

# Electronic transport through single molecules

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# Outline

- Motivation
- Experimental setups
- Physical Picture: strong vs. weak coupling
- Strong coupling (brief)
- Weak coupling: methodology
- Tunneling transport through benzene
- Conclusions

# Molecular electronics

## Attractive features

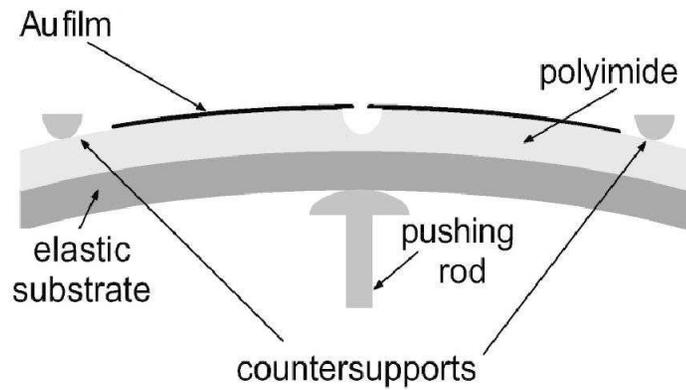
- Large energy scale (meV  $\Rightarrow$  eV)
- Chemically designable geometric/electronic structure
- “Moving parts” / Conformational changes
- Biological assembly possible?
- “Size does matter”

## Difficulties

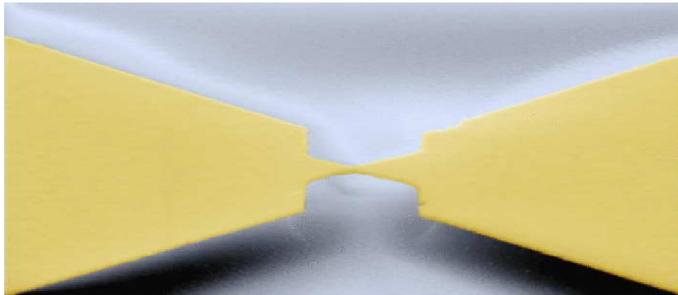
- Contacting a single molecule
- Stability
- Interface properties largely unknown (contacts)
- Gating ?

