signal-to-noise ratio (SNR) imbalance between the access and the backhaul links [30].

Motivated by the above, in this paper, we propose and investigate a novel two-timeslot two-way FD relaying scheme, based on time division multiplexing, where the access and the backhaul links are divided in time domain, while FD operation is introduced in each hop. The available time slots for each hop depend on the configuration from the higher layers. In the available time slots for the access link, bidirectional data are exchanged between the UE and the relay, while the BS can also use these slots to serve users in the BS macro cell. Furthermore, bidirectional data transmission between the relay and the BS is achieved in the available time slots for the backhaul link. Compared with FD (Protocol 2) and two-way FD (Protocol 3), there is no back-propagating interference in two-timeslot two-way FD relaying scheme.

According to the UE capability and services, two scenarios are considered: a) I-relaying channel (IRC);
and b) Y-relaying channel (YRC) [31]–[33]. In I-relaying channel, the UE, the relay, and the base station support FD operation and the UE has concurrent uplink and downlink data, while in Y-relaying channel, the BS and the relay, both equipped with FD transceiver, serve the UE1 with uplink data and the UE2 with downlink data. Among various relaying protocols, we consider the well-known AF and decode-and-forward (DF)\(^3\) [16]. In contrast to [34], we assume that there is no direct link between the UE and the BS, due to transmit power limitation or the severe shadowing effect [18], [20]. Furthermore, we consider the effect of residual self-interference and inter-user interference [35].

The contribution of this paper can be summarized as follows:

- A novel two-timeslot two-way FD relaying scheme, which divides the access and the backhaul links in time domain, is proposed, and the scenarios of three-node I- and four-node Y-relaying channels are studied;
- Closed-form expressions for the average end-to-end rate and the outage probability of the AF and DF based two-timeslot two-way FD relaying schemes, are derived;
- Detailed analysis and performance comparisons between the proposed scheme and the HD relaying, are also presented.

C. Paper Outline

The rest of the paper is organized as follows. Section II describes the system model and explains the main concept of the two-timeslot two-way FD relaying scheme. A detailed derivation of the average end-to-end rate and the outage probability of this relaying scheme for the I- and Y-relaying channels, are presented in Section III. Analytical results, Monte Carlo simulations and discussion are presented in Section IV, followed by the conclusions in Section V.

II. SYSTEM MODEL

A two-timeslot two-way FD relaying model is considered, as in Fig. 2, with (a) I-relaying channel and (b) Y-relaying channel. The hop between the UE and the relay is referred to as the access link, while the backhaul link refers to the hop between the relay and donor BS. Furthermore, no direct link between source and destination nodes is assumed, due to the transmit power limitation or the severe shadowing effect [18], [20]. Also, we consider a simple 1:1 access/backhaul link time slot configuration, where the odd time slots are configured to the access link, while the backhaul link uses the even time slots. To this end, in the odd time slots, the simultaneous uplink and downlink data transmissions between the UE and the relay on the same carrier frequency, are achieved, while the data exchange between the relay and the BS is implemented in the even time slots.

\(^3\)The compute-and-forward (CF) protocol enables relays to decode linear equations of the transmitted messages using the noisy linear combinations provided by the channel, which relies on codes with a linear structure, as the nested lattice codes [15], [18]. Thus, CF protocol is based on a different concept than AF and DF protocols. In this paper, we focus on DF and AF here for their practical simplicity.

In scenario (a) of Fig. 2, all the nodes operate in FD mode, thus they suffer from residual self-interference (SI), due to the co-channel transmission and imperfect interference cancellation. In scenario (b), the relay and the BS operate in FD mode, while the UE1 with uplink data and the UE2 with downlink data work in HD mode, thereby inter-user interference between two UEs replaces self-interference generated at the UE in scenario (a). In this scenario, UE1 as source, UE1 as destination, the relay, the donor BS as source, and the donor BS as destination are denoted as S1, D1, R, S2, and D2, respectively. In scenario (b), UE1, UE2, the relay, the donor BS as source, and the donor BS as destination are represented by S1, D1, R, S2, and D2, respectively. Although the detrimental effect of self-interference can be mitigated by using multiple-stage interference cancellation [36], there is still residual self-interference due to the imperfections of the radio frequency chains. According to [7], [20], and [37], the variance of residual self-interference is approximately proportional to the \(\lambda\)-th power of the average transmitted power, where \(\lambda \in [0, 1]\), depends on the effect of the adopted self-interference cancellation techniques. In practice, the accurate relation between the transmitted power and residual self-interference is still unknown [37]. Usually, it is set to empirical values, which are obtained from field measurements and can be found in [7].

The involved channels are \(S1 \rightarrow R\), \(R \rightarrow D2\), \(S2 \rightarrow R\), \(R \rightarrow D1\), \(S1 \rightarrow D1\), \(R \rightarrow R\), and \(S2 \rightarrow D2\), whose channel coefficients are denoted as \(h_{S1R}, h_{RD2}, h_{S2R}, h_{RDI}, h_{S1D1}\), and \(h_{RR}\), respectively. Note, that in scenario (a), S1 \(\rightarrow D1\) and S2 \(\rightarrow D2\) are the residual self-interference channels, while S1 \(\rightarrow D1\) is the inter-user interference channel and S2 \(\rightarrow D2\) is the residual self-interference channel in scenario (b).

We consider that \(h_{S1R}\) and \(h_{S2R}\) are independent and the channels are reciprocal, thus it holds that \(h_{S1R} = h_{RD1}\) and \(h_{S2R} = h_{RDI}\) for the I-relaying channel, while \(h_{S2R} = h_{RD2}\) holds for the Y-relaying channel. Similarly to [20] and [38], the residual self-interference channels are assumed to be free of fading, while the channels S1 \(\rightarrow R\), \(R \rightarrow D2\), S2 \(\rightarrow R\), \(R \rightarrow D1\), and the inter-user interference (IUI)
channel $S1 \rightarrow D1$ are subjected to Rayleigh fading. Thus, the instantaneous SNR, $\gamma$, is an exponential random variable (RV), with probability density function (PDF) given by [20]

$$f_\gamma(\gamma) = \frac{1}{\bar{\gamma}} e^{-\gamma/\bar{\gamma}},$$

(1)

where $\bar{\gamma}$ is the average SNR. The instantaneous channel SNR is, $\gamma = |h|^2 P/\sigma^2$, where $h$ is the channel coefficient and $\sigma^2$ is the noise power, while the average channel SNR is, $\bar{\gamma} = \mathbb{E}[|h|^2 P/\sigma^2]$, with $\mathbb{E}()$ to denote expectation [20]. The normalized transmitted powers of the source UE, the relay, and the donor BS are, $P_1 = 1$, $P_R = 1$, and $P_2 = 2$, respectively. Also, the instantaneous SNRs of the involved channels are denoted as $\gamma_{S1R}$, $\gamma_{RD2}$, $\gamma_{S2R}$, $\gamma_{RD1}$, $\gamma_{SID1}$, $\gamma_{RR}$, and $\gamma_{SD2}$, while their corresponding average SNRs are represented by $\bar{\gamma}_{S1R}$, $\bar{\gamma}_{RD2}$, $\bar{\gamma}_{S2R}$, $\bar{\gamma}_{RD1}$, $\bar{\gamma}_{SID1}$, $\bar{\gamma}_{RR}$, and $\bar{\gamma}_{SD2}$.

III. PERFORMANCE ANALYSIS

A. I-Relaying Channel

In the odd time slots, $k = 2n-1$, $n = 1, 2, 3, ...$, simultaneous bidirectional data transmission and reception is achieved between the UE1 and the relay. In addition, since both the UE1 and the relay operate in FD mode, they suffer from residual self-interference, because of imperfect interference cancellation. Therefore, the signals received at the relay and UE1 can be respectively expressed as

$$y_R[k] = h_{S1R}x_{S1}[k] + v_R[k] + n_R[k],$$

(2)

and

$$y_{D1}[k] = h_{RD1}[k] + v_{D1}[k] + n_{D1}[k],$$

(3)

where $x_{S_i} \sim CN(0, P_i)$ is the transmit symbol of the source node $i = 1, 2$, $v_R \sim CN(0, h_{RR}^2 P_R)$ residual self-interference at the relay, $n_R \sim CN(0, \sigma_R^2)$ the additive white Gaussian noise (AWGN) at the relay, $I_R$ the relay’s transmit signal, $v_{D1} \sim CN(0, h_{RD1}^2 P_R)$ residual self-interference at the destination node $i = 1, 2$, and $n_{D1} \sim CN(0, \sigma_{D1}^2)$ the AWGN at the destination node. Note, that $I_R$ depends on the relaying scheme, and is given explicitly in the following pages. Similarly, in the even time slots, $k = 2n, n = 1, 2, 3, ...$, simultaneous bidirectional data exchange is achieved between the relay and the donor BS. Both the relay and the donor BS suffer from residual self-interference, because of FD operation and imperfect interference cancellation. So, the signals received at the relay and donor BS can be respectively written as

$$y_R[k] = h_{S2R}x_{S2}[k] + v_R[k] + n_R[k],$$

(4)

and

$$y_{D2}[k] = h_{RD2}[k] + v_{D2}[k] + n_{D2}[k].$$

(5)

1) Amplify-and-Forward: In the odd time slots, the relay receives and buffers uplink data from the UE1, and forwards the buffered downlink data to the UE1 by amplifying the signals, based on the channel gains. Similarly, in the even time slots, the relay receives and buffers downlink data from the donor BS, and forwards the buffered uplink data to the donor BS, with the same processing as with the downlink data forwarding.

In the odd time slots, $k = 2n-1, n = 1, 2, 3, ...$, the relay amplifies the input signal received in the even time slots by an amplification factor $\beta > 0$, which induces a delay of $r$ assumed to be one without loss of generality. Thus, the transmit signal of the relay can be expressed as [20]

$$t_R[k] = \beta y_R[k - r] = \beta(h_{S2R}x_{S2}[k-r] + v_R[k-r] + n_R[k-r]).$$

(6)

Considering the average transmit power of the relay, $\mathbb{E}[|t_R[k]|^2] = P_R = 1$ [29], the amplification factor $\beta$ can be written as [20], [21]

$\beta = (h_{S2R}^2 + h_{RR}^2 + \sigma_R^2)^{-1/2}.$

(7)

By substituting (6) into (3), $y_{D1}[k]$ can be expressed as

$$y_{D1}[k] = h_{RD1}(\beta y_R[k - r]) + v_{D1}[k] + n_{D1}[k] = \beta h_{RD1}(h_{S2R}x_{S2}[k-r] + v_R[k-r] + n_R[k-r]) + v_{D1}[k] + n_{D1}[k].$$

(8)

Therefore, the instantaneous SNR of the signal received at the UE1, can be expressed as

$$\gamma_{IRC,D1} = \frac{\beta^2 h_{RD1}^2 [h_{S2R}]^2}{\beta^2 h_{RD1}^2 [h_{RR}]^2 + h_{SID1}^2 + \sigma_{D1}^2}.$$  

(9)

Finally, by substituting (7) into (9)

$$\gamma_{IRC,D1} = \frac{\gamma_{RD1} \gamma_{S2R}}{\gamma_{RD1} (\gamma_{RR} + 1) + (\gamma_{SID1} + 1)(\gamma_{S2R} + \gamma_{RR} + 1)}.$$  

(10)

Similarly, in the even time slots, $k = 2n, n = 1, 2, 3, ...$, the instantaneous SNR of the signal received at the donor BS is

$$\gamma_{IRC,D2} = \frac{\gamma_{RD2} \gamma_{S1R}}{\gamma_{RD2} (\gamma_{RR} + 1) + (\gamma_{S1R} + 1)(\gamma_{RD2} + \gamma_{RR} + 1)}.$$  

(11)

Compared with HD relaying, the denominator of (10) contains the terms of $\gamma_{SID1}$ and $\gamma_{RR}$, while the denominator of (11) contains the terms of $\gamma_{S2D2}$ and $\gamma_{RR}$. This means that the two-timeslot two-way FD relaying deteriorates the instantaneous SNRs of the end-to-end link, due to residual self-interference at all nodes.

In the AF based two-timeslot two-way FD I-relaying, the average end-to-end rate is defined as

$$\bar{R}_{IRC} = \frac{\epsilon [\log_2(1 + \gamma_{IRC,D1}) + \log_2(1 + \gamma_{IRC,D2})]}{2} = \epsilon [\log_2(1 + \gamma_{IRC,D1}) + \gamma_{IRC,D2}].$$

(12)

Due to no spectral loss in FD operation, the pre-log factor is equal to one, which is different from the average end-to-end rate for HD relaying. Considering channel reciprocity and identical self-interference assumption, $\bar{R}_{IRC}$ can be further written as

$$\bar{R}_{IRC} = \epsilon [\log_2(1 + \gamma_{IRC,D1})] = \epsilon [\log_2(1 + \gamma_{IRC,D2})].$$

(13)
Theorem 1: The average end-to-end rate for the AF based two-timeslot two-way FD 1-relaying over Rayleigh fading channels, can be expressed as

\[
\bar{R}^A_{1RC} = -\frac{1}{\ln 2} \left[ \frac{1}{c_2 - c_1} \left( \frac{c_1 e^\gamma_1}{\gamma_{S1R} - \gamma_{R1D}} E_1 \left( \frac{1}{\gamma_{R1D}} \right) - 1 \right) \right],
\]

where \( E_1(x) = \int_1^x \frac{e^{-t}}{t} dt \) [20], [40], [44], \( c_1 = \gamma_{S1R} / 2 + 1 \), and \( c_2 = \gamma_{R1D} / 2 + 1 \).

Proof: See Appendix A.

If each hop of the two-timeslot two-way FD relaying is allocated two orthogonal channels, e.g., using two time slots to transmit data, then it is degraded to HD relaying. Thus, the average rate can be determined from (14) by setting \( \gamma_{R1D} = 0 \) and \( \gamma_{S2D2} = 0 \) and pre-log factor \( \frac{1}{2} \). Therefore, the average end-to-end rate for the AF based HD relaying can be written as [39], [40]

\[
\bar{R}^A_{HD} = -\frac{1}{\ln 2} \left[ \frac{1}{c_2 - c_1} \left( \frac{c_1 e^\gamma_1}{\gamma_{S1R} - \gamma_{R1D}} E_1 \left( \frac{1}{\gamma_{R1D}} \right) - 1 \right) \right],
\]

Note, that compared with (15), the denominator of (14) in Theorem 1 does not contain the constant 2, which indicates that the two-timeslot two-way FD relaying can achieve an extra rate gain due to time multiplexing. However, it also suffers from a certain loss in the rate resulting from residual self-interference, because (14) contains the self-interference terms of \( \gamma_{R1D} \) and \( \gamma_{S2D2} \). Therefore, if the rate gain from time multiplexing can compensate the rate loss caused by residual self-interference, the two-timeslot two-way FD relaying can achieve better performance than that in the HD case.

