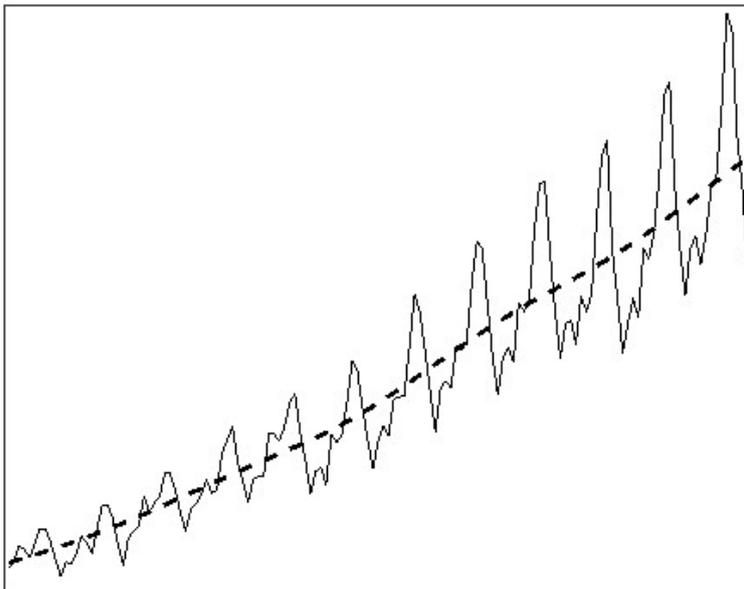


# **The CAPTAIN TOOLBOX for System Identification, Time Series Analysis, Forecasting and Control**

## **Getting Started Guide**



**Handbook Part 1  
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## GLOSSARY

ACF	Autocorrelation Function
AR	Auto-Regression
ARMA	Auto-Regression Moving-Average
ARIMA	Auto-Regression Integrated Moving-Average
ARX	Auto-Regression with eXogenous variables
BSM	Basic Structural Model
DAR	Dynamic Auto-Regression
DARX	Dynamic Auto-Regression with eXogenous variables
DBM	Data-Based Mechanistic
DHR	Dynamic Harmonic Regression
DLR	Dynamic Linear Regression
DTF	Dynamic Transfer Function
FIS	Fixed Interval Smoothing
GRW	Generalised Random Walk
IRW	Integrated Random Walk
KF	Kalman Filter
LLT	Local Linear Trend
ML	Maximum Likelihood
NAN	Not-A-Number
NMSS	Non-Minimal State Space
NVR	Noise Variance Ratio
PACF	Partial Autocorrelation Function
PIP	Proportional-Integral-Plus
RIV	Refined Instrumental Variable
RIVSID	Refined Instrumental Variable System Identification (CAPTAIN folder)
RW	Random Walk
SDARX	State Dependent Auto-Regression with eXogenous variables
SDP	State Dependent Parameter
SDTF	State Dependent Transfer Function
SISO	Single Input, Single Output
SRIV	Simplified Refined Instrumental Variable
SRM	Smoothed Random Walk
SS	State Space
TDC	True Digital Control
TDCONT	True Digital CONTROL (CAPTAIN folder)
TF	Transfer Function
TVP	Time Variable Parameter
TVPMOD	Time Variable Parameter MODels (CAPTAIN folder)
UC	Unobserved Components

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# CHAPTER 1

## INTRODUCTION

The CAPTAIN Toolbox is a collection of MATLAB functions for non-stationary time series analysis, forecasting and control. The toolbox is useful for system identification, signal extraction, interpolation, forecasting, data-based mechanistic modelling and control of a wide range of linear and non-linear stochastic systems. The toolbox consists of three modules, organised into three folders (or directories) as follows:

- **TVPMOD: Time Variable Parameter (TVP) MODEls.** For the identification of unobserved components models, with a particular focus on state-dependent and time-variable parameter models (includes the popular dynamic harmonic regression model).
- **RIVSID: Refined Instrumental Variable (RIV) System Identification** algorithms. For optimal RIV estimation of multiple-input, continuous- and discrete-time Transfer Function models.
- **TDCONT: True Digital CONTROL (TDC).** For multivariable, non-minimal state space control, including pole assignment and optimal design, and with backward shift and delta-operator options.

In addition to the present Getting Started Guide, separate documents are available for each of the TVPMOD and RIVSID modules of the toolbox. These include full descriptions of the algorithms and models, and MATLAB code associated with the included demos. By contrast, the TDCONT module links specifically to the book *True Digital Control: Statistical Modelling and Non-Minimal State Space Design* (Taylor *et al.* 2013) and does not have a separate handbook: in fact, the demos reproduce the figures within this book.

### 1.2 Use of the CAPTAIN Toolbox

1. Wherever the CAPTAIN Toolbox has been used to generate results which have then been used in any written work, please reference it using the text below:

Taylor, C.J., Pedregal, D.J., Young, P.C. and Tych, W. (2007) Environmental Time Series Analysis and Forecasting with the Captain Toolbox, *Environmental Modelling and Software*, **22**, pp. 797-814 (<http://dx.doi.org/doi:10.1016/j.envsoft.2006.03.002>).

2. The CAPTAIN Toolbox is supplied in good faith and whilst all efforts have been made to assure that it is free from errors and bugs, the authors and Lancaster University accept no liability for erroneous results obtained through the use of the Toolbox.

3. Installation of the CAPTAIN Toolbox is carried out at the user's own risk and neither the authors nor Lancaster University accept any responsibility in the unlikely event of installation resulting in detrimental effects to the user's computer hardware or software.
4. The user may not redistribute the Toolbox to any third party.
5. Ownership of the Toolbox is retained by the authors. The web download is an evaluation copy of the Toolbox. If you wish to continue using the Toolbox beyond the evaluation period, please contact C. James Taylor at the address below.

E-mail: [c.taylor@lancaster.ac.uk](mailto:c.taylor@lancaster.ac.uk)  
Web: <http://www.lancs.ac.uk/staff/taylorcj/>

6. Any part of the CAPTAIN Toolbox may be used for scientific or educational purposes. For commercial applications, permission is required from the authors.
7. CAPTAIN is provided without formal support, although questions and bug reports can be emailed to the authors.

### 1.3 How to Install

CAPTAIN is usually distributed as a mixture of pre-parsed MATLAB pseudo-code (P-files) and conventional M-files. It is organised into three self-contained modules, TVPMOD (Time Variable Parameter MODels), RIVSID (Refined Instrumental Variable System Identification) and TDCONT (True Digital CONTrol).

Each module consists of a folder (sub-directory) containing a set of functions, demos and help information. Some users may wish to install only one or two of these modules depending on their requirements. Each module is independent of the others (although a small number of optional demos require more than one module).

The following instructions assume that MATLAB is already installed. Copy the M- and P-files to directories where you want the toolbox to reside. For example, if you are installing all three modules, these might be:

```
Program Files\Matlab\Toolbox\rivsid  
Program Files\Matlab\Toolbox\tdcont  
Program Files\Matlab\Toolbox\tvpmod
```

Start MATLAB and add the above locations of the toolbox to your path. You can use the MATLAB **addpath** function at the Command Line or the MATLAB menu-based user interface to do this. Please refer to your MATLAB documentation for more information.