# Experimental Setups

## Controllable break junction

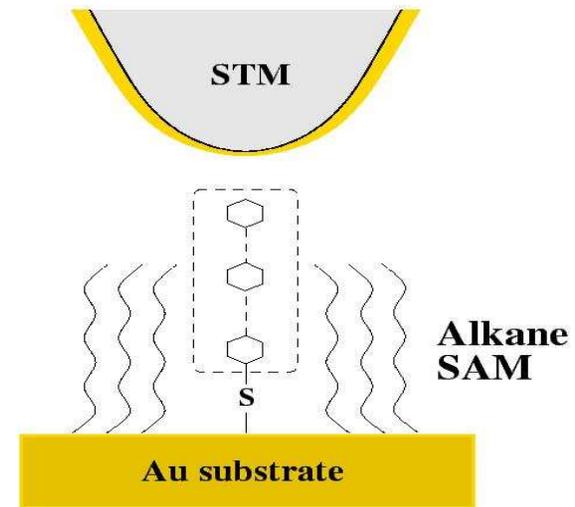


### Top view



*Courtesy of H. Weber, INT*

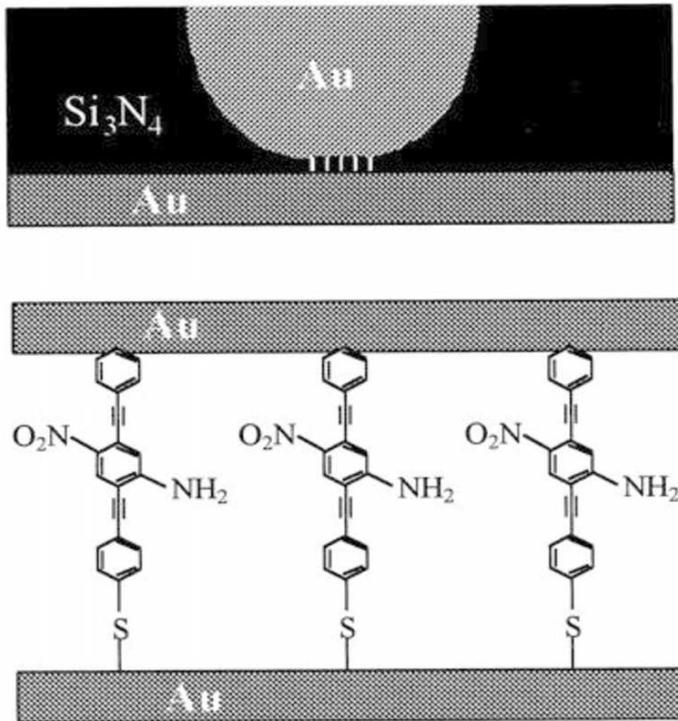
## STM over molecular layer



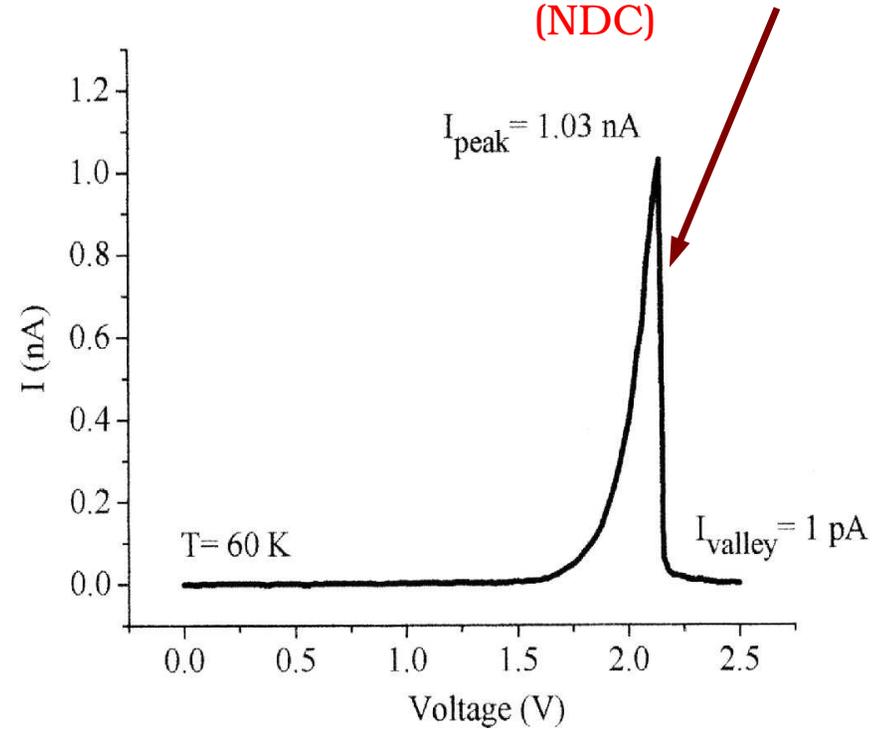
Bumm et al., Science **271** (1996)

# Nanopore Experiments

Chen, Reed, Rawlett and Tour, Science **286** (1999)



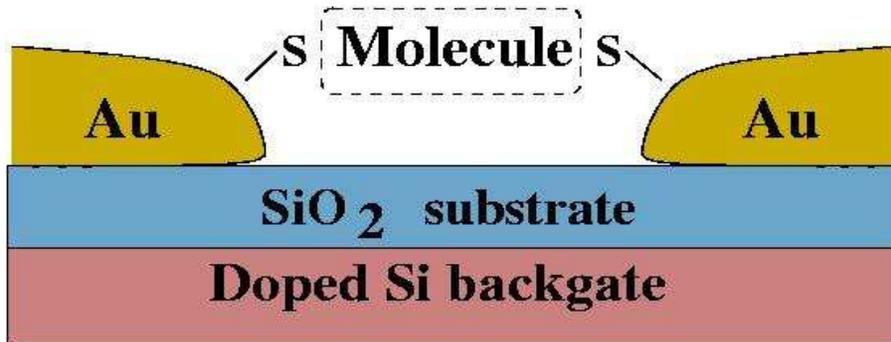
Negative differential conductance  
(NDC)



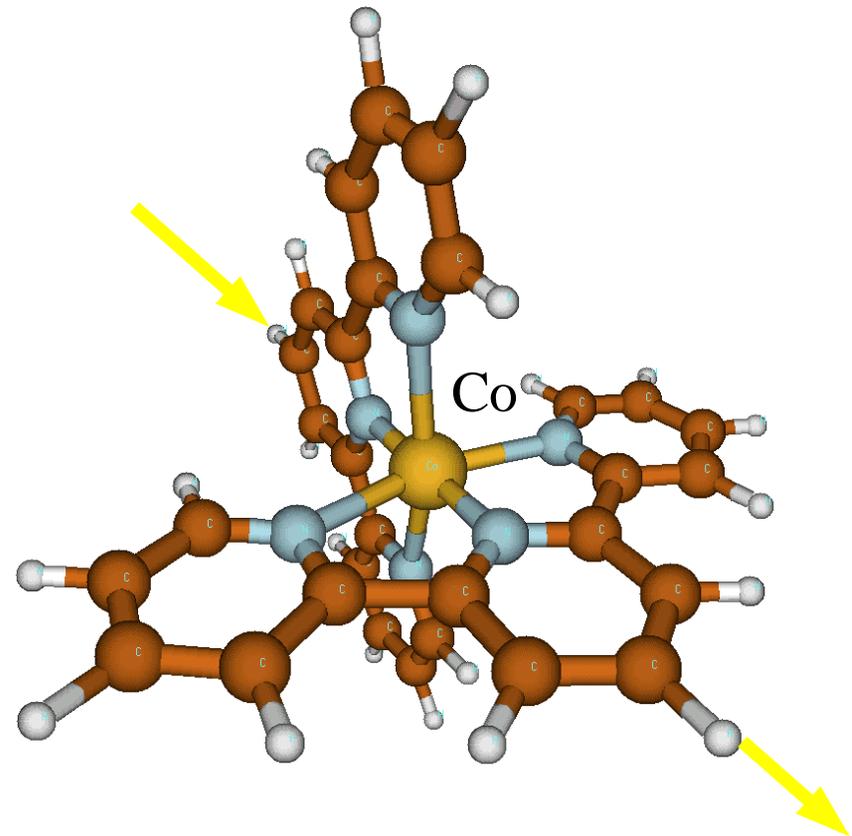
Peak current **per molecule** of order  $10^{-13}$  A !