An outage occurs when the transmission rate is below the target rate, \( R_{th} \). Thus, the outage probability of the AF based two-timeslot two-way FD 1-relaying can be expressed as

\[
P^A_{out,1RC} = Pr(\gamma_{1RC,D1} < R_{th}) + Pr(\gamma_{1RC,D2} < R_{th})
\]

\[
= Pr(\gamma_{1RC,D1} < \gamma_{th}) + Pr(\gamma_{1RC,D2} < \gamma_{th})
\]

\[
= \frac{2}{\ln 2} Pr(\gamma_{1RC,D1} < \gamma_{th}),
\]

where \( \gamma_{th} \) is the SNR threshold for the outage, and we have \( \gamma_{th} = 2^{R_{th}} - 1 \). The outage probability for the AF based HD relaying can be obtained from (16) by replacing \( \gamma_{th} \) by \( 2^{R_{th}} - 1 \). Considering channel reciprocity and identical self-interference assumption, \( P^A_{out,1RC} \) can be further written as

\[
P^A_{out,1RC} = Pr(\gamma_{1RC,D1} < \gamma_{th}) = Pr(\gamma_{1RC,D2} < \gamma_{th}).
\]

Theorem 2: For a given target rate, \( R_{th} \), the outage probability of the AF based two-timeslot two-way FD 1-relaying can be expressed as

\[
P^A_{out,1RC} = 1 - 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)(\gamma_{S2D2} + 1)(\gamma_{RR} + 1)}{\gamma_{S1R} \gamma_{R1D}} \right)^{\frac{1}{2}}
\]

\[
\times e^{-\frac{\gamma_{th}(\gamma_{th} + 1)(\gamma_{S2D2} + 1)(\gamma_{RR} + 1)}{\gamma_{S1R} \gamma_{R1D}}}
\]

\[
\times K_1 \left( \frac{\gamma_{th}(\gamma_{th} + 1)(\gamma_{S2D2} + 1)(\gamma_{RR} + 1)}{\gamma_{S1R} \gamma_{R1D}} \right)^{\frac{1}{2}}.
\]

Note, that for HD and FD relaying, the SNR thresholds for the outage are different. For HD relaying, the SNR threshold for the outage is, \( \gamma_{th} = 2^{R_{th}} - 1 \), while \( \gamma_{th} = 2^{R_{th}} - 1 \) is used for FD relaying.

2) Decode-and-Forward: In the odd time slots, the relay decodes and buffers the received uplink data from the UE1, then forwards the buffered downlink data from the donor BS to the UE1, while the relay decodes and buffers the received downlink data from the donor BS, then forwards the buffered uplink data from the UE1 to the donor BS in the even time slots.

In the odd time slots, \( k = 2n - 1 \), \( n = 1, 2, 3, \ldots \), the signal transmitted by the relay, \( t_k[k] \), is

\[
t_k[k] = x_{S2}[k - \tau].
\]

The instantaneous SNR of the signal received at the relay can be expressed as

\[
\gamma_{S1\rightarrow R} = \frac{\mathbb{E}[|h_{S1R}|^2]|x_{S1}[k]|^2}{\mathbb{E}[|h_{R1D}|^2]|x_{S2}[k]|^2 + \mathbb{E}[|w[k]|^2]}
\]

\[
= \frac{|h_{S1R}|^2}{|h_{R1D}|^2 + \sigma_R^2} \frac{1}{\gamma_{RR} + 1}.
\]

By substituting (20) into (3),

\[
y_{D1}[k] = h_{R1D}(x_{S2}[k - \tau]) + h_{S1D}iS_1[k] + n_{D1}[k].
\]
The instantaneous SNR of the signal received at the UE1 can be expressed as
\[ \gamma_{DF}^{I,R,C,D1} = \frac{\varepsilon(|h_{R1}|^2|x_{S2}[k-t]|^2)}{\varepsilon(|h_{S1}|^2|x_{S1}[k]|^2) + \varepsilon(|n_{D1}|^2)} \]
\[ = \frac{|h_{R1}|^2}{|h_{S1}|^2 + \sigma_{R}^2} = \frac{\gamma_{R1}}{\gamma_{RR} + 1}. \tag{23} \]

Similarly, in the even time slots, the instantaneous SNRs of the signals received at the relay and the UE2 can be respectively expressed as
\[ \gamma_{S2}^{I,R} = \frac{\varepsilon(|h_{S2}|^2|x_{S2}[k]|^2)}{\varepsilon(|h_{RR}|^2|x_{R}|^2) + \varepsilon(|n_{R}|^2)} \]
\[ = \frac{|h_{S2}|^2}{|h_{RR}|^2 + \sigma_{R}^2} = \frac{\gamma_{S2}}{\gamma_{RR} + 1}. \tag{24} \]

and
\[ \gamma_{DF}^{I,R,C,D2} = \frac{\varepsilon(|h_{RD2}|^2|x_{S1}[k-t]|^2)}{\varepsilon(|h_{S2D2}|^2|x_{S2D2}[k]|^2) + \varepsilon(|n_{D2}|^2)} \]
\[ = \frac{|h_{RD2}|^2}{|h_{S2D2}|^2 + \sigma_{D2}^2} = \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1}. \tag{25} \]

The average end-to-end rate for the DF based two-timeslot two-way FD I-relaying is defined as
\[ \bar{R}_{DF}^{I,R,C} = \frac{1}{2} \left[ \varepsilon[\log_2(1 + \min(\gamma_{S2}^{I,R}, \gamma_{DF}^{I,R,C,D1}))] + \varepsilon[\log_2(1 + \min(\gamma_{S1}^{I,R}, \gamma_{DF}^{I,R,C,D2}))] \right]. \tag{26} \]

Assuming channel reciprocity and identical self-interference, the average rate for the DF based two-timeslot two-way FD I-relaying can be further written as
\[ \bar{R}_{DF}^{I,R,C} = \varepsilon[\log_2(1 + \min(\gamma_{S2}^{I,R}, \gamma_{DF}^{I,R,C,D1}))] \]
\[ = \varepsilon[\log_2(1 + \min(\gamma_{S1}^{I,R}, \gamma_{DF}^{I,R,C,D2}))]. \tag{27} \]

**Theorem 3:** The average end-to-end rate for the DF based two-timeslot two-way FD I-relaying over Rayleigh fading channels can be expressed as
\[ \bar{R}_{DF}^{I,R,C} = \frac{1}{2} \ln 2 \left( \frac{\gamma_{S1}(\gamma_{S2D2} + 1) + \gamma_{RD2}(\gamma_{RR} + 1)}{\gamma_{S1}(\gamma_{S2D2} + 1)nD2(\gamma_{RR} + 1)} \right). \tag{28} \]

**Proof:** See Appendix C. \qed

In the same way, the average end-to-end rate for the DF based HD relaying over Rayleigh fading channels, can be determined from (28) by setting \( \gamma_{RR} = 0 \) and \( \gamma_{S2D2} = 0 \) and pre-log factor \( \frac{1}{2} \). Therefore,
\[ \bar{R}_{DF}^{H,D} = \frac{1}{2} \ln 2 \left( \frac{\gamma_{S1}nD2 + \gamma_{RD2}}{\gamma_{S1}nD2 + \gamma_{RD2}} \right). \tag{29} \]

Note, that a similar conclusion on the rate performance of the DF protocol can be observed as the AF one. However, the effect of residual self-interference on DF protocol is less than that of the AF, because DF protocol suppresses residual self-interference propagation, while the last one not. This is evident through the comparison of the instantaneous SNRs in (11) and (25).

The outage probability of the DF based two-timeslot two-way FD I-relaying, is defined as
\[ P_{DF}^{out,I,R,C} = \frac{1}{2} (Pr(\min(\gamma_{S2}^{I,R} - \gamma_{DF}^{I,R,C,D1}) < \gamma_{th})) \]
\[ + Pr(\min(\gamma_{S1}^{I,R} - \gamma_{DF}^{I,R,C,D2}) < \gamma_{th})). \tag{30} \]

Considering channel reciprocity and identical self-interference assumption, \( P_{DF}^{out,I,R,C} \) can be further expressed as
\[ P_{DF}^{out,I,R,C} = 1 - (1 - Pr(\gamma_{S2}^{I,R} < \gamma_{th})) \]
\[ \times (1 - Pr(\gamma_{S1}^{I,R} < \gamma_{th}))) \]
\[ = 1 - (1 - Pr(\gamma_{DF}^{I,R,C,D1} < \gamma_{th}))) \]
\[ \times (1 - Pr(\gamma_{DF}^{I,R,C,D2} < \gamma_{th}))). \tag{31} \]

**Theorem 4:** For a given target rate, \( R_{th} \), the outage probability of the DF based two-timeslot two-way FD I-relaying is given by
\[ P_{DF}^{out,I,R,C} = 1 - e^{-\frac{\gamma_{th}(\gamma_{DF}^{I,R,C,D1} + \gamma_{DF}^{I,R,C,D2})}{\gamma_{S1}(\gamma_{S2D2} + 1)\gamma_{RD2}(\gamma_{RR} + 1)}}. \tag{32} \]

where \( \gamma_{th} = 2R_{th} - 1 \).

**Proof:** See Appendix D. \qed

For the same reason, the outage probability of the DF based HD relaying can be determined from (32) by setting \( \gamma_{RR} = 0 \) and \( \gamma_{S2D2} = 0 \). Thus, the outage probability can be written as [41]
\[ P_{DF}^{out,H,D} = 1 - e^{-\frac{\gamma_{th}(\gamma_{DF}^{I,R,C,D1} + \gamma_{DF}^{I,R,C,D2})}{\gamma_{S1}(\gamma_{RD2})}}. \tag{33} \]

Note, that for HD and FD relaying, the SNR thresholds for the outage are different. For HD relaying, the SNR threshold for the outage is, \( \gamma_{th} = 2R_{th} - 1 \), while \( \gamma_{th} = 2R_{th} - 1 \) is used for FD relaying.

**B. Y-Relaying Channel**

For Y-relaying channel, in the odd time slots, the relay receives the uplink data from the UE1 and forwards the buffered downlink data to the UE2 on the same carrier frequency, simultaneously. Note, that the relay suffers from residual self-interference due to the co-channel transmitted signal and imperfect interference cancellation, while the UE2 suffers from inter-user interference because the UE1 transmits signal on the same carrier frequency. In the even time slots, simultaneous bidirectional data exchange is achieved between the relay and the donor BS.

1) Amplify-and-Forward: In the odd time slots, the relay receives the buffers uplink data from the UE1, then forwards the buffered downlink data to the UE2 by amplifying the signal, based on the channel gains, while the UE2 receives downlink data forwarded by the relay and inter-user interference from the UE1. In the even time slots, the relay receives and forwards downlink data from the donor BS, then forwards the buffered uplink data to the donor BS by amplifying the signal, based on the relaying channel gains.
\[
\tilde{R}_{YRC, D1}^{AF} \leq \left\{ \begin{array}{l}
\frac{1}{2} \left[ \tilde{S}_{RR} + 1 \right] F_1 \left( \tilde{S}_{SLD1} + 1 \right) - \frac{1}{2} F_1 \left( \tilde{S}_{SLD1} \right), \\
\frac{1}{2} \left[ \tilde{S}_{SR} + 1 \right] F_1 \left( \tilde{S}_{SRD1} + 1 \right) - \frac{1}{2} F_1 \left( \tilde{S}_{SRD1} \right)
\end{array} \right.
\]

Compared with the I-relaying channel, in the Y-relaying channel, the destination UE suffers from inter-user interference, which is due to other UEs' co-channel uplink data transmission, instead of residual self-interference. Thus, the instantaneous SNRs at the destination node UE2, can be expressed as

\[
\tilde{S}_{YRC, D1}^{AF} = \frac{\gamma_{RD1} \tilde{S}_{SR} + (\gamma_{SLD1} + 1)(\gamma_{SR} + \gamma_{RD1} + 1)}{\gamma_{RD1} + (\gamma_{SLD1} + 1)(\gamma_{SR} + \gamma_{RD1} + 1)}. \quad (34)
\]

while the instantaneous SNRs at the destination donor BS is written as in (11). Note, that comparing (34) with (10), \( \gamma_{SLD1} \) is the main difference between the \( Y \) and the \( I \) cases, where instead of \( \gamma_{SLD1} \) we have \( \tilde{S}_{SLD1} \).

Theorem 5: For the \( S1 \rightarrow R \rightarrow D2 \) link, the average end-to-end rate for the AF based two-timeslot two-way FD Y-relaying over Rayleigh fading channels, is expressed as in (14). For the \( S2 \rightarrow R \rightarrow D1 \) link, the average end-to-end rate can be upper bounded as in (35), shown at the top of this page, where \( F_1(x) = e^x E_1(x) \), \( c_3 = \tilde{S}_{RD1}(\tilde{S}_{SR} + 1) \),

\[
c_4 = \tilde{S}_{SR}(\tilde{S}_{SLD1} + 1) + 1, \quad c_5 = \tilde{S}_{RD1}(\tilde{S}_{SR} + 1), \quad C_1 : \{ \tilde{S}_{RD1} = \tilde{S}_{SLD1} \text{ and } \tilde{S}_{SR} \neq \tilde{S}_{RD1} \}, \quad C_2 : \{ \tilde{S}_{RD1} = \tilde{S}_{SLD1} \text{ and } \tilde{S}_{SR} = \tilde{S}_{RD1} \}, \quad C_3 : \{ \tilde{S}_{RD1} \neq \tilde{S}_{SLD1} \text{ and } \tilde{S}_{SR} \neq \tilde{S}_{RD1} \}, \quad C_4 : \{ \tilde{S}_{RD1} = \tilde{S}_{SLD1} \text{ and } \tilde{S}_{SR} = \tilde{S}_{RD1} \}.
\]

Proof: See Appendix E.

Theorem 6: For a given target rate, \( R_{th} \), the outage probability of the \( S1 \rightarrow R \rightarrow D2 \) link in the AF based two-timeslot two-way FD Y-relaying can be formulated as in (18), while the outage probability of the \( S2 \rightarrow R \rightarrow D1 \) link can be upper bounded as

\[
p_{YRC, AF, out, D1} \leq 1 - 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)(\tilde{S}_{SR} + 1)(\tilde{S}_{SLD1} + 1)}{\tilde{S}_{SR}(\tilde{S}_{SR} + 1)} \right) \frac{1}{2} \times e^{-\frac{\gamma_{th}(\gamma_{th} + 1)}{\tilde{S}_{SR}(\tilde{S}_{SR} + 1)}} \times K_1 \left( 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)(\tilde{S}_{SR} + 1)}{\tilde{S}_{SR}(\tilde{S}_{SR} + 1)} \right)^{\frac{1}{2}} \right). \quad (37)
\]

where \( \gamma_{th} = 2^{R_{th}} - 1 \).

Proof: See Appendix F.

2) Decode-and-Forward: In the odd time slots, the relay decodes and buffers the received uplink data from the UE1, and forwards the buffered downlink data to the UE2, while the UE2 receives downlink data forwarded by the relay and inter-user interference from the UE1. In the even time slots, the relay decodes and buffers the received downlink data from the donor BS, and forwards the buffered uplink data to the donor BS.

Considering \( \gamma_{SLD1} \) as inter-user interference, the instantaneous SNRs of the DF based two-timeslot two-way FD Y-relaying at two destination nodes, can be obtained from the corresponding I-relaying one. The instantaneous SNR at the destination UE2 is expressed as

\[
\tilde{S}_{YRC, D1}^{DF} = \frac{\gamma_{RD1}}{\gamma_{SLD1} + 1}. \quad (39)
\]

The instantaneous SNR at the destination donor BS can be written as in (25).