### 1.4 How to Uninstall

Start MATLAB and remove the CAPTAIN toolbox paths. You can use the **rmpath** command or the menu-based user interface to do this (refer to the MATLAB user manual). Delete the CAPTAIN toolbox folders and their entire contents.

## 1.5 Starting the Demos

Once installed, typing **captdemo** in the MATLAB Command Window starts a simple graphical user interface for access to the Command Line demos. If this does not work, check that you have correctly added the toolbox locations to your MATLAB path. After typing **captdemo** (but before starting one of the demos) you can check the Command Window for a list of which modules have been added i.e.

```
>> captdemo
Checking MATLAB path...
  RIVSID installed
  TVPMOD installed
  TDCONT installed
```

Or, to open the Command Line demos for each module directly,

```
>> rivdemo
>> tvpdemo
>> tdcdemo
```

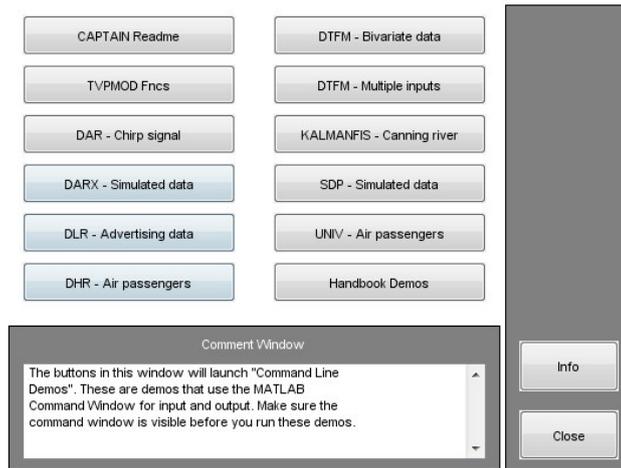
In each case, a simple graphical user interface provides access to the Command Line demos (e.g. Fig. 1.1). The latter utilise the Command Window for input and output, as well as generating graphs in a separate Figure Window, so make sure both of these are visible. Experience suggests that one of the most effective ways to get started with CAPTAIN is to examine each Command Line demo in turn and then to adapt them for each new data set of interest. Demo scripts can be opened in the MATLAB editor.

To obtain a full list of user functions for each module, type **help rivsid**, **help tdcont** or **help tvpmod** in the Command Window, replacing rivsid, tdcont or tvpmod if necessary with the actual name of the folder (directory) chosen when you first installed the toolbox. To illustrate, the first few lines of the function list for TVPMOD are shown below.

```
>> help tvpmod
Captain Toolbox
Time Variable Parameter Models

Unobserved Components Models.
  dhr      - Dynamic Harmonic Regression analysis.
  dhropt   - DHR hyper-parameter estimation.
  irwsm    - Integrated Random Walk smoothing and decimation.
  irwsm    - Integrated Random Walk smoothing and decimation.
  irwsmopt - IRWSM hyper-parameter estimation.
  univ     - Trend with Auto-Regression component.
  univopt  - Trend with AR hyper-parameter estimation.

Time Variable and State Dependent Parameter Models.
  dar      - Dynamic Auto-Regression and time frequency analysis.
  daropt   - DAR hyper-parameter estimation.
  darsp    - DAR spectra plot.
```



**Figure 1.1** Demos for the TVPMOD module obtained by typing `tvpdemo` at the MATLAB Command Line.

Each function includes help information obtained in the usual manner e.g. `help irwsm`. Default input arguments are shown in parenthesis while (\*) implies no default (hence a user input argument is always required for this variable). Some functions include more information, readable using e.g. `type irwsm` or `edit irwsm` (see Chapter 3 for details).

## 1.6 Caveat

CAPTAIN is presently developed for MATLAB R2017b onwards, although some backwards compatibility is maintained at the discretion of the authors. Note that, because of updates over time to MATLAB and CAPTAIN, you may obtain different numerical results when using the toolbox than shown by the examples below. Also, please check the help information within MATLAB for the latest calling syntax and default values of each toolbox function, since these may change over time.

## CHAPTER 2

### TOOLBOX OVERVIEW

CAPTAIN is a MATLAB compatible toolbox for non-stationary time series analysis and forecasting. Based around a powerful state space framework, CAPTAIN extends MATLAB to allow, in the most general case, for the identification of Unobserved Components (UC) models. Here, the time series is assumed to be composed of an additive or multiplicative combination of different components that have defined statistical characteristics but which cannot be observed directly. With Maximum Likelihood estimation of most models and the inclusion of several popular model forms, such as the Basic Structural Model of Harvey (1989) and the Dynamic Linear Model of West and Harrison (1989), together with a standard set of data pre-processing, system identification and model validation tools, CAPTAIN is a wide-ranging package for signal processing and general time series analysis.

Uniquely, however, CAPTAIN focuses on Time Variable Parameter (TVP) models, where the stochastic evolution of each parameter is assumed to be described by a generalised random walk process (Jakeman and Young, 1981). In this regard, the state space formulation utilised is particularly well suited to estimation based on optimal recursive estimation, in which the time variable parameters are estimated sequentially whilst working through the data in temporal order. In the off-line situation, where all the time series data are available for analysis, this Kalman filtering operation (Kalman, 1960) is accompanied by optimal recursive smoothing. Here the estimates obtained from the forward pass filtering algorithm are updated sequentially whilst working through the data in *reverse* temporal order using a backwards-recursive Fixed Interval Smoothing (FIS) algorithm (Bryson and Ho, 1969).

In this manner, CAPTAIN provides novel tools for TVP analysis, allowing for the optimal estimation of dynamic regression models, including linear regression, auto-regression (Young, 1998b) and harmonic regression (Young *et al.*, 1999). Furthermore, a closely related algorithm for state dependent parameter estimation provides for the non-parametric identification and forecasting of a very wide class of nonlinear systems, including chaotic systems. The identification stage in this process again exploits the recursive FIS algorithms, combined with special data re-ordering and ‘back-fitting’ procedures, to obtain estimates of any state dependent parameter variations (Young, 2000).

Of course, in many cases, specifying time invariant parameters for the model yields the equivalent, conventional, stationary model. In this regard, one model that has received special treatment in the toolbox is the multiple-input, single-output Transfer Function (TF)

model. CAPTAIN includes functions for robust unbiased identification and estimation of both discrete- time (Young, 1984, 1985) and continuous- time (Young, 2002) TF models. One advantage of the TF model is its simplicity and ability to characterise the dominant modal behaviour of a dynamic system. This makes such a model an ideal basis for control system design.