# Planar electrodes

e.g. J. Park, A.N. Pasupathy et al., Nature **417** (2002)



"Transition metal holder"  
*2,2':6',2''-terpyridine*



symmetry restricts  
coupling

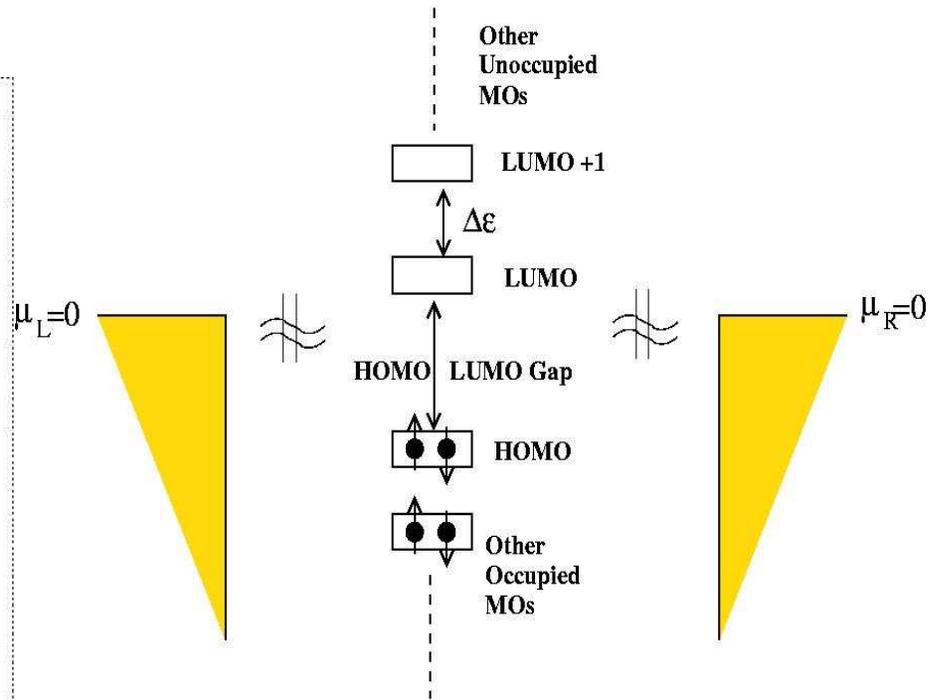
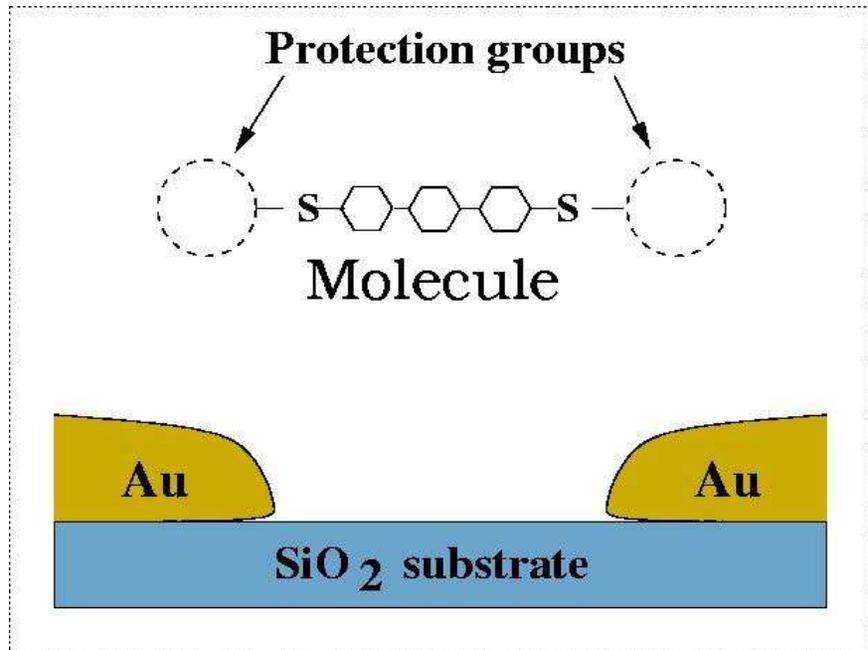
buffer *L* → Buffer *R*