Theorem 7: For the \( S1 \rightarrow R \rightarrow D2 \) link, the average end-to-end rate for the DF based two-timeslot two-way FD
\[ Y \text{-relaying over Rayleigh fading channels, can be expressed as in (28), while for the two-timeslot two-way FD relaying scheme, the average end-to-end rate is lower bounded as} \]
\[
\tilde{R}_{Y,RC,D1}^D F \geq \frac{1}{\ln 2} e^{\frac{1}{\gamma S2R(\bar{\gamma}S1D1 + \bar{\gamma}RD1)} - \frac{E_1(\bar{\gamma}S2R(\gamma S1D1 + 1) + \bar{\gamma}RD1(\gamma RR + 1))}{\gamma S2R\bar{\gamma}RD1}}. \tag{40}
\]

**Proof:** See Appendix G. □

**Theorem 8:** For a given target rate, \( R_{th} \), the outage probability of the S1→R→D2 link in the DF based two-timeslot two-way FD Y-relaying is expressed as in (32), while the outage probability of the S2→R→D1 link can be formulated as
\[
p^{Y,DF}_{out,D1} \equiv 1 - \frac{\gamma RD1}{\gamma S1D1 + \gamma RD1} e^{-\gamma RD1(R_{th} + \bar{\gamma}S1D1)}. \tag{41}
\]
where \( \gamma_{th} = 2^{R_{th}} - 1 \).

**Proof:** See Appendix H. □

### IV. Numerical Results, Simulations and Discussion

In this section, numerical results for the average end-to-end rate and the outage probability of the two-timeslot two-way FD relaying scheme are presented, together with Monte Carlo simulations. We consider that the average SNR of the access link is the same with that of the backhaul link, and also for both inter-user interference and residual self-interference. In simulations, we first fix each node’s transmit power, then adjust the distance and location between two nodes, so that we can change the average SNRs of their end-to-end link.

Fig. 3(a) and Fig. 3(b) compare the average end-to-end rate for the AF and DF based two-timeslot two-way FD I- and HD relaying over Rayleigh fading channels, respectively. The results clearly show that the two-timeslot two-way FD I-relaying can achieve higher average rate than HD relaying, but double rate cannot be obtained. In addition, there is a cross point between the two curves, and this point shifts to the right with the increase in residual self-interference. This is because FD operation can achieve an extra rate gain by time multiplexing, but it also suffers from residual self-interference, which results in a loss in the rate performance.

With the increase of residual self-interference, the rate gain from time multiplexing cannot compensate for the rate loss, caused by the residual self-interference. It is also shown that DF protocol can achieve higher average rate than the AF one, because AF relaying propagates residual self-interference, while the DF one can suppress this propagation.

Fig. 4(a) and Fig. 4(b) depict the outage probability of the AF and DF based two-timeslot two-way FD I- and HD relaying with \( R_{th} = 1 \) b/s/Hz, respectively. The results show that the outage performance of the two-timeslot two-way FD I-relaying is better than that in HD relaying, when residual self-interference is below a certain level (e.g. < 3dB). DF protocol can achieve better outage performance than the AF one in two-timeslot two-way FD I-relaying.
Fig. 5. Average rate for the AF two-timeslot two-way FD Y- and HD relaying: a) 2-ts YRC $D_1$ and $D_2$; b) 2-ts YRC vs. HD relaying.

Fig. 5(a) shows the average rate for the unidirectional links in the AF based two-timeslot two-way FD Y-relaying. Fig. 5(b) compares the average rate for the AF based two-timeslot two-way FD Y- and HD relaying. The results are similar as those in corresponding I-relaying shown in Fig. 3, but the average rate for the downlink (i.e., $S2\rightarrow R\rightarrow D1$ link) is slightly better than that in uplink, when self-interference is very severe. This is because inter-user interference is assumed to be Rayleigh fading, while residual self-interference is free of fading. Thus, the effect of inter-user interference on the rate is less than that of residual self-interference, under the same average SNRs.

Fig. 6(a) depicts the outage probability of the unidirectional links in the AF based two-timeslot two-way FD Y-relaying. Fig. 6(b) depicts the outage probability of the AF two-timeslot two-way FD Y- and HD relaying with $R_{th} = 1$ b/s/Hz. Similar results can be obtained as those in I-relaying shown in Fig. 4, but the outage probability of the downlink is slightly better than that in uplink, when self-interference is very severe.

Fig. 7(a) illustrates the average end-to-end rate for the unidirectional links in the DF based two-timeslot two-way FD Y-relaying. Fig. 7(b) compares the average end-to-end rate for the DF two-timeslot two-way FD Y-relaying and HD relaying. The results are similar as those in the AF one shown in Fig. 5.

Fig. 8(a) depicts the outage probability of the unidirectional links in the DF based two-timeslot two-way FD Y-relaying. Fig. 8(b) depicts the outage probability of the DF based two-timeslot two-way FD Y- and HD relaying with $R_{th} = 1$ b/s/Hz. Similar results can be obtained as those in the AF one shown in Fig. 6.
Fig. 8. Outage probability of the DF based two-timeslot two-way FD $I$- and HD relaying: a) 2-ts YRC $D_1$ and $D_2$; b) 2-ts YRC vs. HD relaying.

Fig. 9. Average rate for the AF and DF based two-timeslot two-way FD $I$-, $Y$-, and HD relaying.

Fig. 10. Outage probability of the AF and DF based two-timeslot two-way FD $I$-, $Y$-, and HD relaying.

is same as self-interference. Compared with two-timeslot two-way FD $I$-relaying, $Y$-relaying can achieve a slight rate gain, only when the average SNRs of inter-user interference and self-interference are at very high region.

Fig. 10 depicts the outage probability of the AF and DF based the two-timeslot two-way FD $I$-, $Y$-, and HD relaying. The results demonstrate that two rate curves of two-timeslot two-way FD $I$- and $Y$-relaying are basically overlapped, when the average SNRs of inter-user interference and HD relaying. The results clearly showed that the proposed scheme could achieve higher rate and better outage performance than HD relaying, when residual self-interference was below a certain level. It was also shown that DF protocol could achieve higher rate than that in the AF one in the proposed relaying scheme. In addition, the effect of inter-user interference on the average rate and the outage probability was slight weaker than self-interference, when considering that inter-user interference is Rayleigh fading and self-interference is non-fading. Furthermore, there were tradeoffs between FD and HD modes, $I$- and $Y$-relaying schemes. If residual self-interference was not very severe, FD mode should be adopted, while $Y$-relaying scheme with weak inter-user interference was superior to $I$-relaying scheme, if UE could not suppress residual self-interference very well. In summary, the two-timeslot two-way FD relaying scheme can achieve reasonable tradeoff of performance and complexity, thus it will be a potentially efficient solution for 5G systems. In a future work, the effect of the access/backhaul link time slot configuration on the proposed scheme, will be investigated.

APPENDIX A

PROOF OF THEOREM 1

Combining (11) and (13), the average rate for the AF based two-timeslot two-way FD $I$-relaying over Rayleigh fading channels is written as in (42), shown at the top of the next page.

By using [40, eq. (12)], the average rate can be expressed as in (43), shown at the top of the next page. After some simplifications, $\bar{R}_{I_{RC}}^{AF}$ can be obtained as in (14) and the proof is completed.

APPENDIX B

PROOF OF THEOREM 2

For the AF based two-timeslot two-way FD $I$-relaying, the instantaneous SNR of the signal received at the donor BS can be rewritten as

$$\gamma_{I_{RC}}^{AF} = \frac{\frac{75R}{75D_2 + 1} + \frac{75D_2}{75R + 1}}{\frac{75R}{75D_2 + 1} + 1}. \quad (43)$$
After combining (17) and (43), and by using [41, eq. (20)], the outage probability can be expressed as

\[ P_{\text{out,AF}} = 1 - 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n \times K_1 \left( 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n \right). \]  

(45)

which can be simplified as in (18) and the proof is completed.

**APPENDIX C**

**PROOF OF THEOREM 3**

We first consider the random variable, \( w \), with PDF

\[ f(w) = \left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right) e^{-\left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n} \].

(46)

According to (21), (25), and (27), the average rate for the DF based two-timeslot two-way FD I-relaying can be rewritten as

\[ \bar{R}_{I,RC}^{DF} = \int_{0}^{\infty} \log_2 (1 + w) f(w) dw \]

\[ = \int_{0}^{\infty} \log_2 (1 + w) \left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right) e^{-\left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n} dw \times e^{-\left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n} \]

\[ = \int_{0}^{\infty} \frac{1}{\ln 2} \ln(1 + w) \left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right) e^{-\left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n} dw \times e^{-\left( \frac{\gamma_{RR} + 1}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n} \]

(47)

Finally, by using [42, eq. (19b)], the average rate can be written as in (28) and the proof is completed.

**APPENDIX D**

**PROOF OF THEOREM 4**

Combining (21), (25), and (31), the outage probability of the DF based two-timeslot two-way FD I-relaying can be expressed as

\[ P_{\text{out,AF}} = 1 - 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n \times K_1 \left( 2 \left( \frac{\gamma_{th}(\gamma_{th} + 1)}{\gamma_{SIR} + \frac{\gamma_{S2D2} + 1}{\gamma_{RD2}}} \right)^n \right). \]  

(48)

By using [41, eq. (21)], the outage probability can be written as in (32) and the proof is completed.

**APPENDIX E**

**PROOF OF THEOREM 5**

For the \( S1 \rightarrow R \rightarrow D2 \) link, the average rate for the AF two-timeslot two-way FD Y-relaying over Rayleigh fading channels is written as in (14), while for the \( S2 \rightarrow R \rightarrow D1 \) link, since the average rate, \( \bar{R}_{Y,RC,D1} \), has the similar form as in (13), replacing \( \gamma_{AF,RC,D1} \) in (13) by \( \gamma_{AF,Y,RC,D1} \) in (34), the average rate is expressed as in (49), shown at the bottom of this page. Function \( g(x, y, z) \) in (49) is defined as

\[ g(x, y, z) = \frac{e^{-x/y_{RD1}} e^{-y/z_{SR}} e^{-z/y_{S1D1}}}{y_{RD1} y_{S2R} y_{S1D1}}. \]  

(50)

The integral \( I_{5,1} \) is given by

\[ I_{5,1} = \int_{0}^{\infty} \int_{0}^{\infty} \int_{0}^{\infty} \ln(xy + x(y_{RR} + 1) + (z + 1)(y + y_{RR} + 1)) g(x, y, z) dx dy dz \]

(49)
After merging the same terms and integrating, the triple integral, $I_{5,1}$, can be rewritten as

$$I_{5,1} = \int_0^\infty \ln(y + \tilde{\gamma}_{RR} + 1) \frac{e^{-\gamma/\tilde{S}2R}}{\tilde{S}2R} \, dy$$

$$+ \int_0^\infty \int_0^\infty \ln(x + z + 1) \frac{e^{-(x + z)/\tilde{S}1D1}}{\tilde{S}1D1} \, dx \, dz.$$

The integrals $I_{5,1-1}$ and $I_{5,1-2}$ can be respectively solved as follows: By using [43, eq. (2.6.23.5)], the integral, $I_{5,1-1}$, can be solved in closed-form as

$$I_{5,1-1} = \ln(\tilde{\gamma}_{RR} + 1) + e^{\tilde{\gamma}_{RR} + 1} E_1 \left( \frac{\tilde{\gamma}_{RR} + 1}{\tilde{S}2R} \right).$$

Regarding the integral $I_{5,1-2}$, after integration by parts for $x$, it can be written as

$$I_{5,1-2} = \int_0^\infty \ln(1 + y) \frac{e^{-z/\tilde{S}1D1}}{\tilde{S}1D1} \, dy$$

$$+ \int_0^\infty \int_0^\infty \ln(x + z + 1) \frac{e^{-z/\tilde{S}1D1}}{\tilde{S}1D1} \, dx \, dz.$$ 

(51)

When $\tilde{\gamma}_{RD1} = \tilde{\gamma}_{S1D1}$, $I_{5,1-2}$ can be written as

$$I_{5,1-2} = \frac{1}{\tilde{\gamma}_{S1D1}} \int_0^\infty E_1 \left( \frac{x + 1}{\tilde{\gamma}_{S1D1}} \right) \, dx.$$  (57)

By using [44, eq. (4.1.9)], $I_{5,1-2}$ can be expressed as

$$I_{5,1-2} = \frac{1}{\tilde{\gamma}_{S1D1}} \left( \tilde{\gamma}_{S1D1} - e^{\tilde{\gamma}_{S1D1}} E_1 \left( \frac{1}{\tilde{\gamma}_{S1D1}} \right) \right).$$

(58)

Next, we solve the triple integral $I_{5,2}$. First, through integration by parts for $x$, it can be rewritten as in (59), shown at the bottom of this page.

According to [43, eq. (2.6.23.5)], $I_{5,2-1}$ in (59) can be evaluated as

$$I_{5,2-1} = \ln(\tilde{\gamma}_{RR} + 1) + e^{\tilde{\gamma}_{RR} + 1} E_1 \left( \frac{\tilde{\gamma}_{RR} + 1}{\tilde{S}2R} \right)$$

$$+ e^{\tilde{S}1D1} E_1 \left( \frac{1}{\tilde{S}1D1} \right).$$  (60)

Note, that in order to obtain the bound for the average end-to-end rate, we apply Jensen’s inequality during deriving the integrals. We first discuss the convexity of integral function

$$f(z) = \frac{\tilde{\gamma}_{RR} + 1}{x(\tilde{\gamma}_{RR} + 1) + (z + 1)(\tilde{\gamma}_{RR} + 1)} e^{-\gamma/\tilde{S}2R} \frac{1}{\tilde{S}2R} e^{-\gamma/\tilde{S}2R}.$$  (61)

It can be further transformed into such form, $f(z) = a(bz + c)^{-1}$, where $a$, $b$, and $c$ are constants. Its second derivative is, $f''(z) = 2ab^2(bz + c)^{-2} > 0$. Therefore, the integral function $f(z)$ is convex. After applying Jensen’s inequality to eliminate the $z$-dimension, and perform variable substitution, $I_{5,2-2}$ can be written as

$$I_{5,2-2} \geq \int_0^\infty \int_1^\infty e^{\tilde{\gamma}_{S1D1} + \tilde{\gamma}_{S1D1} + \tilde{\gamma}_{S1D1} + \tilde{\gamma}_{S1D1}} \, \left\{ e^{\tilde{\gamma}_{RD1} + \tilde{\gamma}_{RD1}} \right\} \, dxdy$$

$$= \int_0^\infty e^{\tilde{\gamma}_{S2R} + \tilde{\gamma}_{S2R}} \, \left\{ e^{\tilde{\gamma}_{S2R} + \tilde{\gamma}_{S2R}} \right\} \, dy.$$  (62)

We further discuss the integral in the following two special cases:

$$I_{5,2} = \int_0^\infty \int_1^\infty \ln(z + 1) + \ln(y + \tilde{\gamma}_{RR} + 1) \, e^{-y/\tilde{S}2R} e^{-z/\tilde{S}1D1} \, dy \, dz$$

$$+ \int_0^\infty \int_0^\infty \int_0^\infty \left( \frac{\tilde{\gamma}_{RR} + 1}{x(\tilde{\gamma}_{RR} + 1) + (z + 1)(\tilde{\gamma}_{RR} + 1)} e^{-x/\tilde{S}2R} e^{-z/\tilde{S}1D1} \right) \, dxdydz$$  (59)
Case (1): When $\gamma_{RD1}(\gamma_{RR} + 1) \neq \gamma_{S2R}(\gamma_{S1D1} + 1)$, $I_{5.2-2}$ can be written as

$$I_{5.2-2} \geq \frac{1}{\gamma_{S2R}} \gamma_{S1D1+1} \int_{0}^{\infty} e^{-\gamma_{S2R}(\gamma_{RD1}(\gamma_{RR} + 1) - \gamma_{S1D1} + 1)} dy$$

or

$$I_{5.2-2} \geq \frac{1}{\gamma_{S2R}} \gamma_{S1D1+1} \int_{0}^{\infty} e^{\gamma_{S1D1} - \gamma_{S1D1}(\gamma_{RD1}(\gamma_{RR} + 1) - \gamma_{S1D1} + 1)} dy,$$

(63)

Case (2): When $\gamma_{RD1}(\gamma_{RR} + 1) = \gamma_{S2R}(\gamma_{S1D1} + 1)$, the integral, $I_{5.2-2}$, can be written as

$$I_{5.2-2} \geq \frac{1}{\gamma_{S2R}} \int_{0}^{\infty} E_{1} \left( \frac{\gamma_{S1D1} + 1}{\gamma_{S1D1} + 1} \gamma_{S1D1} + 1 \right) dy,$$

(64)

or

$$I_{5.2-2} \geq \frac{\gamma_{RR} + 1}{\gamma_{S2R}(\gamma_{S1D1} + 1)} \int_{0}^{\gamma_{S2R}} e^{\gamma_{S1D1} - \gamma_{S1D1}(\gamma_{RD1}(\gamma_{RR} + 1) - \gamma_{S1D1} + 1)} dy,$$

(65)

Finally, by using (52), (54), (56), (58), (60), (64) and (66) into (49), $\tilde{R}_{YRC,D1}^AF$ can be written as in (35) and the proof is completed.