In the latter regard, the toolbox includes a set of functions for True Digital Control (TDC), based on the Proportional-Integral-Plus (PIP) control system design methodology (Young *et al.*, 1987; Taylor *et al.* 2000, 2013). The underlying philosophy of the approach is that the entire design procedure, from the identification and estimation of a suitable model through to the practical implementation of the final control algorithm, is carried out in discrete time. This differs from many conventional digital controllers, where an inherently continuous time algorithm is digitised for implementation purposes. Indeed, CAPTAIN has been successfully utilised for the design of PIP control systems for many years (e.g. Taylor *et al.*, 2004, 2013; Taylor and Shaban, 2006).

Some of the estimation algorithms considered here were developed originally in the 1960/1970/1980's for the CAPTAIN and microCAPTAIN time series analysis and forecasting packages (MS-DOS based). The associated optimisation algorithms were developed in the 1980/1990's and were used in the latest version of microCAPTAIN (Young and Benner, 1991). However, the MATLAB implementation is much more flexible than microCAPTAIN and includes the latest innovations and improvements to the algorithms. Note that the present text refers exclusively to this CAPTAIN Toolbox for MATLAB (Taylor *et al.*, 2007).

## 2.1 Modelling Philosophy

As we look around us, we perceive complexity in all directions: environmental, biological and ecological systems, socio-economic systems, and some of the more complex engineering systems – they all appear to be complicated assemblages of interacting processes, many of which are inherently nonlinear dynamic systems, often with considerable uncertainty about both their nature and their interconnections. It is not too surprising, therefore, that the mathematical models of such systems, as constructed by scientists, social scientists and engineers, are often similarly complex.

What is perhaps surprising, however, is the apparently widespread belief that such systems can be described very well, if not exactly, by *deterministic* mathematical equations, with little or no quantification of the associated uncertainty. Such deterministic reductionism leads inexorably to large, nonlinear simulation models which reflect the popular view that complex systems must be described by similarly complex models.

The CAPTAIN toolbox has evolved from a different Data-Based Mechanistic (DBM) modelling philosophy, which is almost the antithesis of deterministic reductionism. DBM models are obtained initially from the analysis of observational time-series but are only considered credible if they can be interpreted in physically meaningful terms. It is a philosophy that emphasises the importance of parametrically efficient, low order, dominant mode models, as well as the development of stochastic methods and the associated

statistical analysis required for the identification and estimation of such models. Furthermore, it stresses the importance of explicitly acknowledging the basic uncertainty that is essential to any characterisation of physical, chemical, biological and socio-economic processes.

Previous publications map the evolution of the DBM philosophy and its methodological underpinning. Such publications utilise the approach for the analysis of numerous natural and man-made systems. An incomplete list includes: Beck and Young (1975); Jarvis *et al.* (1999); Parkinson and Young (1998); Price *et al.* (1999, 2000, 2001); Shackley *et al.* (1998); Tych *et al.* (1999); Ye *et al.* (1998); Young (1978, 1981; 1983, 1984; 1985; 1993a, 1993b; 1994; 1998a, 1998b, 1999a, 1999b, 2000, 2001a, 2001b, 2002); Young and Beven (1994); Young and Lees (1993); Young and Minchin (1991); Young and Pedregal (1996; 1997; 1998, 1999a, 1999b); Young *et al.* (1996, 1997, 1999, 2000).

Naturally, these publications introduce a wide range of modelling tools, encompassing various model structures and identification algorithms. However, they can be broadly categorised into the four closely related and overlapping themes below.

1. Many of the tools that underpin the DBM modelling philosophy can be unified in terms of the discrete-time UC model. Here, the components may include a trend or low frequency component, a seasonal component (e.g. annual seasonality), additional sustained cyclical or quasi-cyclical components, stochastic perturbations, a component to capture the influence of exogenous input signals and so on. CAPTAIN allows for a wide range of such components.
2. Nonstationary and nonlinear signal processing based on the identification and estimation of stochastic models with time varying parameters. In this case, the term ‘nonstationarity’ is assumed to mean that the statistical properties of the signal, as defined by the parameters in an associated stochastic model, are changing over time at a rate which is ‘slow’ in relation to the rates of change of the stochastic state variables in the system under study. Although such nonstationary systems exhibit nonlinear behaviour, this can often be approximated well by TVP (or piece-wise linear) models, the parameters of which are recursively estimated.
3. Further to item 2. above, if the changes in the parameters are functions of the state or input variables (i.e. they actually constitute stochastic state variables), then the system is truly nonlinear and likely to exhibit severe nonlinear behaviour. Normally, this cannot be approximated in a simple TVP manner; in which case, recourse must be made to alternative, and more powerful in this context State Dependent Parameter (SDP) modelling methods.
4. Finally, if the essential small perturbation behaviour of the system can be approximated by linearised TF models, then robust unbiased, Refined Instrumental Variable (RIV) and Simplified Refined Instrumental Variable (SRIV) algorithms are employed. Here, either discrete-time TF models represented in terms of the backward shift operator (often denoted in the statistical and engineering literature by either  $z^{-1}$ ,  $q$ ,  $B$  or  $L$ ,

where the latter is utilised in the present text) or continuous-time TF models based on the Laplace Transform  $s$ -operator are identified and estimated.

In recent versions of CAPTAIN, items 1–3 are addressed by **TVPMOD**, while item 4 is implemented in **RIVSID**. Finally, the independently developed **TDCONT** module uses discrete-time multivariable TF models obtained from RIVSID for control system design.

## 2.2 MATLAB

MATLAB is a high performance language published by The MathWorks, Inc., integrating computation, visualisation and programming in a single environment (MathWorks, 2017). CAPTAIN is a collection of MATLAB functions for the estimation of UC, TVP, SDP and TF models, and for PIP control system design. By also including a number of additional functions for data pre-processing, system identification and model validation, CAPTAIN provides a powerful all round package for the analysis of complex stochastic systems (Taylor *et al.* 2007). The following sections introduce the three main areas of functionality.

## 2.3 TVPMOD: Time Variable Parameter MODEls

**Unobserved Components models:** CAPTAIN includes a range of UC models, a number of which are unique to this toolbox. In particular, the Dynamic Harmonic Regression (DHR) model, estimated using the function **dhr**, is very useful for signal extraction and forecasting of periodic or quasi-periodic series. This function provides smoothed estimates of the series, as well as all its components (trend, fundamental frequency and harmonic components), together with the estimated changing amplitude and phase of the latter. Typical applications are for the analysis of periodic environmental and economic time-series; restoration of noisy signals with gaps or other aberrations; and the evaluation of temporal changes in environmental data etc. Furthermore, the same function allows for the estimation of the well-known Basic Structural Models (BSM) of Harvey (1989).

It should be pointed out that, while it is sometimes convenient to categorise the functionality of the toolbox, there is considerable overlap between the methodological areas chosen. For example, the DHR model is a particular case of the general stochastic TVP model discussed in the following subsection. In this regard, the hyper-parameters of the model, which define the statistical properties of the time variable parameters, need to be estimated in some manner. CAPTAIN provides three approaches, all through the function **dhropt**, namely: Maximum Likelihood (ML) based on prediction error decomposition; minimisation of the multiple-steps-ahead forecasting errors; and a special frequency domain optimisation, based on fitting the model pseudo-spectrum to the logarithm of the Auto-Regression (AR) spectrum.

