

The Dangerous Shadow of Uncertainty

Research Topic I Talks

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Motivation

As humans, we constantly grapple with the dichotomy of **beliefs** and **uncertainty** in the process of decision-making: a canceled meeting, an earthquake, a rainy day.

In particular, a significant part of our lives is governed by money. There is uncertainty of how money and economy behave across the world. Crashes in economy disrupt lives...

Therefore, It is natural to try to anticipate **bad scenarios** and relieve their consequences.

How to quantify the uncertainty?

The STOR-i: The 2008 Great Recession

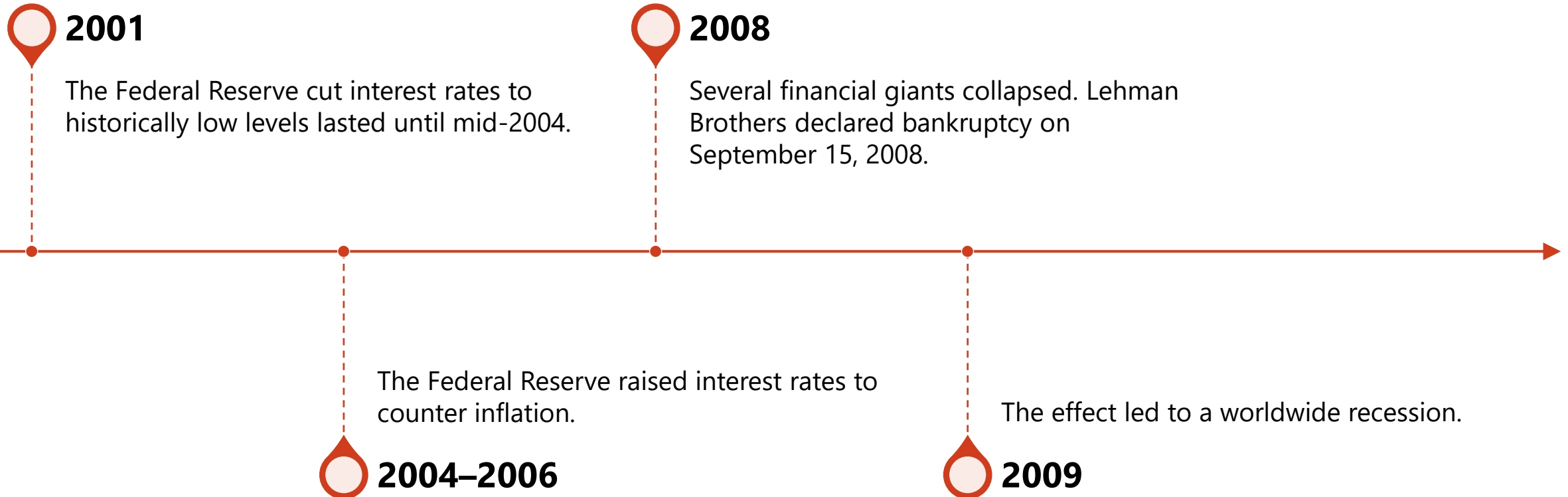
To understand the importance of quantify the uncertainty or **risk** in a phenomena we exemplify how do not do that could cause catastrophic consequences.

We focus on an example on finance sector where this problem raises naturally: **The 2008 Great Recession.**

What were the main causes of this financial crisis?