**APPENDIX F**

**PROOF OF THEOREM 6**

For the $S1 \rightarrow R \rightarrow D2$ link, the average end-to-end rate for the DF based two-timeslot two-way FD Y-relaying over Rayleigh fading channels, can be expressed as in (28). For the $S2 \rightarrow R \rightarrow D1$ link, since the average rate, $\tilde{R}_{YRC,D1}^DF$, has the similar form as in (27), replacing $\gamma_{S2-R}$ and $\gamma_{YRC,D1}$ in (27) by (24) and $\gamma_{YRC,D1}$ in (39), respectively, the average rate can be written as

$$\tilde{R}_{YRC,D1}^DF = E \left[ \log_{2} \left( 1 + \min \left( \frac{\gamma_{S2R}}{\gamma_{RR} + 1}, \frac{\gamma_{RD1} \gamma_{S1D1}}{\gamma_{S1D1} + 1} \right) \right) \right].$$

(70)

Since the integral function, $f(\gamma_{S1D1}) = \log_{2} \left( 1 + \min \left( \frac{\gamma_{S2R}}{\gamma_{RR} + 1}, \frac{\gamma_{RD1} \gamma_{S1D1}}{\gamma_{S1D1} + 1} \right) \right)$, is convex, by applying Jensen’s inequality, the average rate can be written as

$$\tilde{R}_{YRC,D1}^DF \geq \log_{2} \left( 1 + \min \left( \frac{\gamma_{S2R}}{\gamma_{RR} + 1}, \frac{\gamma_{RD1} \gamma_{S1D1}}{\gamma_{S1D1} + 1} \right) \right).$$

(71)

Similar to Theorem 3 and its proof, $\tilde{R}_{YRC,D1}^DF$ can be finally expressed as in (40) and the proof is completed.
For the $S\rightarrow R \rightarrow D_2$ link, the outage probability of the DF based two-timeslot two-way FD Y-relaying is expressed as in (32). For the $S_2\rightarrow R \rightarrow D_1$ link, similar to (31), the outage probability of that can be written as

$$p_{DF,R,D1,\text{out}} = 1 - (1 - P_r(\gamma_{S2,R} < \gamma_{th})) \times (1 - P_r(\gamma_{DF,R,D1} < \gamma_{th})),\quad (72)$$

where

$$P_r(\gamma_{S2,R} < \gamma_{th}) = \int_{\gamma_{th}}^{\infty} \frac{1}{\gamma_{S2,R}} e^{-\frac{1}{\gamma_{S2,R}}} dy = 1 - e^{-\frac{\gamma_{th}}{\gamma_{S2,R}}}, \quad (73)$$

and according to (39) and [23, eqs. (2) and (6)], $Pr(\gamma_{DF,R,D1} < \gamma_{th})$ can be written as

$$Pr(\gamma_{DF,R,D1} < \gamma_{th}) = 1 - e^{-\frac{\gamma_{R,D1}}{\gamma_{th} \gamma_{S1,D1} + \gamma_{R,D1}}} \frac{\gamma_{th}}{2}. \quad (74)$$

By substituting (73) and (74) into (72), $p_{DF,R,D1,\text{out}}$ can be written as in (41) and the proof is completed.
Zhengquan Zhang received the M.Sc. degree in communication and information system from Southwest Jiaotong University in 2008, where he is currently pursuing the Ph.D. degree. From 2008 to 2013, he was with ZTE Corporation as a Communication Protocol Software Engineer. While working with ZTE, he participated in the development of 3G CDMA2000 1xEV-DO and 4G LTE base station. He has submitted over 20 patents. His research interests are cooperative communications, full-duplex radio, multiple access, radio resource management, and network architecture design.

Zheng Ma (M’07) received the B.Sc. and Ph.D. degrees in communications and information system from Southwest Jiaotong University in 2000 and 2006, respectively. He was a Visiting Scholar with the University of Leeds, U.K., in 2003. In 2003 and 2005, he was a Visiting Scholar with the Hong Kong University of Science and Technology. From 2008 to 2009, he was a Visiting Research Fellow with the Department of Communication Systems, Lancaster University, U.K. He is currently a Professor with Southwest Jiaotong University, where he serves as a Deputy Dean of the School of Information Science and Technology. His research interests include information theory and coding, signal design and applications, FPGA/DSP implementation, and professional mobile radio. He has authored over 40 research papers in high-quality journals and conferences. He is an Editor of the IEEE COMMUNICATIONS LETTERS. He is also the Vice Chairman of the Information Theory Chapter in the IEEE Chengdu Section.

Ming Xiao (S’02–M’07–SM’12) received the bachelor’s and master’s degrees in engineering from the University of Electronic Science and Technology of China, Chengdu, in 1997 and 2002, respectively, and the Ph.D. degree from the Chalmers University of Technology, Sweden, in 2007. From 1997 to 1999, he was a Network and Software Engineer with China Telecom. From 2000 to 2002, he also held a position with the Sichuan Communications Administration. Since 2007, he has been with the School of Electrical Engineering, Royal Institute of Technology, Sweden, where he is currently an Associate Professor of communication theory. He received best paper awards at the International Conference on Wireless Communications and Signal Processing in 2010 and the IEEE International Conference on Computer Communication Networks in 2011. He received the Chinese Government Award for Outstanding Self-Financed Students Studying Abroad in 2007, the Hans Werthen Grant from the Royal Swedish Academy of Engineering Science in 2006, and the Ericsson Research Funding from Ericsson in 2010. Since 2012, he has been an Associate Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS and the IEEE WIRELESS COMMUNICATIONS LETTERS, and a Senior Editor of the IEEE COMMUNICATIONS LETTERS (since 2015).

Zhiguo Ding (S’03–M’05–SM’15) received the B.Eng. degree in electrical engineering from the Beijing University of Posts and Telecommunications in 2000, and the Ph.D. degree in electrical engineering from Imperial College London in 2005. From 2005 to 2014, he was with Queen’s University Belfast, Imperial College London, and Newcastle University. Since 2014, he has been with Lancaster University as a Chair Professor. Since 2012, he has also been an Academic Visitor with Princeton University. His research interests are 5G networks, game theory, cooperative and energy harvesting networks, and statistical signal processing. He is serving as an Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS, the IEEE TRANSACTIONS ON VEHICULAR TECHNOLOGY, the IEEE WIRELESS COMMUNICATIONS LETTERS, the IEEE COMMUNICATIONS LETTERS, and the Journal of Wireless Communications and Mobile Computing. He received the Best Paper Award in the IET Communication Conference on Wireless, Mobile, and Computing, in 2009, the IEEE Communication Letter Exemplary Reviewer 2012, and the EU Marie Curie Fellowship 2012–2014.

Pingzhi Fan (M’93–SM’99–F’15) received the Ph.D. degree in electronic engineering from the University of Hull, U.K. He is currently a Professor and Director of the Institute of Mobile Communications with Southwest Jiaotong University, China. He has authored over 200 research papers in the IEEE and other academic journals, and eight books published by John Wiley & Sons Ltd., Springer, and the IEEE Press. His current research interests include high mobility wireless communications, 5G technologies, and computer networks for big data. He is a recipient of the U.K. ORS Award and the NSFC Outstanding Young Scientist Award, and is a Chief Scientist of a national 973 major project. He served as a General Chair or TPC Chair of a number of international conferences, and the Guest Editor-in-Chief, a Guest Editor, or an Editorial Member of several international journals. He is the Founding Chair of the IEEE VTS BJ Chapter, the IEEE Communications Letters, and the IEEE Wireless Communications Letters. He also served as a Board Member of the IEEE Region 10, the IET (IEEE) Council, and the IET Asia-Pacific Region. He is an IEEE VTS Distinguished Lecturer (2015–2017), and a Fellow of IET, CIE, and CIC.

George K. Karagiannidis (M’96–SM’03–F’14) was born in Pithagorio, Greece. He received the University Diploma and Ph.D. degrees in electrical and computer engineering from the University of Patras in 1987 and 1999, respectively. From 2000 to 2004, he was a Senior Researcher with the Institute for Space Applications and Remote Sensing, National Observatory of Athens, Greece. In 2004, he joined the Aristotle University of Thessaloniki, Greece, as a Faculty Member, where he is currently a Professor with the Electrical and Computer Engineering Department and the Director of the Digital Telecommunications Systems and Networks Laboratory. He is also an Honorary Professor with the University of Patras, Greece. From 2009 to 2015, he was a Visiting Professor with Princeton University. His research interests are in the broad area of digital communications systems with an emphasis on wireless communications, optical wireless communications, wireless power transfer and applications, molecular communications, communications and robotics, and wireless security.

He has authored or co-authored over 400 technical papers published in scientific journals and presented at international conferences. He has authored the Greek edition of the book entitled Telecommunications Systems and co-authored the book entitled Advanced Optical Wireless Communications Systems (Cambridge Publications, 2012).

Dr. Karagiannidis has been a General Chair, Technical Program Chair, and member of technical program committees in several IEEE and non-IEEE conferences. He was an Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS, a Senior Editor of the IEEE COMMUNICATIONS LETTERS, an Editor of the EURASIP Journal of Wireless Communications and Networks, and a Guest Editor of the IEEE JOURNAL ON SELECTED AREAS IN COMMUNICATIONS several times. From 2012 to 2015, he was the Editor-in-Chief of the IEEE COMMUNICATIONS LETTERS. Dr. Karagiannidis was selected as a 2015 Thomson Reuters Highly Cited Researcher.
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Two-Timeslot Two-Way Full-Duplex Relaying for 5G Wireless Communication Networks

Zhengquan Zhang, Zheng Ma, Member, IEEE, Ming Xiao, Senior Member, IEEE, George K. Karagiannidis, Fellow, IEEE, Zhiguo Ding, Senior Member, IEEE, and Pingzhi Fan, Fellow, IEEE

Abstract—We propose a novel two-timeslot two-way full-duplex (FD) relaying scheme, in which the access link and the backhaul link are divided in the time domain, and we study the average end-to-end rate and the outage performance. According to the user equipment capability and services, we investigate two scenarios: three-node 1- and four-node Y-relaying channels. Among various relaying protocols, the well-known amplify-and-forward and decode-and-forward are considered. Closed-form expressions for the average end-to-end rate and the outage probability, under the effect of residual self-interference and inter-user interference, are presented. The results show that the proposed two-timeslot two-way FD relaying scheme can achieve higher rate and better outage performance than the half-duplex one, when residual self-interference is below a certain level. Therefore, this relaying scheme presents a reasonable tradeoff between performance and complexity, and so, it could be efficiently used in the fifth-generation wireless networks.

Index Terms—Full-duplex, two-way relaying, time division multiplexing, residual self-interference, Y-relaying channel.

I. INTRODUCTION

RELAYING, which enables wireless networks to work in a cooperative manner, is an efficient way to improve spectrum efficiency and extend coverage. Half-duplex (HD) relaying has already been adopted as one of the key features in long term evolution-advanced (LTE-A) systems [1]. Field tests show that it can improve the coverage in the holes and the data rate in poorly covered areas of a donor eNodeB (DeNB) [2], [3]. In order to satisfy the increasing data rate demands, the research in fifth generation (5G) wireless networks is on-going, both in academia and industry. In the 5G era, wireless networks should offer up to tens of Gbps data rate to support a variety of emerging services [4], [5], which stimulates researchers to constantly explore innovative techniques, with higher spectrum efficiency.

Recently, full-duplex (FD) radio was proposed as a promising technique for the 5G networks, because it can double the spectrum efficiency, by achieving simultaneous transmission and reception on the same carrier frequency [6]–[9]. Furthermore, in order to satisfy the 5G requirements, relaying schemes with high spectrum efficiency, such as two-way, and full-duplex etc., have been recently attracted considerable attention.

A. Related Literature

Fig. 1 summarizes existing three-node relay transmission schemes, which differ in the number of time slots required to achieve the bidirectional data exchange.

- **Four-timeslot HD relaying** [10], [11]. As shown in Fig. 1(a), this scheme needs four time slots to achieve the bidirectional data transmission between the user equipment (UE) and the donor base station (BS) via the relay. In the first time slot, the UE transmits uplink data...
to the relay, while the relay forwards the received data to the BS in the second time slot. Similarly, in the third time slot, the BS transmits downlink data to the relay, while the relay forwards the received data to the UE in the fourth time slot. Among all the relay transmission schemes, this scheme presents the lowest complexity, but its spectrum efficiency is the lowest one.

- **Three-timeslot HD relaying** [12], [13]. Fig. 1(b) shows that bidirectional data transmission between the UE and the BS via the relay, can be achieved in three time slots. In the first time slot, the UE transmits uplink data to the relay, while the BS transmits downlink data to the relay in the second time slot. In the third time slot, the relay broadcasts a combination of the received data to the UE and the BS. In general, network coding [14], [15] is used to combine the received two data flows at the relay. Therefore, the destination node receives not only the desired data from the source node but also its own previous transmitted data. The destination node subtracts back-propagating interference (BI)\(^1\) [16] prior to decoding.

- **Two-timeslot HD relaying** [16]–[19]. The two time slots bidirectional data transmission, between the UE and the BS via the relay, is demonstrated in Fig. 1(c). This scheme consists of the multiple access (MAC) and broadcast (BC) stages. At the MAC stage, the UE and the BS simultaneously transmit their own data to the relay on the same carrier frequency, while the relay broadcasts a combination of the received data to the UE and the BS at the BC stage. Similarly, both the UE and the BS need to suppress the back-propagating interference in two-timeslot HD relaying.

- **One-way FD relaying (Protocol 1)** [20]–[24]. In this scheme, unidirectional data transmission between the UE and the BS via the FD relay is achieved in one time slot, as shown in Fig. 1(d). In order to exchange the bidirectional data between the UE and the BS, it still needs two time slots. In the first time slot, the UE transmits uplink to the BS via the relay, while the BS transmits downlink data to the UE via the relay in the second time slot. In this scheme, only the relay operates in FD mode, and suffers from residual self-interference\(^2\) [20]. When the amplify-and-forward (AF) protocol is adopted, it is also called as full-duplex repeater [25], [26], which has widely been used in cellular networks. Unlike the BS with whole baseband and radio remote units, a full-duplex repeater consists of a radio receiver and a transmitter, which can enable the signal to cover longer distances without degradation, through retransmitting the received weak signal at a higher power.