An alternative to **dhr/dhropt** is provided by the pair **univ/univopt**, which allow for the estimation of various additional UC model forms. Here, the trend is extracted from the time series and a perturbational component about the trend is modelled as a pure AR component. Although they may also be utilised for modelling seasonal series, **univ/univopt** are particularly useful in cases where the periodic behaviour of the perturbation about the trend is not very marked. In this case, the models are estimated

using either standard statistical methods or a sequential spectral decomposition approach that has been developed for the toolbox in order to avoid identifiability problems.

**Time Variable Parameter models:** the class of TVP, or ‘dynamic’, regression models, includes: Dynamic Linear Regression (DLR), Dynamic Harmonic Regression (DHR), Dynamic Auto-Regression (DAR), Dynamic Auto-Regression with eXogenous variables (DARX) and the closely related Dynamic Transfer Function (DTF) model. It should be noted that the term ‘dynamic’, which is used to differentiate time variable parameter regression models from their standard constant parameter relatives, is somewhat misleading, since not all of these models are inherently dynamic in a systems sense. However, it is a common term in certain areas of statistics (see e.g. West and Harrison, 1989 and the references therein) and is retained for this reason.

CAPTAIN provides functions that allow for the optimal estimation of all these dynamic regression models. In each case, Fixed Interval Smoothing (FIS) estimates of the TVPs are obtained, under the assumption that the parameters vary as one of a family of generalised random walks namely: Random Walk (RW); Integrated Random Walk (IRW); Smoothed Random Walk (SRW); and Local Linear Trend (LLT). The associated filtering and FIS algorithms are accessible via shells, namely the functions **dlr**, **dhr**, **dar**, **darx** and **dtfm**. Since the regressors are freely defined by the user, the most flexible toolbox function for TVP analysis is **dlr**, which can include all the remaining models as special cases. The other functions all restrict the model to the most commonly used forms. For example, **dhr** automatically constrains the regressors to model harmonic components. As one of the key tools for estimating UC models, it has already been discussed above.

At this juncture, it is worth pointing out that CAPTAIN includes the functions **mar** and **arspec** for Auto-Regression (AR) model and spectrum estimation. However, in the context of dynamic regression, **dar** and **darsp** are instead useful for evaluating *changing* signal spectra and *time*-frequency analysis based on DAR models, since they provide the AR spectrum at each point in time based on the locally optimum time variable AR parameters.

Further to this, **darx** is an extension of the DAR model to include measured eXogeneous or input time series that are thought to affect the output, while **dtfm** augments the model in order to allow for coloured noise in the output signal. The latter function employs instrumental variables in the solution to ensure that the parameter estimates are unbiased. In this manner, the functions **darx** and **dtfm** are truly dynamic in a systems sense and form a link between the dynamic regression analysis considered here and the dedicated TF modelling component of the toolbox discussed in the next section.

In the case of **dlr**, **dar**, **darx** and **dtfm**, the Noise Variance Ratio (NVR) and other hyper-parameters, which define the statistical properties of the TVP’s, are optimised via ML based on prediction error decomposition. The relevant toolbox functions are **dlropt**, **daropt**, **darxopt** and **dtfmopt**. Hence, in comparison with most other algorithms for TVP estimation, the main innovations in CAPTAIN are this automatic hyper-parameter optimisation, the provision of FIS rather than the filtered TVP estimates and the various special uses outlined above.

**State Dependent Parameter models:** the approach to TVP estimation discussed above works very well in situations where the parameters are slowly varying when compared to the observed temporal variation in the measured system inputs and outputs. Although such models are nonlinear systems, since the same inputs, injected at different times, will elicit quite different output responses, the resultant nonlinearity is fairly mild. It is only when the parameters are varying at a rate commensurate with that of the system variables themselves that the model behaves in a heavily nonlinear or even chaotic manner. For such cases, CAPTAIN includes a novel algorithm for state dependent parameter estimation, **sdp**, allowing for the non-parametric identification and forecasting of a very wide class of nonlinear systems.

Specifying time invariant parameters for the above TVP models usually yields the equivalent stationary time series model. In this manner, many of the functions above may be utilised to estimate either the well-known conventional model or the more sophisticated TVP version, depending on the input arguments chosen.

System identification is inherent to the modelling approach utilised by most of the functions already discussed. Identification tools not yet mentioned include, for example, **acf** to determine the sample and partial autocorrelation function; **ccf** for the sample cross-correlation; **period** to estimate the periodogram; and **statist** for some sample descriptive statistics. Furthermore, **del** generates a matrix of delayed variables, **fcast** may be employed to prepare data for forecasting and interpolation, and **irwsm** is used for smoothing, decimation or for fitting a simple trend to a time series. These examples complement various other included auxiliary functions (see toolbox help for details).

## 2.4 RIVSID: Refined Instrumental Variable System Identification

**Multi-Input Transfer Function models:** although there are numerous algorithms for estimating TF models, the primary technique employed in CAPTAIN, is the least squares-based instrumental variable approach. Here, an adaptive auxiliary model is introduced into the solution in order to avoid parameter bias and to optimally filter the data, so making the estimation more statistically efficient. In particular, CAPTAIN provides the recursive and en-block RIV algorithms, as well as more conventional least squares based approaches, primarily through the functions **rivbj** (for discrete-time systems) and **rivcbj** (continuous-time). Both these functions return the modelling results in the form of a special matrix from which the various parameters and standard errors may be extracted using **getparbj**. Such parameters are subsequently be utilised for simulation and forecasting through conventional MATLAB commands like **filter**, or by using SIMULINK<sup>®</sup> (MathWorks, 2017).

For a given physical system, an appropriate structure first needs to be identified, i.e. the most appropriate values for the time delay and the orders of the numerator and denominator polynomials in the TF. In this regard, CAPTAIN utilises two functions, namely **rivbjid** (discrete-time) and **rivcbjid** (continuous-time), which provide numerous statistical diagnostics associated with the model. These include the Coefficient of Determination  $R_T^2$ , based on the response error, which is a simple measure of model fit; and the more sophisticated Young Identification Criterion (YIC), which provides a combined measure of fit and parametric efficiency.

Since 2007, CAPTAIN has allowed for the estimation of TF models with an autoregressive, moving average (ARMA) noise component, i.e. full Box-Jenkins (BJ) models. The functions for TF modelling listed above allow for such BJ models (or simpler models as special cases using the input arguments). However, older CAPTAIN algorithms that are limited to an AR noise model are still included for backwards compatibility (with long time users of the toolbox) and sometimes as a back-up option. These functions are called **riv/rivid**, **rivc/rivcid** and **getpar**.

Finally, the toolbox includes various data preparation and auxiliary functions, including, for example, **prepz** to prepare data for input-output modelling and **prbs** for generating a Pseudo Random Binary Signal (PRBS), among others.