*d*-like  
Co states

Strong Coulomb  
correlations

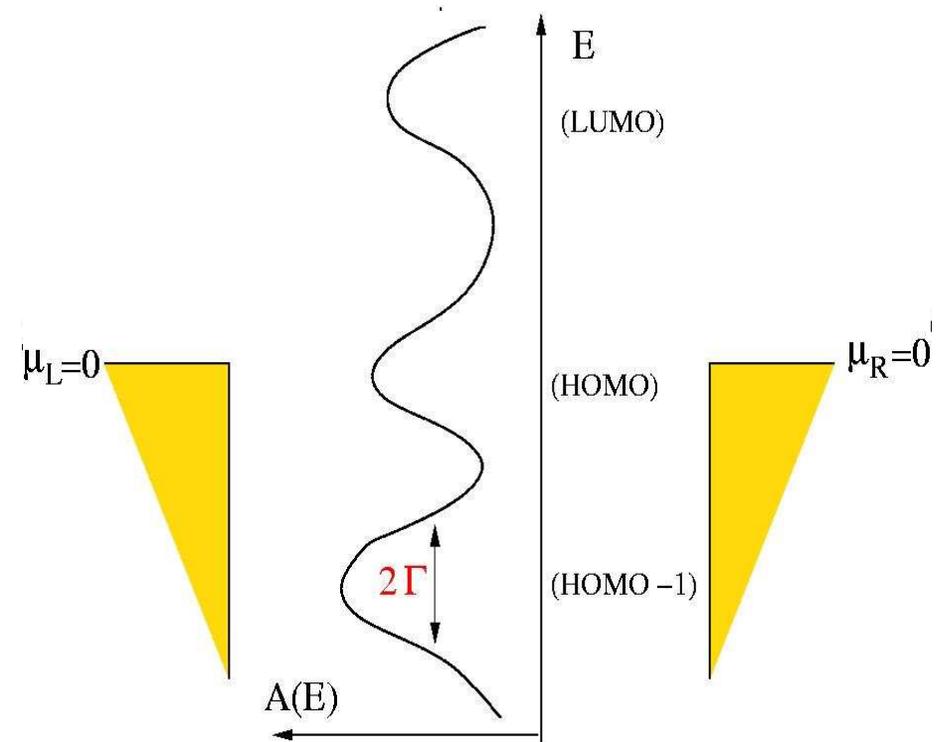
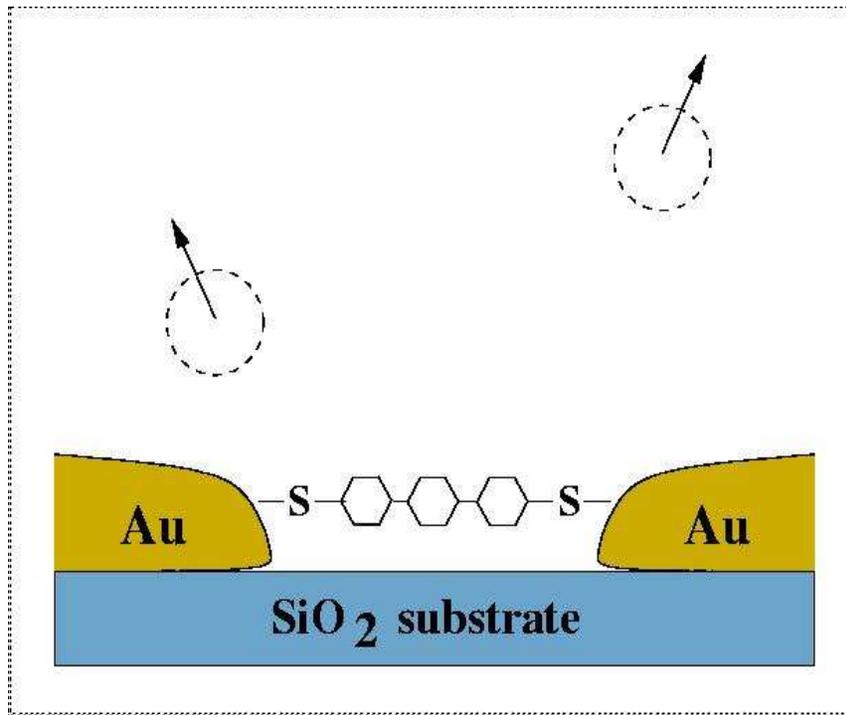
# Physical Picture: Separate components