- **FD relaying (Protocol 2)** [27]. As shown in Fig. 1(e), two time slots are used to achieve the bidirectional data exchange between the UE and the BS via the relay. In the first time slot, the UE transmits the uplink data to the relay. In the second time slot, the relay receives the downlink data from the BS, then broadcasts a combination of the received data to the UE and the BS. In this scheme, the relay and the BS operate in FD mode, thus they suffer from residual self-interference generated by the co-channel transmission and imperfect interference cancellation. In addition, both the UE and the BS need to cancel the back-propagating interference as well.

- **Two-way FD relaying (Protocol 3)** [27]–[29]. Fig. 1(f) demonstrates the bidirectional data exchange between the UE and the BS via the relay in one time slot. The relay simultaneously receives two data flows from the UE and the BS on the same carrier frequency, then broadcasts their combination to the UE and the BS. Compared with the above relaying schemes, two-way FD relaying (Protocol 3) can achieve highest spectrum efficiency, but it also presents the maximum processing complexity. This is because the UE, the relay, and the BS need to suppress residual self-interference, created by the co-channel transmission and imperfect interference cancellation, and the back-propagating interference needs to be cancelled at both the UE and the BS.

**B. Motivation and Contribution**

Even though there are several available relaying schemes, which are described above, it seems that they are not optimal for the future needs of wireless networks. For one-way FD relaying (Protocol 1), the BS operates in HD mode, and thus, does not fully take the advantages of FD; In FD (Protocol 2), the relay performs signal combining and the UE perfectly cancel the back-propagating interference; the relay needs two sets of FD transceivers to achieve simultaneous bidirectional data exchange between the UE and the BS in two-way FD (Protocol 3) and also performs signal combining. Besides, in this scheme, both UE and BS are required to perfectly cancel the back-propagating interference. In addition, the BS cannot dynamically adjust the time resources to optimize the performance for some scenarios, such as the signal-to-noise ratio (SNR) imbalance between the access and the backhaul links [30].

Motivated by the above, in this paper, we propose and investigate a novel two-timeslot two-way FD relaying scheme, based on time division multiplexing, where the access and the backhaul links are divided in time domain, while FD operation is introduced in each hop. The available time slots for each hop depend on the configuration from the higher layers. In the available time slots for the access link, bidirectional data are exchanged between the UE and the relay, while the BS can also use these slots to serve users in the BS macro cell. Furthermore, bidirectional data transmission between the relay and the BS is achieved in the available time slots for the backhaul link. Compared with FD (Protocol 2) and two-way FD (Protocol 3), there is no back-propagating interference in two-timeslot two-way FD relaying scheme.

According to the UE capability and services, two scenarios are considered: a) 1-relaying channel (IRC);
and b) $Y$-relaying channel (YRC) [31]–[33]. In $I$-relaying channel, the UE, the relay, and the base station support FD operation and the UE has concurrent uplink and downlink data, while in $Y$-relaying channel, the BS and the relay, both equipped with FD transceiver, serve the UE1 with uplink data and the UE2 with downlink data. Among various relaying protocols, we consider the well-known AF and decode-and-forward (DF)\(^3\) [16]. In contrast to [34], we assume that there is no direct link between the UE and the BS, due to transmit power limitation or the severe shadowing effect [18], [20]. Furthermore, we consider the effect of residual self-interference and inter-user interference [35].

The contribution of this paper can be summarized as follows:
- A novel two-timeslot two-way FD relaying scheme, which divides the access and the backhaul links in time domain, is proposed, and the scenarios of three-node $I$- and four-node $Y$-relaying channels are studied;
- Closed-form expressions for the average end-to-end rate and the outage probability of the AF and DF based two-timeslot two-way FD relaying schemes, are derived;
- Detailed analysis and performance comparisons between the proposed scheme and the HD relaying, are also presented.

C. Paper Outline

The rest of the paper is organized as follows. Section II describes the system model and explains the main concept of the two-timeslot two-way FD relaying scheme. A detailed derivation of the average end-to-end rate and the outage probability of this relaying scheme for the $I$- and $Y$-relaying channels, are presented in Section III. Analytical results, Monte Carlo simulations and discussion are presented in Section IV, followed by the conclusions in Section V.

II. SYSTEM MODEL

A two-timeslot two-way FD relaying model is considered, as in Fig. 2, with (a) $I$-relaying channel and (b) $Y$-relaying channel. The hop between the UE and the relay is referred to as the access link, while the backhaul link refers to the hop between the relay and donor BS. Furthermore, no direct link between source and destination nodes is assumed, due to the transmit power limitation or the severe shadowing effect [18], [20]. Also, we consider a simple 1:1 access/backhaul link time slot configuration, where the odd time slots are configured to the access link, while the backhaul link uses the even time slots. To this end, in the odd time slots, the simultaneous uplink and downlink data transmissions between the UE and the relay on the same carrier frequency, are achieved, while the data exchange between the relay and the BS is implemented in the even time slots.

\(^3\)The compute-and-forward (CF) protocol enables relays to decode linear equations of the transmitted messages using the noisy linear combinations provided by the channel, which relies on codes with a linear structure, as the nested lattice codes [15], [18]. Thus, CF protocol is based on a different concept than AF and DF protocols. In this paper, we focus on DF and AF here for their practical simplicity.

In scenario (a) of Fig. 2, all the nodes operate in FD mode, thus they suffer from residual self-interference (SI), due to the co-channel transmission and imperfect interference cancellation. In scenario (b), the relay and the BS operate in FD mode, while the UE1 with uplink data and the UE2 with downlink data work in HD mode, thereby inter-user interference between two UEs replaces self-interference generated at the UE in scenario (a). In this scenario, UE1 as source, UE1 as destination, the relay, the donor BS as source, and the donor BS as destination are denoted as $S_1$, $D_1$, $R$, $S_2$, and $D_2$, respectively. In scenario (b), UE1, UE2, the relay, the donor BS as source, and the donor BS as destination are represented by $S_1$, $D_1$, $R$, $S_2$, and $D_2$, respectively.

Although the detrimental effect of self-interference can be mitigated by using multiple-stage interference cancellation [36], there is still residual self-interference due to the imperfections of the radio frequency chains. According to [7], [20], and [37], the variance of residual self-interference is approximately proportional to the $\lambda$-th power of the average transmitted power, where, $\lambda \in [0, 1]$, depends on the effect of the adopted self-interference cancellation techniques.

In practice, the accurate relation between the transmitted power and residual self-interference is still unknown [37]. Usually, it is set to empirical values, which are obtained from field measurements and can be found in [7].

The involved channels are $S_1\rightarrow R$, $R\rightarrow D_2$, $S_2\rightarrow R$, $R\rightarrow D_1$, $S_1\rightarrow D_1$, $R\rightarrow R$, and $S_2\rightarrow D_2$, whose channel coefficients are denoted as $h_{S_1R}$, $h_{RD_2}$, $h_{S_2R}$, $h_{RD_1}$, $h_{S_1D_1}$, $h_{RR}$, and $h_{S_2D_2}$, respectively. Note, that in scenario (a), $S_1\rightarrow D_1$ and $S_2\rightarrow D_2$ are the residual self-interference channels, while $S_1\rightarrow D_1$ is the inter-user interference channel and $S_2\rightarrow D_2$ is the residual self-interference channel in scenario (b). We consider that $h_{S_1R}$ and $h_{S_2R}$ are independent and the channels are reciprocal, thus it holds that $h_{S_1R} = h_{RD_1}$ and $h_{S_2R} = h_{RD_2}$ for the $I$-relaying channel, while $h_{S_2R} = h_{RD_2}$ holds for the $Y$-relaying channel. Similarly to [20] and [38], the residual self-interference channels are assumed to be free of fading, while the channels $S_1\rightarrow R$, $R\rightarrow D_2$, $S_2\rightarrow R$, $R\rightarrow D_1$, and the inter-user interference (IUI)
channel $S1 \rightarrow D1$ are subjected to Rayleigh fading. Thus, the instantaneous SNR, $\gamma$, is an exponential random variable (RV), with probability density function (PDF) given by [20]

$$f_\gamma(\gamma) = \frac{1}{\bar{\gamma}} e^{-\gamma/\bar{\gamma}},$$

(1)

where $\bar{\gamma}$ is the average SNR. The instantaneous channel SNR is, $\gamma = |h|^2 P / \sigma^2$, where $h$ is the channel coefficient and $\sigma^2$ is the noise power, while the average channel SNR is, $\bar{\gamma} = E[|h|^2] P / \sigma^2$, with $E[\cdot]$ to denote expectation [20]. The normalized transmitted powers of the source UE, the relay, and the donor BS are, $P_1 = 1$, $P_R = 1$, and $P_2 = 1$, respectively. Also, the instantaneous SNRs of the involved channels are denoted as $\gamma_{S1R}$, $\gamma_{RD2}$, $\gamma_{RD1}$, $\gamma_{SD1}$, $\gamma_{RR}$, and $\gamma_{SD2}$, while their corresponding average SNRs are represented by $\bar{\gamma}_{S1R}$, $\bar{\gamma}_{RD2}$, $\bar{\gamma}_{RD1}$, $\bar{\gamma}_{SD1}$, $\bar{\gamma}_{RR}$, and $\bar{\gamma}_{SD2}$.

III. PERFORMANCE ANALYSIS

A. 1-Relaying Channel

In the odd time slots, $k = 2n - 1$, $n = 1, 2, 3, ...$, simultaneous bidirectional data transmission and reception is achieved between the UE1 and the relay. In addition, since both the UE1 and the relay operate in FD mode, they suffer from residual self-interference, because of imperfect interference cancellation. Therefore, the signals received at the relay and UE1 can be respectively expressed as

$$y_R[k] = h_{S1RXS1}[k] + v_R[k] + n_R[k],$$

(2)

and

$$y_D[k] = h_{RD1RXD1}[k] + v_D[k] + n_D[k],$$

(3)

where $x_{S_i} \sim CN(0, P_i)$ is the transmit symbol of the source node $i=1, 2$, $v_R \sim CN(0, h_{RR}^2 P_R)$ residual self-interference at the relay, $n_R \sim CN(0, \sigma_R^2)$ the additive white Gaussian noise (AWGN) at the relay, $v_D \sim CN(0, h_{RD2}^2 P_R)$ residual self-interference at the destination node $i=1, 2$, and $n_D_i \sim CN(0, \sigma_D^2)$ the AWGN at the destination node. Note, that $\tau_R$ depends on the relaying scheme, and is given explicitly in the following pages.

Similarly, in the even time slots, $k = 2n, n = 1, 2, 3, ...$, simultaneous bidirectional data exchange is achieved between the relay and the donor BS. Both the relay and the donor BS suffer from residual self-interference, because of FD operation and imperfect interference cancellation. So, the signals received at the relay and donor BS can be respectively written as

$$y'_R[k] = h_{S2RXS2}[k] + v_R[k] + n_R[k],$$

(4)

and

$$y_D[k] = h_{RD2RXD2}[k] + v_D[k] + n_D[k].$$

(5)

1) Amplify-and-Forward: In the odd time slots, the relay receives and buffers uplink data from the UE1, and forwards the buffered downlink data to the UE1 by amplifying the signals, based on the channel gains. Similarly, in the even time slots, the relay receives and buffers downlink data from the donor BS, and forwards the buffered uplink data to the donor BS, with the same processing as with the downlink data forwarding.

In the odd time slots, $k = 2n - 1, n = 1, 2, 3, ...$, the relay amplifies the input signal received in the even time slots by an amplification factor $\beta > 0$, which induces a delay of $\tau$ assumed to be one without loss of generality. Thus, the transmit signal of the relay can be expressed as [20]

$$t_R[k] = \beta y_R[k - \tau] = \beta h_{S2RXS2}[k - \tau] + v_R[k - \tau] + n_R[k - \tau].$$

(6)

Considering the average transmit power of the relay, $E[|t_R[k]|^2] = P_R$ [29], the amplification factor $\beta$ can be written as [20], [21]

$$\beta = (h_{S2RXS2}^2 + h_{RR}^2 + \sigma_R^2)^{-1/2}.$$ (7)

By substituting (6) into (3), $y_D[k]$ can be expressed as

$$y_D[k] = h_{RD1}(\beta y_R[k - \tau]) + v_D[k] + n_D[k] = \beta h_{RD1}(h_{S2RXS2}[k - \tau] + v_R[k - \tau] + n_R[k - \tau]) + v_D[k] + n_D[k].$$ (8)

Therefore, the instantaneous SNR of the signal received at the UE1, can be expressed as

$$\gamma_{IRC, D1} = \frac{\beta^2 |h_{RD1}|^2 |h_{S2RXS2}|^2}{\beta^2 |h_{RD1}|^2 (|h_{RR}^2 + \sigma_R^2|) + |h_{SD1}^2|^2 + \sigma_D^2}.$$ (9)

Finally, by substituting (7) into (9)

$$\gamma_{IRC, D2} = \frac{\gamma_{RD2XTS2}}{\gamma_{RD2XTS2} + \bar{\gamma}_{SD2} + \gamma_{SD1} + \bar{\gamma}_{RR} + 1}.$$ (10)

Compared with HD relaying, the denominator of (10) contains the terms of $\gamma_{SD1}$ and $\gamma_{RR}$, while the denominator of (11) contains the terms of $\bar{\gamma}_{SD2}$ and $\gamma_{RR}$. This means that the two-timeslot two-way FD relaying deteriorates the instantaneous SNRs of the end-to-end link, due to residual self-interference at all nodes.

In the AF based two-timeslot two-way FD I-relaying, the average end-to-end rate is defined as

$$R_{IRC} = \frac{\gamma_{IRC, D1}}{2} + \frac{\gamma_{IRC, D2}}{2}.$$ (12)

Due to no spectral loss in FD operation, the pre-log factor is equal to one, which is different from the average end-to-end rate for HD relaying. Considering channel reciprocity and identical self-interference assumption, $\tilde{R}_{IRC}$ can be further written as

$$\tilde{R}_{IRC} = c \{\log_2(1 + \gamma_{IRC, D1}) + \log_2(1 + \gamma_{IRC, D2})\}.$$ (13)
Theorem 1: The average end-to-end rate for the AF based two-timeslot two-way FD 1-relaying over Rayleigh fading channels, can be expressed as

$$
\tilde{R}_{\text{IRC}}^\text{AF} = \left\{ \begin{array}{ll}
\frac{1}{\ln 2} & \left( \frac{\tilde{y}_{\text{SIR}} + \tilde{y}_{\text{RR}} + 1}{\tilde{y}_{\text{SIR}}} e^{\tilde{y}_{\text{SIR}}} E_1 \left( \frac{\tilde{y}_{\text{RR}} + 1}{\tilde{y}_{\text{SIR}}} \right) \right), \\
\frac{1}{(\ln 2)(c_1 - c_2)} & \left( c_1 e^{\tilde{y}_{\text{SIR}}} E_1 \left( \frac{\tilde{y}_{\text{SIR}} + 1}{\tilde{y}_{\text{RR}}} \right) - c_2 e^{\tilde{y}_{\text{SIR}}} E_1 \left( \frac{\tilde{y}_{\text{RR}} + 1}{\tilde{y}_{\text{SIR}}} \right) \right), \\
\tilde{y}_{\text{RR}} - 2 & \tilde{y}_{\text{SIR}} \neq \tilde{y}_{\text{RR}}.
\end{array} \right.
$$

(14)

where $E_1(x) = \int_1^x e^{-t} \frac{dt}{t}$ [20], [40], [44], $c_1 = \tilde{y}_{\text{SIR}}(\tilde{y}_{\text{S}}2 + 1)$, and $c_2 = \tilde{y}_{\text{RR}}(\tilde{y}_{\text{RR}} + 1)$.