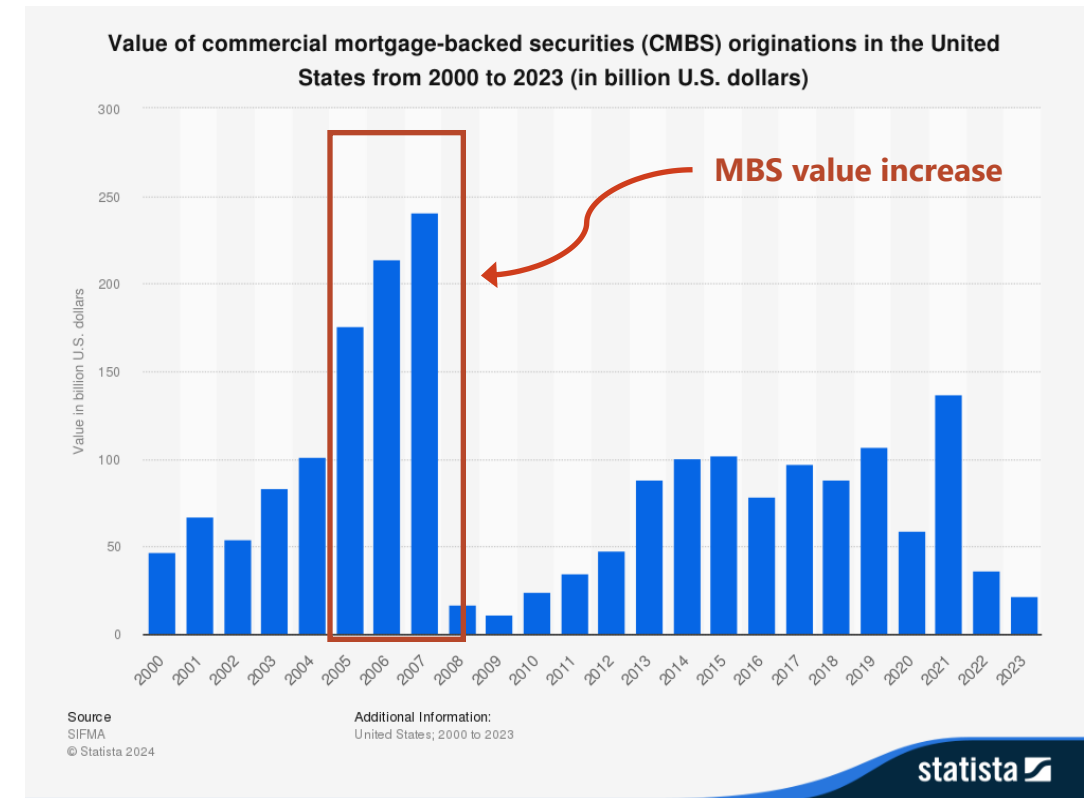


Timeline of the crisis



Causes

- Low interest rates and government politics let to a dramatic expansion of mortgage debt.
- Financial institutions aggressively bought, sold and securitized mortgages through an instrument called **Mortgage-Backed Securities (MBS)**.
- Underestimation of the risk.
- Lack of **diversification** by the financial institutions.
- Change of the conditions in 2004-2006 lead to **massive decrease** of the MBS price.



Overview of Risk Theory

Mathematically, the way to understand the **risk** is by assessing the volatility. In Probability and Statistics, we do through the **variance**.

In finance, this idea was introduced by Harry Markowitz in 1952.

However, using variance could be too conservative. This motivates the development of more refined **risk measures**.



Risk Measures

Let Z the random variable that represents the loss of the **log-returns** and F_Z its distribution