MO: Molecular Orbital

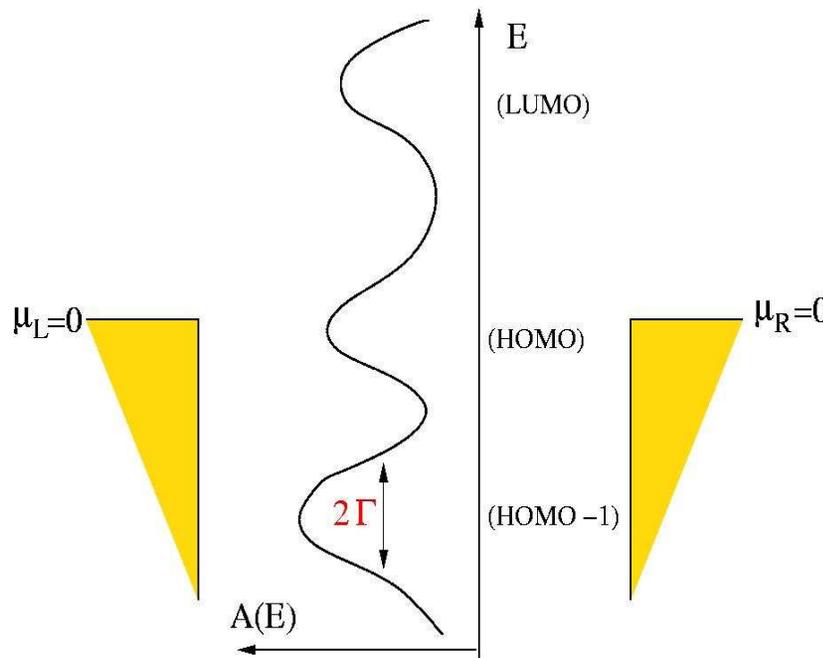


# Physical picture: Strong molecule-electrode coupling (1)

$\Gamma$ : Molecule-electrode coupling



## Physical picture: Strong molecule-electrode coupling (2)



- Molecular Orbitals severely broadened on order of **coupling energy**
- Electrons stay short time on molecule
- Only static e-e interactions important  $\Rightarrow$  **single particle description suffices**
- If  $\Gamma \sim$  charging energy  $\Rightarrow$  Transport via **coherent scattering states**

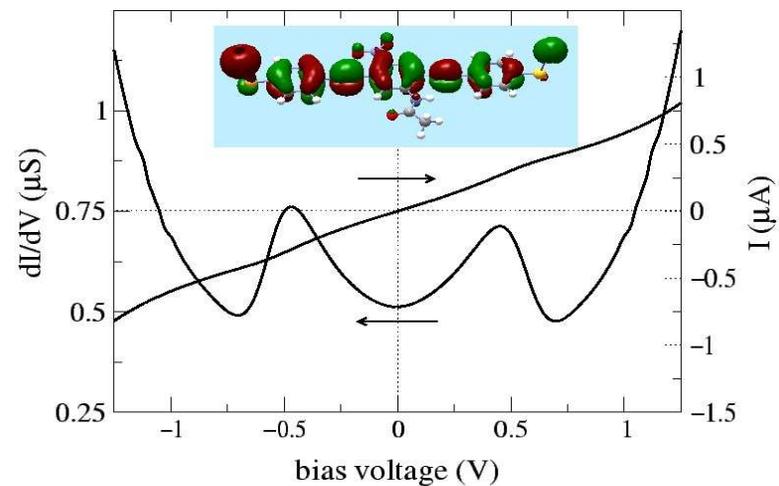
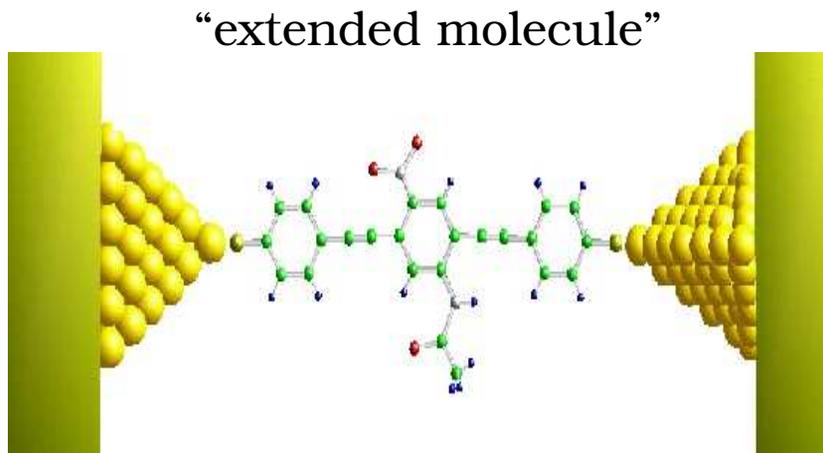
Landauer Approach:  $I(V) = 2e/h \int dE T(E, V) [f(E - \mu_L) - f(E - \mu_R)]$

$F(E)$ : Fermi function       $T(E, V)$ : Transmission function,  $eV = \mu_L - \mu_R$