Proof: See Appendix A. □

If each hop of the two-timeslot two-way FD relaying is allocated two orthogonal channels, e.g., using two time slots to transmit data, then it is degraded to HD relaying. Thus, the average rate can be determined from (14) by setting $\tilde{y}_{\text{RR}} = 0$ and $\tilde{y}_{\text{S}}2 = 0$ and pre-log factor $1/2$. Therefore, the average end-to-end rate for the AF based HD relaying can be written as [39], [40]

$$
\tilde{R}_{\text{IRC}}^\text{AF} = \frac{1}{2\ln 2} \left[ \left( 1 + \frac{1}{\tilde{y}_{\text{SIR}}} \right) e^{\tilde{y}_{\text{SIR}}} E_1 \left( \frac{1}{\tilde{y}_{\text{RR}}} \right) - 1 \right].
$$

(15)

Note, that compared with (15), the denominator of (14) in Theorem 1 does not contain the constant $2$, which indicates that the two-timeslot two-way FD relaying can achieve an extra rate gain due to time multiplexing. However, it also suffers from a certain loss in the rate resulting from residual self-interference, because (14) contains the self-interference terms of $\tilde{y}_{\text{RR}}$ and $\tilde{y}_{\text{S}}2$. Therefore, if the rate gain from time multiplexing can compensate the rate loss caused by residual self-interference, the two-timeslot two-way FD relaying can achieve better performance than that in the HD case.

An outage occurs when the transmission rate is below the target rate, $R_{\text{th}}$. Thus, the outage probability of the AF based two-timeslot two-way FD 1-relaying can be expressed as

$$
P_{\text{out, IRC}}^\text{AF} = \frac{Pr(\gamma_{\text{IRC,D1}}^\text{AF} < R_{\text{th}}) + Pr(\gamma_{\text{IRC,D2}}^\text{AF} < R_{\text{th}})}{2} = \frac{Pr(\gamma_{\text{IRC,D1}} < \gamma_{\text{th}}) + Pr(\gamma_{\text{IRC,D2}} < \gamma_{\text{th}})}{2},
$$

(16)

where $\gamma_{\text{th}}$ is the SNR threshold for the outage, and we have $\gamma_{\text{th}} = 2^{R_{\text{th}}} - 1$. The outage probability for the AF based HD relaying can be obtained from (16) by replacing $\gamma_{\text{th}}$ by $2^{R_{\text{th}}} - 1$. Considering channel reciprocity and identical self-interference assumption, $P_{\text{out, IRC}}^\text{AF}$ can be further written as

$$
P_{\text{out, IRC}}^\text{AF} = Pr(\gamma_{\text{IRC,D1}}^\text{AF} < \gamma_{\text{th}}) = Pr(\gamma_{\text{IRC,D2}}^\text{AF} < \gamma_{\text{th}}).
$$

(17)

Theorem 2: For a given target rate, $R_{\text{th}}$, the outage probability of the AF based two-timeslot two-way FD 1-relaying can be expressed as

$$
P_{\text{out, IRC}}^\text{AF} = 1 - 2 \left( \frac{\gamma_{\text{th}}(\gamma_{\text{th}} + 1)(\tilde{y}_{\text{S}}2 + 1)(\tilde{y}_{\text{RR}} + 1)}{\tilde{y}_{\text{SIR}}(\tilde{y}_{\text{RR}} + 1)} \right)^{1/2} e^{-\frac{\tilde{y}_{\text{RR}}^2}{4(\tilde{y}_{\text{RR}} - 2)}}
$$

(18)

where $K_{\nu}(.)$ is the modified Bessel function of the second kind [38], and $\gamma_{\text{th}} = 2^{R_{\text{th}}} - 1$.

Proof: See Appendix B. □

Following similar procedure, the outage probability of the AF based half-duplex relaying can also be determined from (18) by setting $\tilde{y}_{\text{RR}} = 0$ and $\tilde{y}_{\text{S}}2 = 0$. Therefore, the outage probability can be expressed as [41]

$$
P_{\text{out, HD}}^\text{AF} = 1 - 2 \left( \frac{\gamma_{\text{th}}(\gamma_{\text{th}} + 1)}{\tilde{y}_{\text{SIR}}^2} \right)^{1/2} e^{-\frac{\tilde{y}_{\text{RR}}^2}{4(\tilde{y}_{\text{RR}} - 2)}}
$$

(19)

Note, that for HD and FD relaying, the SNR thresholds for the outage are different. For HD relaying, the SNR threshold for the outage is, $\gamma_{\text{th}} = 2^{R_{\text{th}}} - 1$, while $\gamma_{\text{th}} = 2^{R_{\text{th}}} - 1$ is used for FD relaying.

2) Decode-and-Forward: In the odd time slots, the relay decodes and buffers the received uplink data from the UE1, then forwards the buffered downlink data from the donor BS to the UE1, while the relay decodes and buffers the received downlink data from the donor BS, then forwards the buffered uplink data from the UE1 to the donor BS in the even time slots.

In the odd time slots, $k = 2n - 1$, $n = 1, 2, 3, ..., $ the signal transmitted by the relay, $t_{R}[k]$, is

$$
t_{R}[k] = x_{S2}[k - \tau].
$$

(20)

The instantaneous SNR of the signal received at the relay can be expressed as

$$
\gamma_{S1 \rightarrow R} = \frac{\varepsilon(\lvert h_{S1R} \rvert^2 \lvert x_{S1} \rvert^2)}{\varepsilon(\lvert h_{R} \rvert^2 \lvert t_{R}[k] \rvert^2) + \varepsilon(\lvert n_{R} \rvert^2)}
$$

(21)

By substituting (20) into (3),

$$
\gamma_{D1}[k] = h_{RD1}(x_{S2}[k - \tau]) + h_{S1DiS1}[k] + n_{D1}[k].
$$

(22)
The instantaneous SNR of the signal received at the UE1 can be expressed as
\[
\gamma_{\text{DF}, D1} = \frac{e((h_{RD1})^2|x_{S2}[k - l]|^2)}{e((h_{S1D1})^2|x_{S1}[k]|^2) + e((h_{D1})^2)}
\]
\[
= \frac{|h_{RD1}|^2}{|h_{S1D1}|^2 + \sigma_{D1}^2} = \gamma_{RD1} |\gamma_{S1D1} + 1| \quad (23)
\]
Similarly, in the even time slots, the instantaneous SNRs of the signals received at the relay and the UE2 can be respectively expressed as
\[
\gamma_{S2 - R} = \frac{e((h_{S2D2})^2|x_{S2}[k]|^2)}{e((h_{R}|x_{R}[k]|^2) + e((h_{R}[k]|^2)}
\]
\[
= \frac{|h_{S2D2}|^2}{|h_{RR}|^2 + \sigma_{R}^2} = \gamma_{RD2} \frac{1}{\gamma_{RR} + 1} \quad \gamma_{S2D2} + 1 \quad (24)
\]
and
\[
\gamma_{\text{DF}, D2} = \frac{e((h_{RD2})^2|x_{S1}[k - l]|^2)}{e((h_{S2D2})^2|x_{S2}[k]|^2) + e((h_{D2})^2)}
\]
\[
= \frac{|h_{RD2}|^2}{|h_{S2D2}|^2 + \sigma_{D2}^2} = \gamma_{RD2} |\gamma_{S2D2} + 1| \quad (25)
\]
The average end-to-end rate for the DF based two-timeslot two-way FD I-relaying is defined as
\[
\bar{R}_{\text{DF}} = \frac{1}{2} (e(\log_2(1 + \min(\gamma_{S2-R}, \gamma_{DF, D1})))
\]
\[
+ e(\log_2(1 + \min(\gamma_{S1-R}, \gamma_{DF, D2})))) \quad (26)
\]
Assuming channel reciprocity and identical self-interference, the average rate for the DF based two-timeslot two-way FD I-relaying can be further written as
\[
\bar{R}_{\text{DF}} = e(\log_2(1 + \min(\gamma_{S2-R}, \gamma_{DF, D1})))
\]
\[
= e(\log_2(1 + \min(\gamma_{S1-R}, \gamma_{DF, D2}))) \quad (27)
\]
**Theorem 3:** The average end-to-end rate for the DF based two-timeslot two-way FD I-relaying over Rayleigh fading channels can be expressed as
\[
\bar{R}_{\text{DF}} = \frac{1}{2} \ln \left( \frac{\gamma_{S1R} \gamma_{S2D2} + 1}{\gamma_{S1R} \gamma_{S2D2}} \right) \right) \quad (28)
\]
**Proof:** See Appendix C. \(\square\)

In the same way, the average end-to-end rate for the DF based HD relaying over Rayleigh fading channels, can be determined from (28) by setting \(\gamma_{R} = 0\) and \(\gamma_{S2D2} = 0\) and pre-log factor \(\frac{1}{2}\). Therefore,
\[
\bar{R}_{\text{DF}} = \frac{1}{2} \ln \left( \frac{\gamma_{S1R} \gamma_{S2D2} + 1}{\gamma_{S1R} \gamma_{S2D2}} \right) \right) \quad (29)
\]
Note, that a similar conclusion on the rate performance of the DF protocol can be observed as the AF one. However, the effect of residual self-interference on DF protocol is less than that of the AF, because DF protocol suppresses residual self-interference propagation, while the last one not. This is evident through the comparison of the instantaneous SNR in (11) and (25).

The outage probability of the DF based two-timeslot two-way FD I-relaying, is defined as
\[
P_{\text{out,DF}} = \frac{1}{2} (Pr(\min(\gamma_{S2-R}, \gamma_{DF, D1}) < \gamma_{th})
\]+ Pr(\min(\gamma_{S1-R}, \gamma_{DF, D2} < \gamma_{th})). \quad (30)
\]
Considering channel reciprocity and identical self-interference assumption, \(P_{\text{out,DF}}\) can be further expressed as
\[
P_{\text{out,DF}} = 1 - (1 - Pr(\gamma_{S2-R} < \gamma_{th}))
\] \[
	\times (1 - Pr(\gamma_{S1-R} < \gamma_{th})) = 1 - (1 - Pr(\gamma_{df, D1} < \gamma_{th}))
\] \[
	\times (1 - Pr(\gamma_{df, D2} < \gamma_{th})). \quad (31)
\]

**Theorem 4:** For a given target rate, \(R_{th}\), the outage probability of the DF based two-timeslot two-way FD I-relaying is given by
\[
P_{\text{out,DF}} = 1 - \frac{\gamma_{th}^{\gamma_{S1R} \gamma_{S2D2} + 1}}{\gamma_{S1R} \gamma_{S2D2}} \quad (32)
\]
where \(\gamma_{th} = 2^{R_{th}} - 1\).

**Proof:** See Appendix D. \(\square\)

For the same reason, the outage probability of the DF based HD relaying can be determined from (32) by setting \(\gamma_{RR} = 0\) and \(\gamma_{S2D2} = 0\). Thus, the outage probability can be written as [41]
\[
P_{\text{out,DF}} = 1 - e^{-\gamma_{th}^{\gamma_{S1R} \gamma_{S2D2} + 1}} \quad (33)
\]
Note, that for HD and FD relaying, the SNR thresholds for the outage are different. For HD relaying, the SNR threshold for the outage is, \(\gamma_{th} = 2^{R_{th}} - 1\), while \(\gamma_{th} = 2^{R_{th}} - 1\) is used for FD relaying.

**B. Y-Relaying Channel**

For Y-relaying channel, in the odd time slots, the relay receives the uplink data from the UE1 and forwards the buffered downlink data to the UE2 on the same carrier frequency, simultaneously. Note, that the relay suffers from residual self-interference due to the co-channel transmitted signal and imperfect interference cancellation, while the UE2 suffers from inter-user interference because the UE1 transmits signal on the same carrier frequency. In the even time slots, simultaneous bidirectional data exchange is achieved between the relay and the donor BS.

1) Amplify-and-Forward: In the odd time slots, the relay receives and buffers uplink data from the UE1, then forwards the buffered downlink data to the UE2 by amplifying the signal, based on the channel gains, while the UE2 receives downlink data forwarded by the relay and inter-user interference from the UE1. In the even time slots, the relay receives and buffers downlink data from the donor BS, then forwards the buffered uplink data to the donor BS by amplifying the signal, based on the relaying channel gains.
\[ R_{AF, D1} \leq \begin{cases} \frac{1}{\ln 2} \left( \frac{\tilde{y}_{RR} + 1}{\tilde{y}_{SR}} \left( \frac{\tilde{y}_{SD1} + 1}{\tilde{y}_{RD1}} - \frac{1}{\tilde{y}_{SD1}} \right) - \frac{1}{\ln 2} \left( \frac{\tilde{y}_{SD1} + 1}{\tilde{y}_{RD1}} - \frac{1}{\ln 2} \left( \frac{\tilde{y}_{SD1} + 1}{\tilde{y}_{RD1}} \right) \right) \right), & C_1 \\ \frac{1}{\ln 2} \left( \frac{1}{\tilde{y}_{SD1}} - \frac{1}{\tilde{y}_{SD1}} \right) - \frac{1}{c_3} F_1 \left( \frac{\tilde{y}_{SD1} + 1}{\tilde{y}_{RD1}} \right), & C_2 \\ \frac{1}{\ln 2} \left( \frac{1}{\tilde{y}_{RD1}} - \frac{1}{\tilde{y}_{SD1}} \right) - \frac{1}{c_3} \left( \frac{\tilde{y}_{SD1} + 1}{\tilde{y}_{RD1}} - 1 \right), & C_3 \\ \frac{1}{\ln 2} \left( \frac{1}{\tilde{y}_{RD1}} - \frac{1}{\tilde{y}_{SD1}} \right) - \frac{1}{c_3 - c_4} F_1 \left( \frac{\tilde{y}_{SD1} + 1}{\tilde{y}_{RD1}} \right) - F_1 \left( \frac{\tilde{y}_{RR} + 1}{\tilde{y}_{SR}} \right), & C_4 \end{cases} \]

\[ \gamma_{YRC, D1} = \frac{\gamma_{RD1} \gamma_{SR}}{\gamma_{RD1}(\gamma_{RR} + 1) + (\gamma_{SD1} + 1)(\gamma_{SR} + \gamma_{RR} + 1)}, \]  

while the instantaneous SNRs at the destination BS is written as in (11). Note, that comparing (34) with (10), \( \gamma_{SD1} \) is the main difference between the Y and the I cases, where instead of \( \gamma_{SI1} \) we have \( \gamma_{SR} \).

**Theorem 5:** For the S1→R→D2 link, the average end-to-end rate for the AF based two-timeslot two-way FD Y-relaying over Rayleigh fading channels, is expressed as in (14). For the S2→R→D1 link, the average end-to-end rate can be upper bounded as in (35), shown at the top of this page, where \( F_1(x) = e^{-x} E_1(x) \), \( C \) is the rate of self-interference, and the rate of inter-user interference is due to other UEs’ co-channel uplink data transmission, instead of residual self-interference. Thus, the instantaneous SNRs at the destination node UE2, can be expressed as

\[ y_{YRC, D1} = \frac{y_{RD1} y_{SR}}{y_{RD1}(y_{RR} + 1) + (y_{SD1} + 1)(y_{SR} + y_{RR} + 1)}, \]  

while the instantaneous SNRs at the destination donor BS is written as in (11). Note, that comparing (34) with (10), \( y_{SD1} \) is the main difference between the Y and the I cases, where instead of \( y_{SI1} \) we have \( y_{SR} \).