## 2.5 TDCONT: True Digital CONTROL (TDC)

**True Digital Control:** following the identification of a suitable discrete-time TF model, PIP control systems are determined using either the **pip** or **pipopt** functions, for pole assignment or linear quadratic optimal design respectively. These functions are for the single input, single output (SISO) case, while **mpipdc** and **mpiplq** are used for multivariable PIP control design (for which **mtf2mfd** is used to convert a multivariable TF into the required Matrix Fraction Description). Furthermore, **dlqrqf** provides direct access to the iterative linear quadratic regulator solution for either the SISO or multivariable cases; while **tdclib** is the Simulink<sup>®</sup> library for various PIP control structures, including the conventional feedback form and an alternative forward path approach.

The PIP approach is based on the definition of Non-Minimal State Space (NMSS) models, using either **nmss** (SISO) or **mfd2nmss** (multivariable), so that full state variable feedback control can be implemented directly from the measured input and output signals of the controlled process. The PIP controller can be interpreted as a logical extension of Proportional-Integral-Derivative (PID) control, with additional dynamic feedback and input compensators introduced automatically, when the process has second order or higher dynamics or pure time delays greater than one sampling interval.

Finally, the TDCONT module includes a number of auxiliary functions and tools for designing other types of control system, including delta operator design (**dpip**), Monte Carlo simulation (**mcsim**) and Generalised Predictive Control (**gpc**).

## CHAPTER 3 EXAMPLES TO GET STARTED

The following examples aim to provide a brief illustration of toolbox functionality for users already familiar with the methodology, or at least to introduce some of the ideas to the open minded reader who is not. In this regard, it should be pointed out that formal stochastic descriptions of the models are omitted from this Getting Started Guide.

Installation instructions and conditions of use are given in Chapter 1. It is assumed that all three modules, RIVSID, TDCONT and TVPMOD are installed. Since CAPTAIN is largely a command line toolbox, it is also assumed that the reader is already familiar with basic MATLAB usage, such as loading data, plotting graphs and writing simple M-files. Introductory guides include Etter (1993) and Biran and Breiner (1995). Hence, for brevity, the straightforward MATLAB code to label the plots and set the axis limits etc. is not necessarily shown in the examples below.

### Example 3.1 IRW smoothing of the airline passenger series

To plot the well-known airline passenger series (e.g. Box and Jenkins, 1970), enter the following text at the MATLAB Command Window prompt,

```
>> load air.dat
>> plot(air)
>> title('thousands of passengers per month (1949-1960)')
```

These data are included in the TVPMOD module for demonstration purposes, in a standard text file. If an error occurs, then check that you have correctly added the toolbox location to your MATLAB path.

We will smooth these data using **irwsm**. In general, the brief calling syntax for each function in CAPTAIN is obtained by entering its name without any input arguments:

```
>> irwsm

irwsm  Integrated Random Walk smoothing and decimation

[ys,deriv,fitse,trse,derivse,y0,PkN,ers,ykk1,er]=...
                                             irwsm(y,TVP,nvr,Int,dt,delt)
```

More information is provided using the standard **help** command, as illustrated below. In this case, each input argument is described in turn, followed by the output arguments and any other information.

```
>> help irwsm

irwsm  Integrated Random Walk smoothing and decimation

[ys,deriv,fitse,trse,derivse,y0,PkN,ers,ykk1,er]=...
      irwsm(y,TVP,nvr,Int,dt,delt)

y: Time series (*)
TVP: Model type (RW=0, IRW=1, DIRW=2) (1)
nvr: NVR hyper-parameter (1605*(1/(2*dt))^4)
Int: Vector of variance intervention points (0)
dt: decimation rate (1)
     with dt>1 only the following returned arguments
     are decimated: ys, deriv, fitse, trse, derivse, y0
delt: sampling rate (1)

ys: Decimated (or simply smoothed if dt=1) series
deriv: Derivatives
fitse: Standard error of model fit (including observation noise)
trse: Trend (state) standard error
derivse: standard error of the remaining states (trend derivs.)
y0: Interpolated data
...
```

The on-line help messages in CAPTAIN are deliberately concise. This is so that an experienced user can find information quickly. However, many functions include supplementary information, readable using:

```
>> type irwsm
```

The supplementary information can also be examined by opening the m-file in an editor and scrolling down to find it:

```
>> edit irwsm
```

In the help information, default values for any optional inputs are given in brackets, whilst any necessary inputs, such as the data vector **y** above, are listed with an asterix (\*). In this case, the default **TVP** = 1 implies the following model based on an IRW model plus noise,

$$y_t = T_t + e_t \quad (3.1)$$

$$T_t = 2T_{t-1} - T_{t-2} + \eta_t \quad (3.2)$$

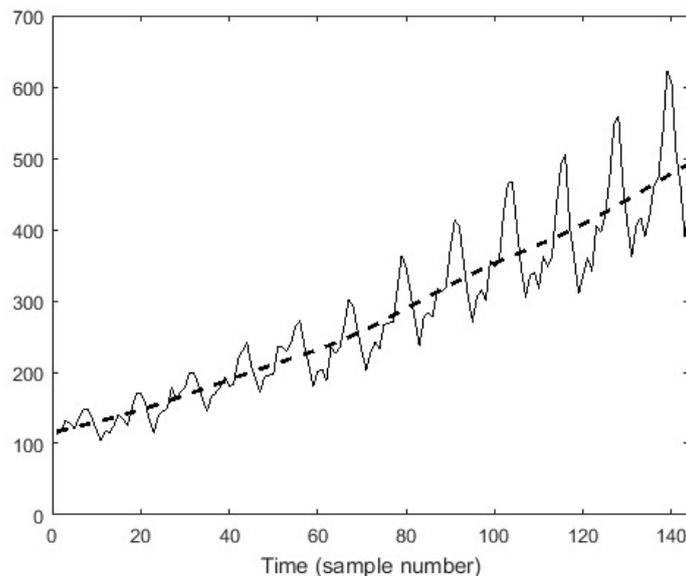
where  $y_t$  is the time series,  $T_t$  is the smoothed signal at sample  $t$ , returned by **irwsm** as the first output argument, and  $T_{t-1}$  and  $T_{t-2}$  are their values at the two previous samples,

respectively. Here,  $T_t$  is effectively a time variable parameter, whose stochastic evolution in the form of an IRW is described by equation (3.2). Finally,  $\eta_t$  and  $e_t$  are independent zero mean white noise sequences with variance  $q^2$  and  $\sigma^2$ , representing the system disturbances and measurement noise respectively. The present Getting Started Guide omits a full explanation of this model and the state space form actually used for estimation: see additional toolbox documentation for details.