# Strong coupling methodology

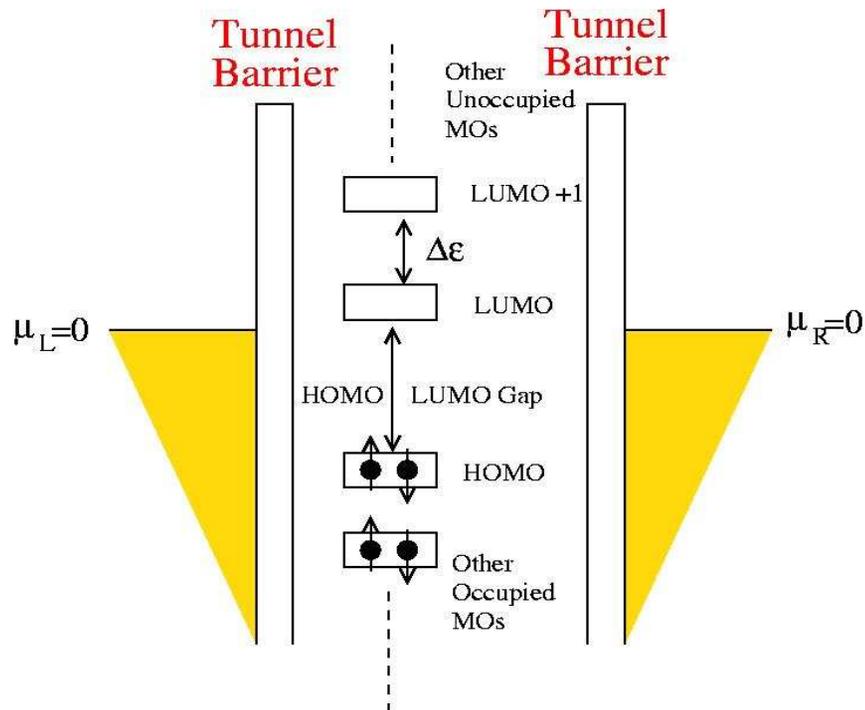
- Density Functional Theory (DFT) treatment of “extended molecule”
- Couple the resulting Kohn-Sham eigenstates to bulk electrodes
- “Diagonalize”, compute electron density on molecule, and iterate

Many groups, many variations in many aspects of theory



Figures from Heurich, Cuevas, Wenzel and Schön, PRL **88** (2002)

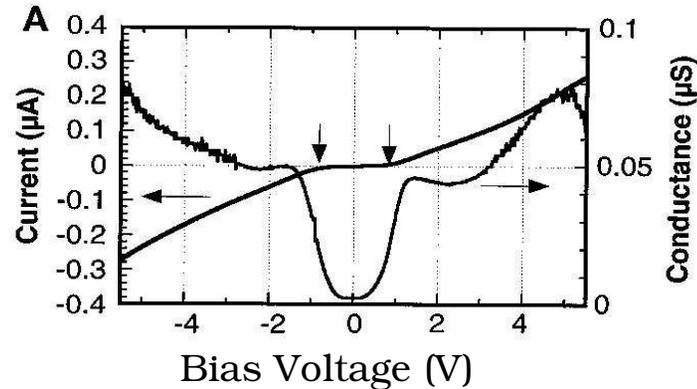
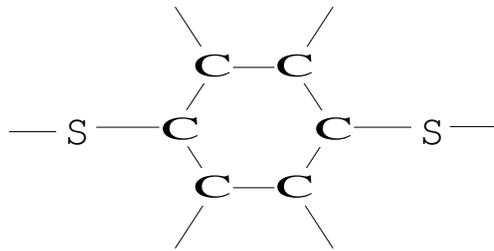
# Physical picture: Weak molecule-electrode coupling



- Molecular Orbitals stay **sharp**
- Electrons stay long time on molecule
- Dynamic e-e interactions important  
⇒ **many-body description necessary**
- If  $\Gamma < \text{temperature}$ ,  $\Gamma \ll \text{charging energy}$   
⇒ Transport via **sequential tunneling**

# Benzene-(1,4)-dithiolate/Au system

M.A.Reed et al., Science **278** (1997): First single molecule experiment?



Small current?