**Theorem 6:** For a given target rate, \( R_{th} \), the outage probability of the S1→R→D2 link in the AF based two-timeslot two-way FD Y-relaying can be formulated as in (18), while the outage probability of the S2→R→D1 link can be upper bounded as

\[ P_{YRC, AF, out, D1} \leq 1 - 2 \left( \frac{P_{th}(y_{th} + 1)(y_{RR} + 1)(y_{SD1} + 1)}{y_{SR} y_{RD1}} \right)^{\frac{1}{2}} \times e^{-\frac{y_{th} y_{RR} + 1}{y_{SR} y_{RD1}}} \times K_1 \left( \frac{2(y_{th}(y_{th} + 1)(y_{RR} + 1))}{y_{SR} y_{RD1}} \right)^{\frac{1}{2}}. \]

where \( y_{th} = 2^{R_{th}} - 1 \).

**Proof:** See Appendix E.

Note, that if there is no inter-user interference between two UEs, \( P_{YRC, AF, out, D1} \) can be further simplified as

\[ P_{YRC, AF, out, D1} = 1 - 2 \left( \frac{y_{th}(y_{th} + 1)(y_{RR} + 1)}{y_{SR} y_{RD1}} \right)^{\frac{1}{2}} \times e^{-\frac{y_{th} y_{RR} + 1}{y_{SR} y_{RD1}}} \times K_1 \left( \frac{2(y_{th}(y_{th} + 1)(y_{RR} + 1))}{y_{SR} y_{RD1}} \right)^{\frac{1}{2}}. \]

2) Decode-and-Forward: In the odd time slots, the relay decodes and buffers the received uplink data from the UE1, and forwards the buffered downlink data to the UE2, while the UE2 receives downlink data forwarded by the relay and inter-user interference from the UE1. In the even time slots, the relay decodes and buffers the received downlink data from the donor BS, and forwards the buffered uplink data to the donor BS.

Considering \( y_{SD1} \) as inter-user interference, the instantaneous SNRs of the DF based two-timeslot two-way FD Y-relaying at two destination nodes, can be obtained from the corresponding I-relaying one. The instantaneous SNR at the destination UE2 is expressed as

\[ y_{YRC, D1} = \frac{y_{RD1} y_{SR}}{y_{RD1} + y_{SD1} + 1}. \]

The instantaneous SNR at the destination donor BS can be written as in (25).

**Theorem 7:** For the S1→R→D2 link, the average end-to-end rate for the DF based two-timeslot two-way FD
Y-relaying over Rayleigh fading channels, can be expressed as in (28), while for the $S_2 \rightarrow R \rightarrow D_1$ link, the average end-to-end rate is lower bounded as
\[
\bar{R}_{Y,RC,D_1}^{DF} \geq \frac{1}{\ln 2} e^{\gamma_{R,D_1}^{S_2R}(\gamma_{S_1D_1} + 1) + \gamma_{R,D_1}^{S_2R}(\gamma_{R} + 1) - \gamma_{S_2R}^{S_2R}(\gamma_{R} - 1)} \times E_1 \left( \frac{\gamma_{R,D_1}^{S_2R}(\gamma_{S_1D_1} + 1) + \gamma_{R,D_1}^{S_2R}(\gamma_{R} + 1) - \gamma_{S_2R}^{S_2R}(\gamma_{R} - 1)}{\gamma_{S_2R}^{S_2R}(\gamma_{R} - 1)} \right).
\]
(40)

**Proof:** See Appendix G.
□

Theorem 8: For a given target rate, $R_{th}$, the outage probability of the $S_1 \rightarrow R \rightarrow D_2$ link in the DF based two-timeslot two-way FD Y-relaying is expressed as in (32), while the outage probability of the $S_2 \rightarrow R \rightarrow D_1$ link can be formulated as
\[
p_{Y,RC,DF}^{out,D_1} = 1 - \frac{\gamma_{R,D_1}^{S_2R}}{\gamma_{R,D_1}^{S_2R} + 1} e^{\gamma_{R,D_1}^{S_2R}(\gamma_{S_1D_1} + 1) + \gamma_{R,D_1}^{S_2R}(\gamma_{R} + 1) - \gamma_{S_2R}^{S_2R}(\gamma_{R} - 1)},
\]
(41)
where $\gamma_{th} = 2^{R_{th}} - 1$.

**Proof:** See Appendix H.
□

IV. NUMERICAL RESULTS, SIMULATIONS AND DISCUSSION

In this section, numerical results for the average end-to-end rate and the outage probability of the two-timeslot two-way FD $I$- and HD relaying scheme are presented, together with Monte Carlo simulations. We consider that the average SNR of the access link is the same with that of the backhaul link, and also for both inter-user interference and residual self-interference. In simulations, we first fix each node’s transmit power, then adjust the distance and location between two nodes, so that we can change the average SNRs of their end-to-end link.

Fig. 3(a) and Fig. 3(b) compare the average end-to-end rate for the AF and DF based two-timeslot two-way FD $I$- and HD relaying over Rayleigh fading channels, respectively. The results clearly show that the two-timeslot two-way FD $I$-relaying can achieve higher average rate than HD relaying, but double rate cannot be obtained. In addition, there is a cross point between the two curves, and this point shifts to the right with the increase in residual self-interference. This is because FD operation can achieve an extra rate gain by time multiplexing, but it also suffers from residual self-interference, which results in a loss in the rate performance. With the increase of residual self-interference, the rate gain from time multiplexing cannot compensate for the rate loss, caused by the residual self-interference. It is also shown that DF protocol can achieve higher average rate than the AF one, because AF relaying propagates residual self-interference, while the DF one can suppress this propagation.

Fig. 4(a) and Fig. 4(b) depict the outage probability of the AF and DF based two-timeslot two-way FD $I$- and HD relaying with $R_{th} = 1$ b/s/Hz, respectively. The results show that the outage performance of the two-timeslot two-way FD $I$-relaying is better than that in HD relaying, when residual self-interference is below a certain level (e.g. < 3dB). DF protocol can achieve better outage performance than the AF one in two-timeslot two-way FD $I$-relaying.
Fig. 5. Average rate for the AF two-timeslot two-way FD Y- and HD relaying: a) 2-ts YRC $D_1$ and $D_2$; b) 2-ts YRC vs. HD relaying.

Fig. 5(a) shows the average rate for the unidirectional links in the AF based two-timeslot two-way FD Y-relaying. Fig. 5(b) compares the average rate for the AF based two-timeslot two-way FD Y- and HD relaying. The results are similar as those in corresponding I-relaying shown in Fig. 3, but the average rate for the downlink (i.e., $S_2 \rightarrow R \rightarrow D_1$ link) is slightly better than that in uplink, when self-interference is very severe. This is because inter-user interference is assumed to be Rayleigh fading, while residual self-interference is free of fading. Thus, the effect of inter-user interference on the rate is less than that of residual self-interference, under the same average SNRs.

Fig. 6(a) depicts the outage probability of the unidirectional links in the AF based two-timeslot two-way FD Y-relaying. Fig. 6(b) depicts the outage probability of the AF two-timeslot two-way FD Y- and HD relaying with $R_{th} = 1 \text{ b/s/Hz}$. Similar results can be obtained as those in I-relaying shown in Fig. 4, but the outage probability of the downlink is slightly better than that in uplink, when self-interference is very severe.

Fig. 7(a) illustrates the average end-to-end rate for the unidirectional links in the DF based two-timeslot two-way FD Y-relaying. Fig. 7(b) compares the average end-to-end rate for the DF two-timeslot two-way FD Y-relaying and HD relaying. The results are similar as those in the AF one shown in Fig. 5.

Fig. 8(a) depicts the outage probability of the unidirectional links in the DF based two-timeslot two-way FD Y-relaying. Fig. 8(b) depicts the outage probability of the DF based two-timeslot two-way FD Y- and HD relaying with $R_{th} = 1 \text{ b/s/Hz}$. Similar results can be obtained as those in the AF one shown in Fig. 6.

Fig. 9 compares the average end-to-end rate for the AF and DF based two-timeslot two-way FD I-, Y-, and HD relaying.
is same as self-interference. Compared with two-timeslot two-way FD I-relaying, Y-relaying can achieve a slight rate gain, only when the average SNRs of inter-user interference and self-interference are at very high region.

Fig. 10 depicts the outage probability of the AF and DF based the two-timeslot two-way FD I-, Y-, and HD relaying with $R_{th} = 1$ b/s/Hz. Similar results can be obtained as the rate performance shown in Fig. 9.

V. CONCLUSIONS

A two-timeslot two-way FD relaying scheme, which was based on dividing the access link and the backhaul link in time domain, was proposed and investigated. Closed-form expressions for the average end-to-end rate and the outage probability, were derived. According to UE capability and services, two scenarios of I- and Y-relaying channels, were considered. The results clearly showed that the proposed scheme could achieve higher rate and better outage performance than HD relaying, when residual self-interference was below a certain level. It was also shown that DF protocol could achieve higher rate than that in the AF one in the proposed relaying scheme. In addition, the effect of inter-user interference on the average rate and the outage probability was slight weaker than self-interference, when considering that inter-user interference is Rayleigh fading and self-interference is non-fading. Furthermore, there were tradeoffs between FD and HD modes, I- and Y-relaying schemes. If residual self-interference was not very severe, FD mode should be adopted, while Y-relaying scheme with weak inter-user interference was superior to I-relaying scheme, if UE could not suppress residual self-interference very well. In summary, the two-timeslot two-way FD relaying scheme can achieve reasonable tradeoff of performance and complexity, thus it will be a potentially efficient solution for 5G systems. In a future work, the effect of the access/backhaul link time slot configuration on the proposed scheme, will be investigated.

APPENDIX A

PROOF OF THEOREM 1

Combining (11) and (13), the average rate for the AF based two-timeslot two-way FD I-relaying over Rayleigh fading channels is written as in (42), shown at the top of the next page.

By using [40, eq. (12)], the average rate can be expressed as in (43), shown at the top of the next page. After some simplifications, $R_{1RC}^{AF}$ can be obtained as in (14) and the proof is completed.

APPENDIX B

PROOF OF THEOREM 2

For the AF based two-timeslot two-way FD I-relaying, the instantaneous SNR of the signal received at the donor BS can be rewritten as

$$\gamma_{1RC}^{AF} = \frac{1}{\gamma_{RR} + 1 + \gamma_{RD} + 1}.$$  

(43)
\[
\tilde{R}_{IRC}^{AF} = e \log_2 \left( 1 + \frac{\gamma_{RD2} \gamma_{SIR}}{\gamma_{RD2} \gamma_{RR} + 1 + (\gamma_{S2D2} + 1)(\gamma_{SIR} + \gamma_{RR} + 1)} \right) \\
= e \log_2 \left( 1 + \frac{\gamma_{SIR}}{\gamma_{RR} + 1} \right) + \log_2 \left( 1 + \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1} \right) - \log_2 \left( 1 + \frac{\gamma_{SIR}}{\gamma_{RR} + 1} + \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1} \right) \\
= e \left[ \frac{1}{\ln 2} \left( 1 + \frac{\gamma_{SIR}}{\gamma_{RR} + 1} \right) \right] - e \left[ \frac{1}{\ln 2} \left( 1 + \frac{\gamma_{SIR}}{\gamma_{RR} + 1} + \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1} \right) \right].
\]

\[
\tilde{R}_{IRC}^{AF} = \left\{ \begin{array}{l}
\frac{1}{\ln 2} \left( 1 + \frac{\gamma_{SIR}}{\gamma_{RR} + 1} \right) e^{\gamma_{SIR}} \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1} e^{-\gamma_{SIR}} E_1 \left( \frac{\gamma_{SIR}}{\gamma_{S2D2} + 1} \right) - \frac{\gamma_{SIR}}{\gamma_{RR} + 1} - \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1} E_1 \left( \frac{\gamma_{SIR}}{\gamma_{S2D2} + 1} \right) \nonumber \\
\quad \ln 2 \left( \frac{\gamma_{SIR}}{\gamma_{RR} + 1} - \frac{\gamma_{RD2}}{\gamma_{S2D2} + 1} \right), \quad \gamma_{SIR} \neq \gamma_{RD2} \quad \gamma_{SIR} \neq \gamma_{RD2} + 1
\end{array} \right.
\]

Finally, by using [42, eq. (19b)], the average rate can be written as in (28) and the proof is completed.

**APPENDIX D**

**PROOF OF THEOREM 4**

Combining (21), (25), and (31), the outage probability of the DF based two-timeslot two-way FD I-relaying can be expressed as

\[
P_{out,DF} = 1 - \left( 1 - \int_0^\infty \gamma_{SIR} e^{-\gamma_{SIR} dy} \right) \left( 1 - \int_0^\infty \gamma_{RD2} e^{-\gamma_{RD2} dy} \right).
\]

By using [41, eq. (19)], the outage probability can be written as in (32) and the proof is completed.

**APPENDIX E**

**PROOF OF THEOREM 5**

For the S1→R→D2 link, the average rate for the AF two-timeslot two-way FD Y-relaying over Rayleigh fading channels is written as in (14), while for the S2→R→D1 link, since the average rate, \(R_{IRC,D1}^{AF} \), has the similar form as in (13), replacing \(\gamma_{IRC,D1}^{AF} \) by \(\gamma_{IRC,D1}^{AF} \) in (34), the average rate is expressed as in (49), shown at the bottom of this page. Function \(g(x, y, z)\) in (49) is defined as

\[
g(x, y, z) = e^{-x/\gamma_{RD1}} e^{-y/\gamma_{S2R}} e^{-z/\gamma_{S1D1}}.
\]
After merging the same terms and integrating, the triple integral, $I_{5,1}$, can be rewritten as

$$I_{5,1} = \int_0^\infty \ln(y + \frac{y}{\gamma_{RD1}} + 1) e^{-\frac{y}{\gamma_{RD1}}} dy$$

$$+ \int_0^\infty \int_0^\infty \ln(x + z + 1) e^{-x/\gamma_{RD1}} e^{-z/\gamma_{S1D1}} dxdz.$$

The integrals $I_{5,1-1}$ and $I_{5,1-2}$ can be respectively solved as follows: By using [43, eq. (2.6.23.5)], the integral, $I_{5,1-1}$, can be solved in closed-form as

$$I_{5,1-1} = \ln(\frac{y}{\gamma_{RR} + 1}) + e^{\frac{y}{\gamma_{RD1}}} E_1\left(\frac{\gamma_{RR} + 1}{\gamma_{S2R}}\right).$$

Regarding the integral $I_{5,1-2}$, after integration by parts for $x$, it can be written as

$$I_{5,1-2} = \int_0^\infty \ln(z + 1) e^{-z/\gamma_{S1D1}} dz$$

$$+ \int_0^\infty \int_0^\infty \frac{1}{x + z + 1} e^{-x/\gamma_{RD1}} e^{-z/\gamma_{S1D1}} dxdz.$$

The following procedure, according to [43, eq. (2.6.23.5)],

$$I_{5,1-2-1} = e^{\frac{1}{\gamma_{S1D1}}} E_1\left(\frac{1}{\gamma_{S1D1}}\right).$$

while the integral $I_{5,1-2-2}$ can be evaluated as follows. When

$$\gamma_{RD1} \neq \gamma_{S1D1}, I_{5,1-2-2}$$

can be written as

$$I_{5,1-2-2} = \int_0^\infty \frac{1}{\gamma_{S1D1}} \int_0^\infty \frac{1}{t} e^{-\frac{t(1+1)(1+1)}{\gamma_{RD1}}} e^{-\frac{t}{\gamma_{S1D1}}} dt dtdz$$

$$= \frac{1}{\gamma_{S1D1}} \frac{e^{\frac{1}{\gamma_{RD1}}}}{\gamma_{RD1}} \int_0^\infty E_1\left(\frac{z(1 + 1)}{\gamma_{RD1}}\right) dz,$$

or

$$I_{5,1-2-2} = \frac{\gamma_{RD1}}{(\gamma_{RD1} - \gamma_{S1D1})} \left[ e^{\frac{1}{\gamma_{RD1}}} E_1\left(\frac{1}{\gamma_{RD1}}\right) \right.$$

$$- e^{\frac{1}{\gamma_{S1D1}}} E_1\left(\frac{1}{\gamma_{S1D1}}\right) \left.\right].$$

When $\gamma_{RD1} = \gamma_{S1D1}, I_{5,1-2-2}$ can be written as

$$I_{5,1-2-2} = \frac{1}{\gamma_{S1D1}} e^{\frac{1}{\gamma_{S1D1}}} \int_0^\infty E_1\left(\frac{x + 1}{\gamma_{S1D1}}\right) dx. \quad (57)$$

By using [44, eq. (4.1.9)], $I_{5,1-2-2}$ can be expressed as

$$I_{5,1-2-2} = \frac{1}{\gamma_{S1D1}} \left(\gamma_{S1D1} - e^{\frac{1}{\gamma_{S1D1}}} E_1\left(\frac{1}{\gamma_{S1D1}}\right)\right). \quad (58)$$

Next, we solve the triple integral $I_{5,2}$. First, through integration by parts for $x$, it can be rewritten as in (59), shown at the bottom of this page.