Empty variables [ ] may be used to indicate default values when a mixture of defaults and user specified arguments are required. For example, a smoothed trend is fitted to the airline passenger series as follows,

```
>> load air.dat
>> t = irwsm(air, [], 0.0001); % equivalent to t = irwsm(air, 1, 0.0001)
>> plot([air t])
```

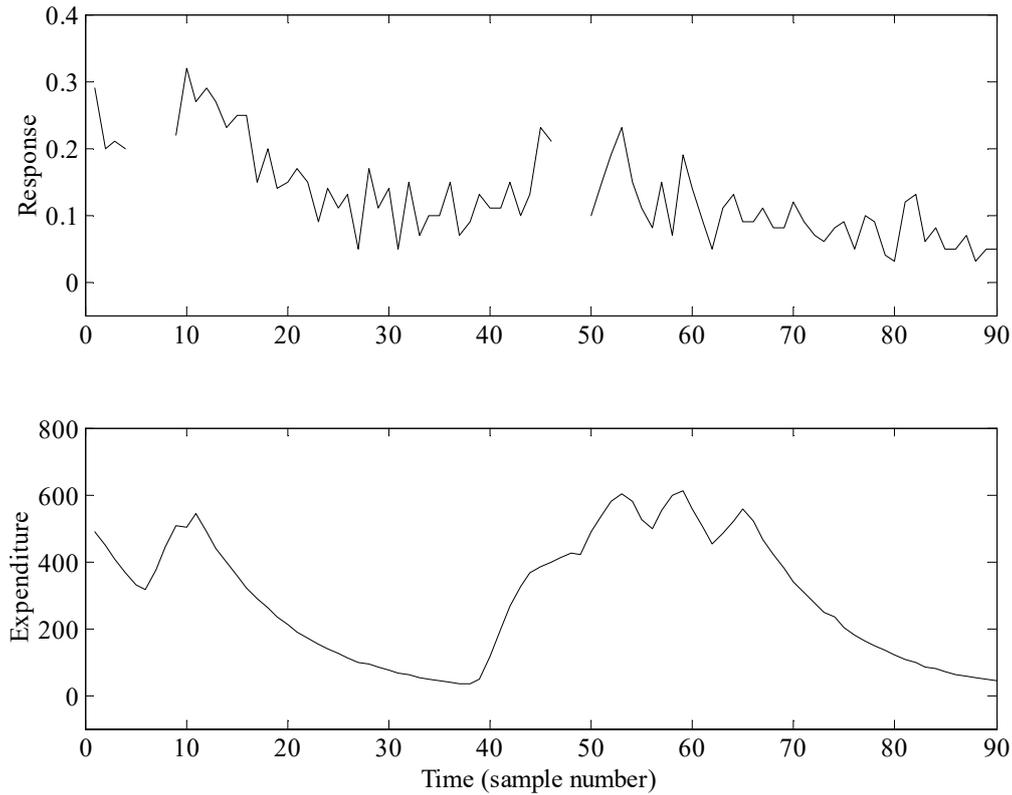
The plot compares the smoothed and original series, as illustrated in Fig. 3.1. Note that the 3rd input argument to `irwsm` specifies the associated Noise Variance Ratio (NVR) hyperparameter. Defined here as  $q^2/\sigma^2 = 0.0001$ , this variable is closely related to the bandwidth of the filter. Try using values of e.g. 0.1 and 0 for this fourth input argument.



**Figure 3.1** Thousands of airline passengers per month (1949-1960) and IRW trend.

### Example 3.2 Interpolation of advertising data using DLR

Dynamic Linear Regression or DLR provides an excellent vehicle for the analysis of data in areas such as economic, business and social data, where regression analysis is a popular method of modelling relationships between variables and where these relationships may change over time. In this regard, consider the following straightforward demonstration from the toolbox, which examines the relationship between a particular company's expenditure on advertising and their measure of the public's response to this expenditure, as illustrated in Figure 3.2.



**Figure 3.2** Scaled advertising data plotted against an arbitrary fixed sampling rate.  
Top: response to advertising. Bottom: expenditure on advertising.

For the purposes of the example, these confidential data have been scaled in an arbitrary manner, so no units are given in the plots. The output response data are in the range 0-1, where a larger number implies a more successful response to the advertising. It is clear that the response data contain missing values, represented in MATLAB by special Not-a-Number or **nan** values and forming gaps in the top plot of Figure 3.2. The filtering and smoothing algorithms implemented in CAPTAIN automatically account for these.

For a preliminary analysis of these data, we will utilise the following model,

$$y_t = T_t + b_t u_t + e_t \quad t = 1, 2, \dots, 90 \quad (3.3)$$

where  $y_t$  is the response and  $u_t$  is the expenditure, while  $T_t$  and  $b_t$  are the time variable parameters. Finally,  $e_t$  is a serially uncorrelated and normally distributed Gaussian sequence with zero mean value and variance  $\sigma^2$ . Note that a full description of the general DLR methodology and state space model is omitted from this Getting Started Guide.

For constant parameters  $T_t = T$  and  $b_t = b$ , equation (3.3) takes the form of a conventional regression model based on the equation of a straight line. However, here we utilise **dlropt** to determine if the optimal values of the parameters, in a ML sense, in fact vary over time. In this regard, assuming a default random walk model for each of the parameters, the associated NVR hyper-parameters are estimated as follows,

```

>> load adv.dat
>> u = adv(:, 1); % expenditure
>> y = adv(:, 2); % response
>> z = [ones(size(u)) u]; % regressors
>> nvr = dlropt(y, z)
nvr =
    0.0078
    0.0000

```

While **dlropt** is running, a window will briefly appear on screen indicating the optimisation algorithm being utilised, together with an update of the Log-Likelihood.

It should be pointed out that default values for the toolbox have been carefully chosen, in order to be as widely applicable as possible. In the present case, the default initial conditions and optimisation settings converge to a solution without any problem, hence only the first two input arguments are required.

From this analysis, it appears that the  $T_i$  level or trend parameter varies significantly over time (NVR = 0.0078), while the  $b_i$  slope parameter is relatively time invariant and has a NVR value close to zero. To determine the fit and parameters,

```

>> [fit, fitse, par] = dlr(y, z, [], nvr);

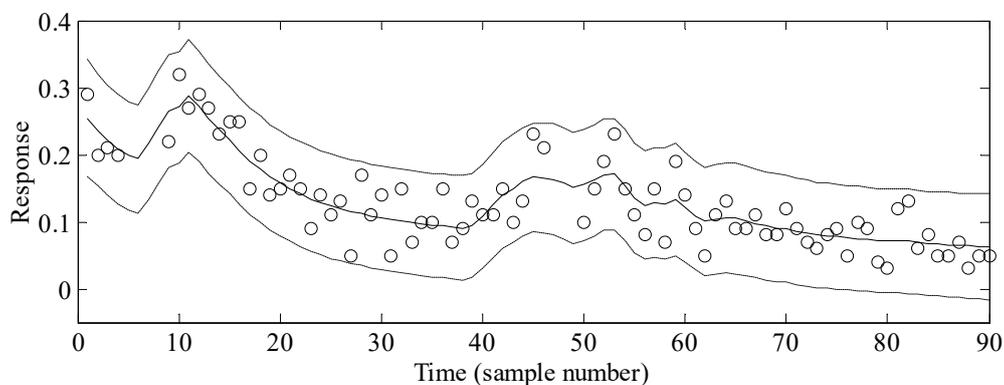
```

By default, **dlr** assumes NVR's of zero, so the 4th input argument above is necessary to specify the previously optimised values. The 3rd input argument selects the model type: in this case, empty brackets imply the default random walk model. Examination of the parameters, returned as the first and second columns of **par**, show how these evolve gradually over time (not plotted here). The model fit and associated standard errors are shown in Figure 3.3, which is obtained using the code below,

```

>> plot(y, 'o')
>> hold on
>> plot(fit)
>> plot(fit+2*fitse, ':')
>> plot(fit-2*fitse, ':')

```



**Figure 3.3** Scaled response to advertising plotted against an arbitrary fixed sampling rate. Data (circles), DLR fit (solid) and standard errors (dashed).