Downside Risk Measures

- Semi Variance

$$\text{SemiVar}(Z) = \mathbb{E}\left[|Z - \mathbb{E}[Z]|_+^2\right]$$

- Mean Regret

$$\text{MeanRegret}_\tau(Z) = \mathbb{E}\left[|Z - \tau|_+\right]$$

Tail Risk Measures

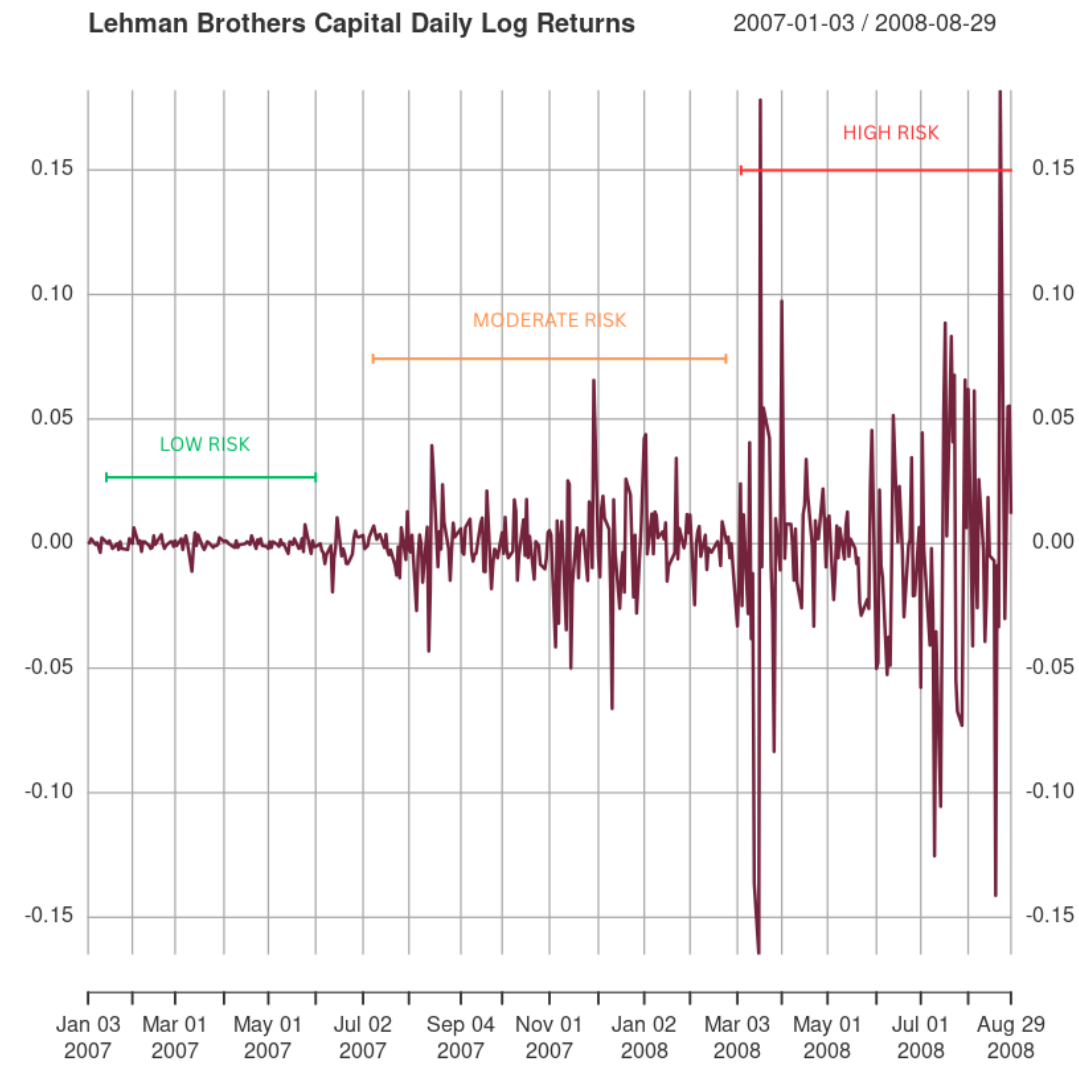
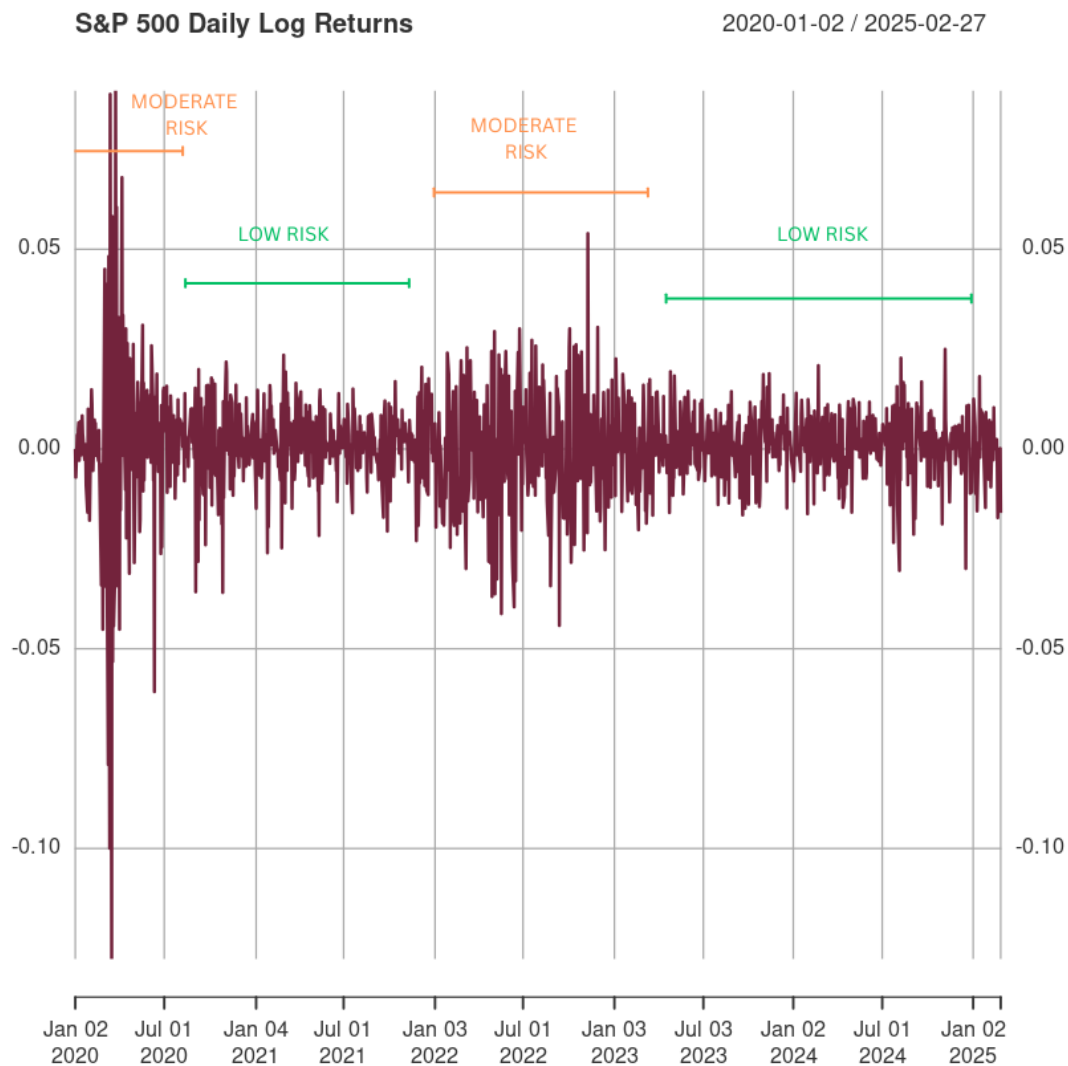
- Value-at-Risk (VaR) (J.P. Morgan, 1996)

$$\beta\text{-VaR}(Z) = F_Z^{-1}(\beta)$$

- Conditional Value-at-Risk (CVaR)
(Rockafellar et al., 2000)

$$\beta\text{-CVaR}(Z) = \mathbb{E}[Z | Z \geq \beta\text{-VaR}]$$

Analysis



Risk Measures Results

	S&P 500	Lehman Brothers
Volatility	0.01337	0.02833
VaR	-0.01867	-0.03855
CVaR	-0.03264	-0.07294
Mean Regret	-0.00900	-0.01506
Semi Var	0.00021	0.00080

- Each risk measure has a different interpretation.
- There is more or less difference between the two stocks depending on the risk measure used.
- In particular, the CVaR captures better the distance in risk between the two markets.

"La Morajela"

- Risk measures serve as thermometers to anticipating a crash.
- The choice depends on the specific situation at hand.
- These are tools for decision-making as alarms to investigate the underlying causes.

Risk measures are the light to banish the shadow of uncertainty

References

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