According to [43, eq. (2.6.23.5)], $I_{5,2}$ in (59) can be evaluated as

$$I_{5,2-1} = \ln(\frac{y}{\gamma_{RR} + 1}) + e^{\frac{y}{\gamma_{RD1}}} E_1\left(\frac{\gamma_{RR} + 1}{\gamma_{S2R}}\right)$$

$$+ e^{\frac{1}{\gamma_{S1D1}}} E_1\left(\frac{1}{\gamma_{S1D1}}\right). \quad (60)$$

Note, that in order to obtain the bound for the average end-to-end rate, we apply Jensen’s inequality during deriving the integrals. We first discuss the convexity of integral function

$$f(z) = \frac{(\gamma_{RR} + 1)}{x(\gamma_{RR} + 1) + (z + 1)(y + \gamma_{RR} + 1)} e^{-\frac{z}{\gamma_{RD1}}} \frac{1}{\gamma_{S2R}} e^{-\frac{y}{\gamma_{RD1}}}.$$ \quad (61)

It can be further transformed into such form, $f(z) = a(bz + c)^{-1}$, where $a$, $b$, and $c$ are constants. Its second derivative is, $f''(z) = 2ab^2(bz + c)^{-2} > 0$. Therefore, the integral function $f(z)$ is convex. After applying Jensen’s inequality to eliminate the $z$-dimension, and perform variable substitution, $I_{5,2-2}$ can be written as

$$I_{5,2-2} \geq \int_0^\infty \int_0^\infty \frac{e^{\left(\gamma_{S1D1} + (y + \gamma_{RR} + 1)\right)/\gamma_{RD1}}} {e^{(y + \gamma_{RR} + 1)/\gamma_{RD1}}} e^{-\frac{z}{\gamma_{S1D1}}} e^{-\frac{y}{\gamma_{S2R}}} dtdy$$

$$= \int_0^\infty e^{\left(\gamma_{S1D1} + (y + \gamma_{RR} + 1)\right)/\gamma_{RD1}} e^{-\frac{z}{\gamma_{S1D1}}} e^{\frac{1}{\gamma_{S2R}}} dtdy \quad (62)$$

We further discuss the integral in the following two special cases:

$$I_{5,2} = \int_0^\infty \int_0^\infty \left(\ln(z + 1) + \ln(y + \gamma_{RR} + 1)\right) e^{-\frac{y}{\gamma_{S2R}}} e^{-\frac{z}{\gamma_{S1D1}}} dydz$$

$$+ \int_0^\infty \int_0^\infty \int_0^\infty \frac{\gamma_{RD1}}{(\gamma_{RD1} - \gamma_{S1D1})} \left[ e^{\frac{1}{\gamma_{RD1}}} E_1\left(\frac{1}{\gamma_{RD1}}\right) \right.$$

$$- e^{\frac{1}{\gamma_{S1D1}}} E_1\left(\frac{1}{\gamma_{S1D1}}\right) \left.\right]$$

$$x(\gamma_{RR} + 1) + (z + 1)(y + \gamma_{RR} + 1) e^{-\frac{z}{\gamma_{RD1}}} e^{-\frac{y}{\gamma_{S2R}}} dydz \quad (59)$$

$$I_{5,2-1}$$

$$I_{5,2}$$
Case (1): When $\tilde{y}_{RD1}(\tilde{y}_{RR} + 1) \neq \tilde{y}_{S2R}(\tilde{y}_{SID1} + 1)$, $I_{5,2-2}$ can be written as

$$I_{5,2-2} \geq \frac{1}{\gamma S2R} e^{\frac{\tilde{y}_{SID1} + 1}{\gamma RD1}} \int_{0}^{\infty} e^{-\frac{1}{\gamma S2R} \left( \frac{\gamma RD1(\tilde{y}_{RR} + 1)}{\gamma S2R} - \tilde{y}_{SID1} - 1 \right)} dy \times E_{1} \left( \tilde{y}_{SID1} + 1, \frac{\tilde{y}_{SID1} + 1}{\gamma RD1} \right) dy,$$  

(63)

or

$$I_{5,2-2} \geq \frac{\tilde{y}_{RD1}(\tilde{y}_{RR} + 1)}{\gamma S2R(\tilde{y}_{SID1} + 1)} \tilde{y}_{RD1} - (\tilde{y}_{SID1} + 1) e^{\frac{\tilde{y}_{SID1} + 1}{\gamma RD1}} E_{1} \left( \tilde{y}_{SID1} + 1, \frac{\tilde{y}_{SID1} + 1}{\gamma RD1} \right).$$  

(64)

Case (2): When $\tilde{y}_{RD1}(\tilde{y}_{RR} + 1) = \tilde{y}_{S2R}(\tilde{y}_{SID1} + 1)$, the integral, $I_{5,2-2}$, can be written as

$$I_{5,2-2} \geq \frac{1}{\gamma S2R} e^{\frac{\tilde{y}_{SID1} + 1}{\gamma RD1}} \int_{0}^{\infty} E_{1} \left( \tilde{y}_{SID1} + 1, \frac{\tilde{y}_{SID1} + 1}{\gamma RD1} \right) \left( \tilde{y}_{RD1}(\tilde{y}_{RR} + 1) - \tilde{y}_{SID1} - 1 \right) dy,$$  

(65)

or

$$I_{5,2-2} \geq \frac{\tilde{y}_{RD1}(\tilde{y}_{RR} + 1)}{\gamma S2R(\tilde{y}_{SID1} + 1)} \tilde{y}_{RD1} - (\tilde{y}_{SID1} + 1) e^{\frac{\tilde{y}_{SID1} + 1}{\gamma RD1}} E_{1} \left( \tilde{y}_{SID1} + 1, \frac{\tilde{y}_{SID1} + 1}{\gamma RD1} \right).$$  

(66)

Finally, by using (52), (54), (56), (58), (60), (64) and (66) into (49), $\tilde{R}_{YRC,D1}^{AF}$ can be written as in (35) and the proof is completed.

**APPENDIX F**

**PROOF OF THEOREM 6**

For the $S1 \rightarrow R \rightarrow D2$ link, the outage probability of the AF based two-timeslot two-way FD Y-relaying can be expressed as in (18). For the $S2 \rightarrow R \rightarrow D1$ link, the integral domains for its outage probability consist of $D_{1} = \{ (x, y, z) \mid 0 < x < \infty, 0 < y < \gamma_{th}(\tilde{y}_{RR} + 1), 0 < z < \infty \}$ and $D_{2} = \{ (x, y, z) \mid 0 < y < \gamma_{th}(\tilde{y}_{RR} + 1), 0 < \gamma_{th}(\tilde{y}_{RR} + 1) < x < \infty, 0 < z < \infty \}$. Thus, the outage probability of the AF based two-timeslot two-way FD Y-relaying can be written as in (67), shown at the bottom of this page.
APPENDIX H

PROOF OF THEOREM 8

For the $S_1 \rightarrow R \rightarrow D_2$ link, the outage probability of the DF based two-timeslot two-way FD $Y$-relaying is expressed as in (32). For the $S_2 \rightarrow R \rightarrow D_1$ link, similar to (31), the outage probability of that can be written as

$$p_{DF, out}^{YRC} = 1 - (1 - Pr(Y_S2 < \gamma_h)) \times (1 - Pr(Y_{DF, D1} < \gamma_h)),$$  \hspace{1cm} (72)

where

$$Pr(Y_S2 < \gamma_h) = Pr\left(\frac{S_2 R}{R} + 1 < \gamma_h\right) = \int_0^{\gamma_h} \frac{1}{\gamma} e^{-\frac{y}{\gamma_S2R}} dy = 1 - e^{-\frac{\gamma_h}{\gamma_S2R}}.$$  \hspace{1cm} (73)

and according to (39) and (23), eqs. (2) and (6),

$$Pr(Y_{DF, D1} < \gamma_h) = 1 - \frac{1}{\gamma_h^{\gamma_R1D1 + \gamma_R1D1}} e^{-\frac{\gamma_h}{\gamma_R1D1}}.$$  \hspace{1cm} (74)

By substituting (73) and (74) into (72), $p_{DF, out}^{YRC}$ can be written as in (41) and the proof is completed.
Zhengquan Zhang received the M.Sc. degree in communication and information system from Southwest Jiaotong University in 2008, where he is currently pursuing the Ph.D. degree. From 2008 to 2013, he was with ZTE Corporation as a Communication Protocol Software Engineer. While working with ZTE, he participated in the development of 3G CDMA2000 1xEV-DO and 4G LTE base station. He has submitted over 20 patents. His research interests are cooperative communications, full-duplex radio, multiple access, radio resource management, and network architecture design.

Zheng Ma (M’07) received the B.Sc. and Ph.D. degrees in communications and information systems from Southwest Jiaotong University in 2000 and 2006, respectively. He was a Visiting Scholar with the University of Leeds, U.K., in 2003. In 2003 and 2005, he was a Visiting Scholar with the Hong Kong University of Science and Technology. From 2008 to 2009, he was a Visiting Research Fellow with the Department of Communication Systems, Lancaster University, U.K. He is currently a Professor with Southwest Jiaotong University, where he serves as a Deputy Dean of the School of Information Science and Technology. His research interests include information theory and coding, signal design and applications, FPGA/DSP implementation, and professional mobile radio. He has authored over 40 research papers in high-quality journals and conferences. He is an Editor of the IEEE Communications Letters. He is also the Vice Chairman of the Information Theory Chapter in the IEEE Chengdu Section.

Ming Xiao (S’02–M’07–SM’12) received the bachelor’s and master’s degrees in engineering from the University of Electronic Science and Technology of China, Chengdu, in 1997 and 2002, respectively, and the Ph.D. degree from the Chalmers University of Technology, Sweden, in 2007. From 1997 to 1999, he was a Network and Software Engineer with China Telecom. From 2000 to 2002, he also held a position with the Sichuan Communications Administration. Since 2007, he has been with the School of Electrical Engineering, Royal Institute of Technology, Sweden, where he is currently an Associate Professor of communication theory. He received best paper awards at the International Conference on Wireless Communications and Signal Processing in 2010 and the IEEE International Conference on Computer Communication Networks in 2011. He received the Chinese Government Award for Outstanding Self-Financed Students Studying Abroad in 2007, the Hans Werthen Grant from the Royal Swedish Academy of Engineering Science in 2006, and the Ericsson Research Funding from Ericsson in 2010. Since 2012, he has been an Associate Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS and the IEEE WIRELESS COMMUNICATIONS LETTERS, and a Senior Editor of the IEEE COMMUNICATIONS LETTERS (since 2015).

Zhiguo Ding (S’03–M’05–SM’15) received the B.Eng. degree in electrical engineering from the Beijing University of Posts and Telecommunications in 2000, and the Ph.D. degree in electrical engineering from Imperial College London in 2005. From 2005 to 2014, he was with Queen’s University Belfast, Imperial College London, and Newcastle University. Since 2014, he has been with Lancaster University as a Chair Professor. Since 2012, he has also been an Academic Visiting with Princeton University.

His research interests are 5G networks, game theory, cooperative and energy harvesting networks, and statistical signal processing. He is serving as an Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS, the IEEE TRANSACTIONS ON VEHICULAR TECHNOLOGY, the IEEE WIRELESS COMMUNICATIONS LETTERS, the IEEE COMMUNICATIONS LETTERS, and the Journal of Wireless Communications and Mobile Computing. He received the Best Paper Award in the IET Communication Conference on Wireless, Mobile, and Computing, in 2009, the IEEE Communication Letter Exemplary Reviewer 2012, and the EU Marie Curie Fellowship 2012–2014.

Pingzhi Fan (M’93–SM’99–F’15) received the Ph.D. degree in electronic engineering from the University of Hull, U.K. He is currently a Professor and Director of the Institute of Mobile Communications with Southwest Jiaotong University, China. He has authored over 200 research papers in the IEEE and other academic journals, and eight books published by John Wiley & Sons Ltd., Springer, and the IEEE Press. His current research interests include high mobility wireless communications, 5G technologies, and software-defined radio. He was a recipient of the U.K. ORS Award and the NSFC Outstanding Young Scientist Award, and is a Chief Scientist of a national 973 major project. He served as a General Chair or TPC Chair of a number of international conferences, and the Guest Editor-in-Chief, a Guest Editor, or an Editorial Member of many other academic journals.

Dr. Karagiannidis has been a General Chair, Technical Program Chair, and member of technical program committees in several IEEE and non-IEEE conferences. He was an Editor of the IEEE TRANSACTIONS ON COMMUNICATIONS, a Senior Editor of the IEEE COMMUNICATIONS LETTERS, an Editor of the EURASIP Journal of Wireless Communications and Networks, and a Guest Editor of the IEEE JOURNAL ON SELECTED AREAS IN COMMUNICATIONS several times. From 2012 to 2015, he was the Editor-in-Chief of the IEEE COMMUNICATIONS LETTERS. Dr. Karagiannidis was selected as a 2015 Thomson Reuters Highly Cited Researcher.

George K. Karagiannidis (M’96–SM’03–F’14) was born in Pithagorio, Greece. He received the University Diploma and Ph.D. degrees in electrical and computer engineering from the University of Patras in 1987 and 1999, respectively. From 2000 to 2004, he was a Senior Researcher with the Institute for Space Applications and Remote Sensing, National Observatory of Athens, Greece. In 2004, he joined the Aristotle University of Thessaloniki, Greece, as a Faculty Member, where he is currently a Professor with the Electrical and Computer Engineering Department and the Director of the Digital Telecommunications Systems and Networks Laboratory. He is also a Honorary Professor with Southwest Jiaotong University, Chengdu, China.

His research interests are in the broad area of digital communications systems with an emphasis on wireless communications, optical wireless communications, wireless power transfer and applications, molecular communications, communications and robotics, and wireless security.

He has authored or co-authored over 400 technical papers published in scientific journals and presented at international conferences. He has authored the Greek edition of the book entitled Telecommunications Systems and co-authored the book entitled Advanced Optical Wireless Communications Systems (Cambridge Publications, 2012).

Zhiguo Ding and Pingzhi Fan are General Chairs of this special issue. They wish to thank all authors for submitting their work for consideration, and all reviewers for their constructive comments, which made this special issue a reality.
AUTHOR QUERIES

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