## Theory

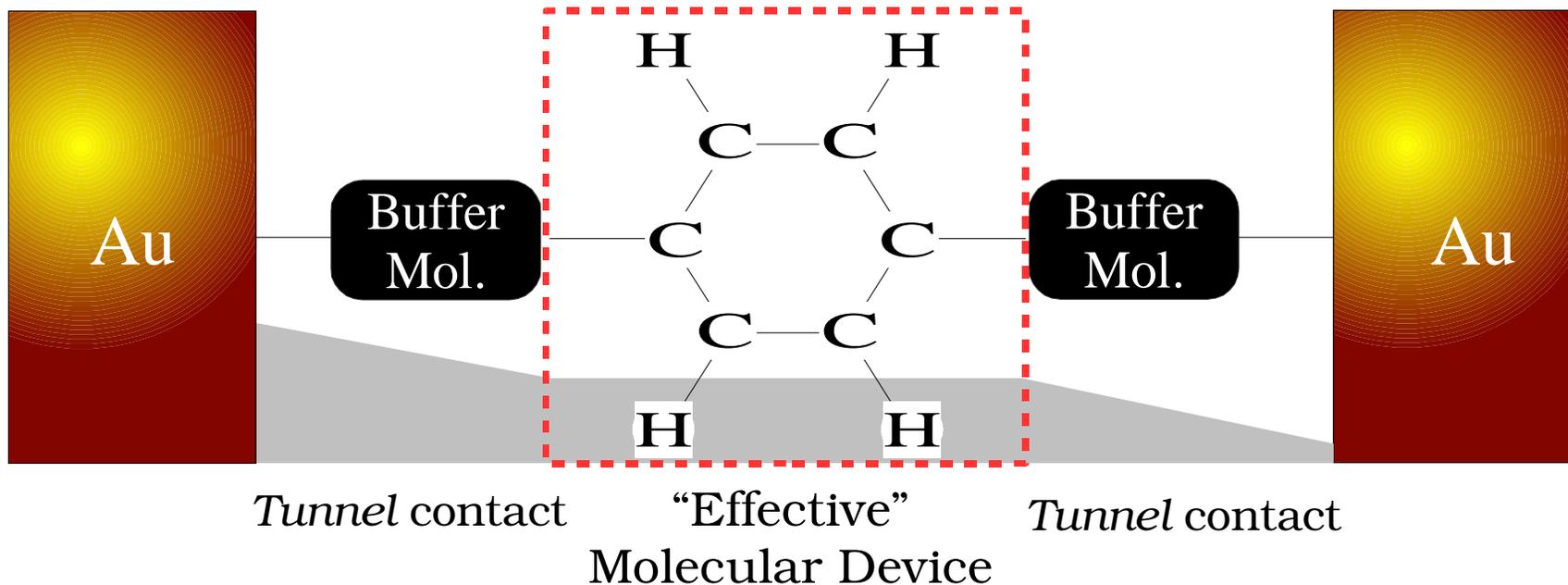
M. DiVentra, S.T. Pantelides, N.D. Lang, PRL **84**, 979 (2000)

P.S. Damle, A. W. Gosh, S. Datta, PRB **64**, 201403 (2001)

E. G. Emberly, G. Kirczenow, PRB **64**, 235412 (2001)

2 benzenes, each one connected to different electrode!

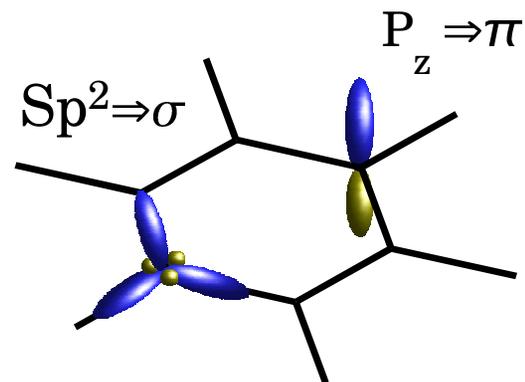
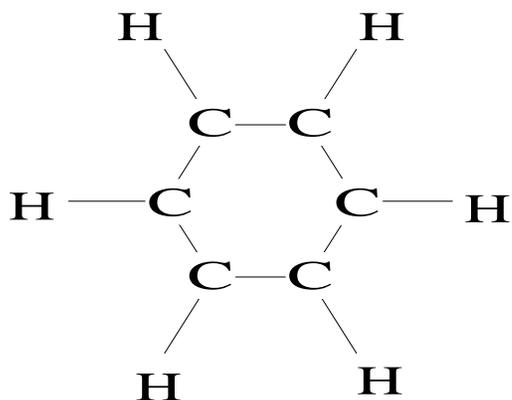
## How to weakly coupled molecules?



Sequential tunneling on/off molecule,  
transitions between *many-electron states*

Example: J. Park, A.N. Pasupathy et al., Nature **417** (2002)

# Benzene $\pi$ and $\sigma$ electron system



- *Prototype* aromatic molecule  
 $\sigma$  (C,H atoms) and  $\pi$  (C atoms) electron system
- High symmetry, good energetic separation of  $\sigma$  and  $\pi$  systems
- Small enough to test theoretical methods

## Electronic structure $\Rightarrow$ Interacting Model

$$H_{\text{mol. } \pi} = \sum_{ij \sigma} \epsilon_{ij} c_{i \sigma}^\dagger c_{j \sigma} + \sum_{ijkl \sigma \sigma'} U_{ijkl} c_{i \sigma}^\dagger c_{j \sigma'}^\dagger c_{k \sigma'} c_{l \sigma}$$

Create orthogonalized Wannier-states  $\Phi_i$   
localized at C-atom  $i = 1, \dots, 6$  on the ring

- Effective *interacting* Hamiltonian for  $\pi$  electrons  
Low energy spectrum 0-5 eV well-reproduced  
for neutral states molecule (exp. & theory)  
less accurate for the charged states (anion) (not much known)
- Wavefunction amplitudes  $\Rightarrow$  Tunneling  
Dipole moments  $\Rightarrow$  Emission and Absorption of Photons  
 $\Rightarrow$  radiative relaxation of many-body states