It is clear from Figure 3.3 that the data all lie within the standard error bounds. Note also that no user intervention was required to interpolate over the missing response data: both **fit** and **par** apply over the entire time series. Refer to the on-line help for a full list of optimisation settings and output arguments. For example, **dlr** can return the interpolated output **y0**, consisting of the original series with any missing data replaced by the model fit.

### Example 3.3 Transfer Function model estimation using RIV

Many control systems, both classical and modern, are analysed by means of TF models. Indeed, CAPTAIN has been successfully utilised for the design of control systems for many years, particularly with regards to the development of PIP control methods (see Taylor *et al.* 2013 for numerous examples). One practical application is concerned with forced ventilation in animal houses (Taylor *et al.*, 2004). Here, uncontrolled data are first collected in order to identify the dominant dynamics of the fan.

For a particular test installation at the Katholieke Universiteit Leuven, the SRIV algorithm, combined with the  $R_T^2$  and YIC identification criteria, reveal that a first order model with 6 seconds time delay provides the best estimated model and most optimum fit to the data across a wide range of operating conditions. In a typical experiment, based on a 2 second sampling rate, the SRIV algorithm yields the following difference equation,

$$y_t = 0.438y_{t-1} + 79.8 u_{t-3} \quad (3.4)$$

where  $y_t$  is the airflow rate ( $\text{m}^3/\text{h}$ ) and  $u_t$  is the applied voltage to the fan expressed as a percentage. Equation (3.4) shows that the output variable  $y_t$ , is a simple linear function of its value at the previous sample and the delayed input variable. Equation (3.4) may alternatively be represented in terms of the backward shift operator  $L$ , i.e.  $L^j y_t = y_{t-j}$ , by the following discrete-time TF model,

$$y_t = \frac{79.8L^3}{1-0.438L} u_t \quad (3.5)$$

The response of the model (3.5) closely follows the noisy measured data, as illustrated by Figure 3.4. These data are included with CAPTAIN for demonstration purposes and the associated MATLAB commands for estimating the model are shown below.

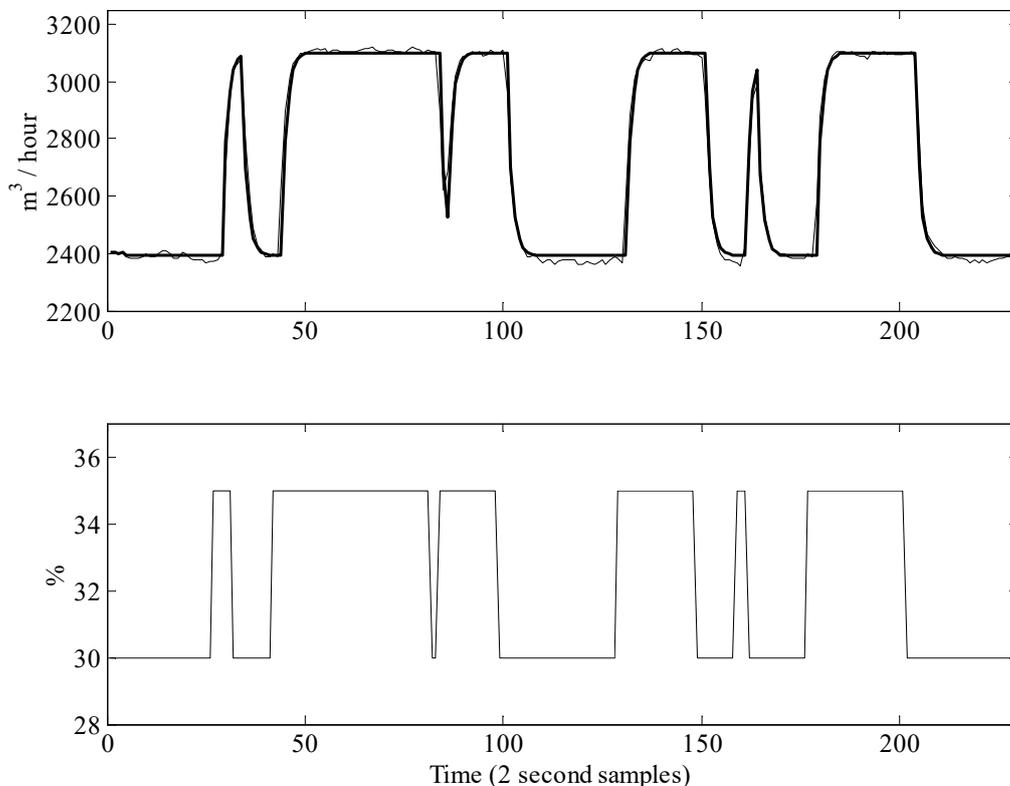
```
>> load vent.dat
>> [z, m] = prepz(vent, [], 25);
>> [th, stats, e] = riv(z, [1 1 3 0]);
>> [at, bt] = getpar(th)
at =
    1.0000    -0.4381
bt =
         0         0         0    79.7835
>> rt2 = stats(3)
rt2 =
    0.9873
```

```
>> subplot(211); plot([z(:, 1) z(:, 1)-e]+m(1))
>> subplot(212); plot(z(:, 2)+m(2))
```

Here, the experimental data are organised into matrix form, with the first column of **vent** consisting of the output variable  $y_t$ , and the second the input variable  $u_t$ . The function **prepz** is utilised to prepare the data for modelling. In particular, the 3rd input argument subtracts the mean of the first 25 samples from the data in order to remove the baseline from the series. Such data pre-processing sometimes yields better results in the context of TF model estimation.

The TF is estimated using **riv**, where the second input argument defines the model structure: in this case, 1 denominator parameter, 1 numerator parameter, 3 samples time delay and no model required for the noise. Refer to the function help information for a full description of the TF modelling tools and the syntax required. In particular, note that MISO and continuous-time models are also possible, while additional functions allow for the identification of the most appropriate model structure.

The first output argument, **th**, is a matrix containing information about the TF model structure, the estimated parameters and their estimated accuracy. In this case, **getpar** is utilised to extract the required parameter estimates for later control system design. Note that these parameter vectors include the leading unity of the TF denominator, and that the time delays are represented as zero valued elements in the numerator.



**Figure 3.4** Top: ventilation rate ( $\text{m}^3/\text{h}$ ) and response of the identified TF model (thick trace)  
Bottom: applied voltage to the control fan expressed as a percentage.

The second output argument, **stats**, lists nine statistical diagnostics associated with the model, including  $R_T^2 = 0.9873$ , implying that the model describes nearly 99% of the variation in the data. Finally, the modelling errors are returned as the variable **e** and are used in the code above to compare the TF response with the original data, as shown in Figure 3.4. In this graph, the baseline is returned to the series. The built-in MATLAB function **filter** may also be employed to simulate the TF response using these parameter vectors. This is useful for simulation and (if estimates of the future input variable are available) forecasting purposes.

### Example 3.4 PIP Control Design and Simulation

Consider again the ventilation system introduced by Example 3.3 and the associated TF model (3.4) or (3.5). The digital control algorithms developed below require that the model has at least one sample pure time delay and that the first element of the denominator polynomial is unity. For these reasons, the model will be defined in MATLAB as follows:

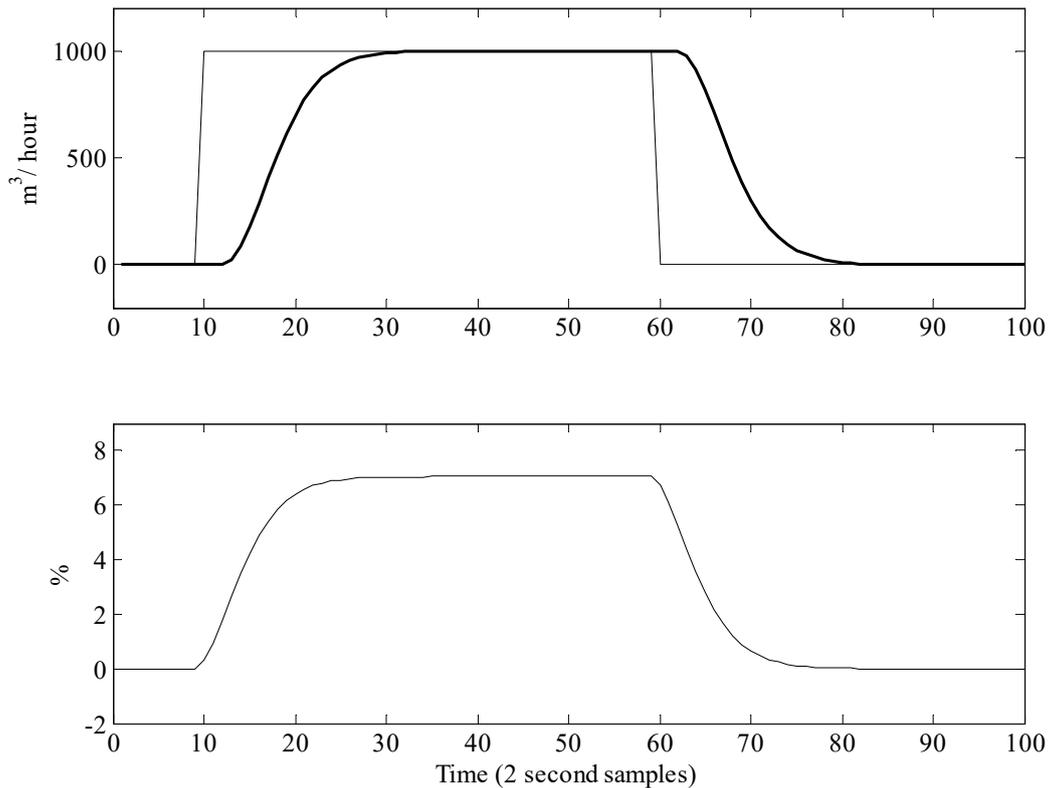
```
>> a=-0.4381          % denominator polynomial with leading unity removed
>> b=[0 0 79.7835]   % numerator with one sample time delay removed
```

Help messages for functions in the TDCONT module often refer to this ‘truncated form’ of the TF polynomials. For the present example, the NMSS model is defined by the non-minimal state vector,  $\mathbf{x}_i = [y_i \ u_{i-1} \ u_{i-2} \ z_i]^T$ , in which  $z_i$  is the *integral-of-error* between the reference or command input  $r_i$  and the sampled output i.e.  $z_i = z_{i-1} + r_i - y_i$ . The reader is directed to one of the many articles on PIP control for details of the design approach; see e.g. Taylor *et al.* (2000, 2004, 2013) and the references therein. The commands below specify closed-loop poles for the ventilation system and plot the time response. For the purpose of this example, the poles have been arbitrarily chosen within the unit circle on the complex  $z$ -plane as follows: 0.5,  $0.6 \pm 0.1i$  and 0.7.

```
>> k = pip(a, b, [0.5 0.6+0.1i 0.6-0.1i 0.7]);          % control gains
>> [acl, bcl, bclu] = pipcl(a, b, k);                  % closed-loop TF
>> r = zeros(100, 1); r(10:59) = ones(50, 1)+1000;    % command input
>> y = filter(bcl, acl, r); subplot(211); plot([y r])   % output variable
>> u = filter(bclu, acl, r); subplot(212); plot(u)      % input variable
```

The output argument of the pole assignment algorithm, **pip**, is the control gain vector. Linear quadratic design is achieved using **pipopt** instead, for which the input arguments specify weights on the integral-of-error state, input states and output states. In the code above, **pipcl** determines the closed-loop TF i.e. the relationships between  $r_i$  and the input or output variables. The MATLAB function **filter** uses these to evaluate the time response, as illustrated in Figure 3.5. To confirm that the closed-loop poles are those expected:

```
>> roots(acl)
ans =
    0.7000
    0.6000 + 0.1000i
    0.6000 - 0.1000i
    0.5000
```



**Figure 3.5** Top: ventilation rate command input and simulated closed-loop response (thick trace).  
Bottom: simulated applied voltage expressed as a percentage.

The function **pipgains** returns the control polynomials if desired:

```
>> [fpip, gpip, kpip]=pipgains(a, b, k)
fpip =
    0.00024
gpip =
    1.0000    -0.9619     0.3386
kpip =
    0.00032
```

In this case, the proportional gain  $f_0 = 0.00024$ , the denominator of the input filter  $G(L) = 1 - 0.9619L + 0.3386L^2$  and the integral gain  $k_i = 0.00032$ . This brief example omits many details, including the block diagram form of the PIP controller. The included demos in the toolbox provide MATLAB code for reproducing almost all of the examples in the book by Taylor *et al* (2013). The book provides a tutorial introduction to multivariable state space control system design with numerous worked examples, block diagrams, and guidance on the practical implementation of the control systems developed.

Note that, if the SIMULINK extension to MATLAB is installed, then it is often more convenient to use this package rather than **pipcl** and **filter** for closed-loop simulation. The library **tdclib** includes various PIP control structures. In this manner, it is straightforward to investigate the response to disturbance inputs and other practical issues. For example, if a high order, nonlinear simulation model is available, PIP control can be applied and evaluated using this model (Taylor and Shaban, 2006).

### **3.4 Concluding Remarks**

Some of the algorithms discussed here have been in constant use for over 30 years. The present authors hope that the CAPTAIN toolbox for MATLAB will allow interested researchers to add to the ever expanding list of successful applications, which already includes time series analysis, forecasting and control of numerous biological, engineering, environmental and socio-economic processes.

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