# Effective Hamiltonian

$$H_{\pi} = \sum_{ij\sigma} \epsilon_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} + \sum_{ijkl\sigma\sigma'} U_{ijkl} c_{i\sigma}^{\dagger} c_{j\sigma'}^{\dagger} c_{k\sigma'} c_{l\sigma}$$

$$\epsilon_{ij} = \langle \Phi_i | H_{\text{kin}} + V_{\text{nucl.}} + V_{\sigma \text{ eff.}} + V_{\text{ext}} | \Phi_j \rangle$$

Freeze “core”  $\sigma$ -electrons  
 $\Rightarrow$  effective potential  
 for remaining  $\pi$  electrons

e.g. partial drop  
 of bias potential

$$(V_{\sigma \text{ eff.}})_{il} = \sum_{jk \in \sigma} \langle ij | \frac{e^2}{|\mathbf{x} - \mathbf{x}'|} | kl \rangle$$

$$U_{ijkl} = \langle ij | \frac{e^2}{|\mathbf{x} - \mathbf{x}'|} | kl \rangle \quad \text{Full unscreened Coulomb interaction for } \pi \text{ electrons (no } \sigma\text{-} \pi \text{ polarization)}$$

## External Bias Potential

Adjustment of  $\pi$  electrons to external linear ramp potential

$$V_{ij}^{\text{ext}} = \int d^3 r \Phi_i(\mathbf{r}) V^{\text{ext}}(\mathbf{r}) \Phi_j(\mathbf{r})$$

$$H_{\text{bias}} = e \sum_{ij\sigma} V_{ij}^{\text{ext}} c_{i\sigma}^\dagger c_{j\sigma}$$

$$V^{\text{ext}}(\mathbf{r}_x) = \frac{V_L + V_R}{2} - \frac{(V_L - V_R)\mathbf{x}}{L}$$

$$V_{\text{bias}} = V_L - V_R \quad L = 0.4 \text{ nm}$$

“Worst case”: All the bias drops between the tunnel barriers

## Electron Tunneling

$$H_{\text{mol.} - \text{leads}} = \sqrt{\frac{\Gamma}{2\pi\rho_e}} \sum_{l\mathbf{k}\sigma\alpha} (c_{l\sigma}^\dagger a_{\mathbf{k}\sigma\alpha} + \text{h.c.})$$

$\rho_e, a_{\mathbf{k}\sigma\alpha}$ : Density of states and operators in electrode  $\alpha=L,R$

## Transition Rates

$$\Gamma_{s' \leftarrow s}^{\alpha+} = \Gamma f_{\alpha}(\mathbf{E}_s - \mathbf{E}_{s'}) \sum_{\sigma} \left| \sum_i t_i^{\alpha} \langle \mathbf{s} | \mathbf{c}_{i\sigma} | \mathbf{s}' \rangle \right|^2$$

$$\Gamma_{s' \leftarrow s}^{\alpha-} = \Gamma (1 - f_{\alpha}(\mathbf{E}_s - \mathbf{E}_{s'})) \sum_{\sigma} \left| \sum_i t_i^{\alpha} \langle \mathbf{s} | \mathbf{c}_{i\sigma} | \mathbf{s}' \rangle \right|^2$$

$$\Gamma_{s' \rightarrow s}^d = \frac{4e^2}{3\hbar^3 c^3} (\mathbf{E}_s - \mathbf{E}_{s'})^3 N(\mathbf{E}_s - \mathbf{E}_{s'}) |\langle \mathbf{s} | \mathbf{d} | \mathbf{s}' \rangle|^2$$

s,s': many-particle states, determined by effective Hamiltonian

$$\mathbf{d}_{ij} = \int d^3r \Phi_i(\mathbf{r}) e \mathbf{r} \Phi_j(\mathbf{r}) \quad \Phi_i : \text{single-particle states}$$

$$N(\mathbf{E}) = \frac{1}{e^{\beta \mathbf{E}} - 1}$$

$$N(-|\mathbf{E}|) = -(1 + N(|\mathbf{E}|))$$

higher energies => relaxation mostly (photons)

lower energies => relaxation + excitation (phonons)

# Stationary master equation

$$\frac{\partial P_s}{\partial t} = \sum_{s'} (\Gamma_{s \leftarrow s'} P_{s'} - \Gamma_{s' \leftarrow s} P_s) \equiv 0$$

Rates determine  
non-equilibrium  
occupations P

dipole transitions  
affect occupations,  
*thereby* the current

**Rates**

$$\Gamma_{s \leftarrow s'} = \sum_{\alpha = LR} \sum_{p = \pm} \Gamma_{s \leftarrow s'}^{\alpha p} + \Gamma_{s \leftarrow s'}^d$$

tunneling  
in/out (+/-), lead  $\alpha = L, R$   
*directly* enters into current

**Current**

$$I_\alpha = e \sum_{ss'} (\Gamma_{s \rightarrow s'}^{\alpha +} P_{s'} - \Gamma_{s' \rightarrow s}^{\alpha -} P_s)$$

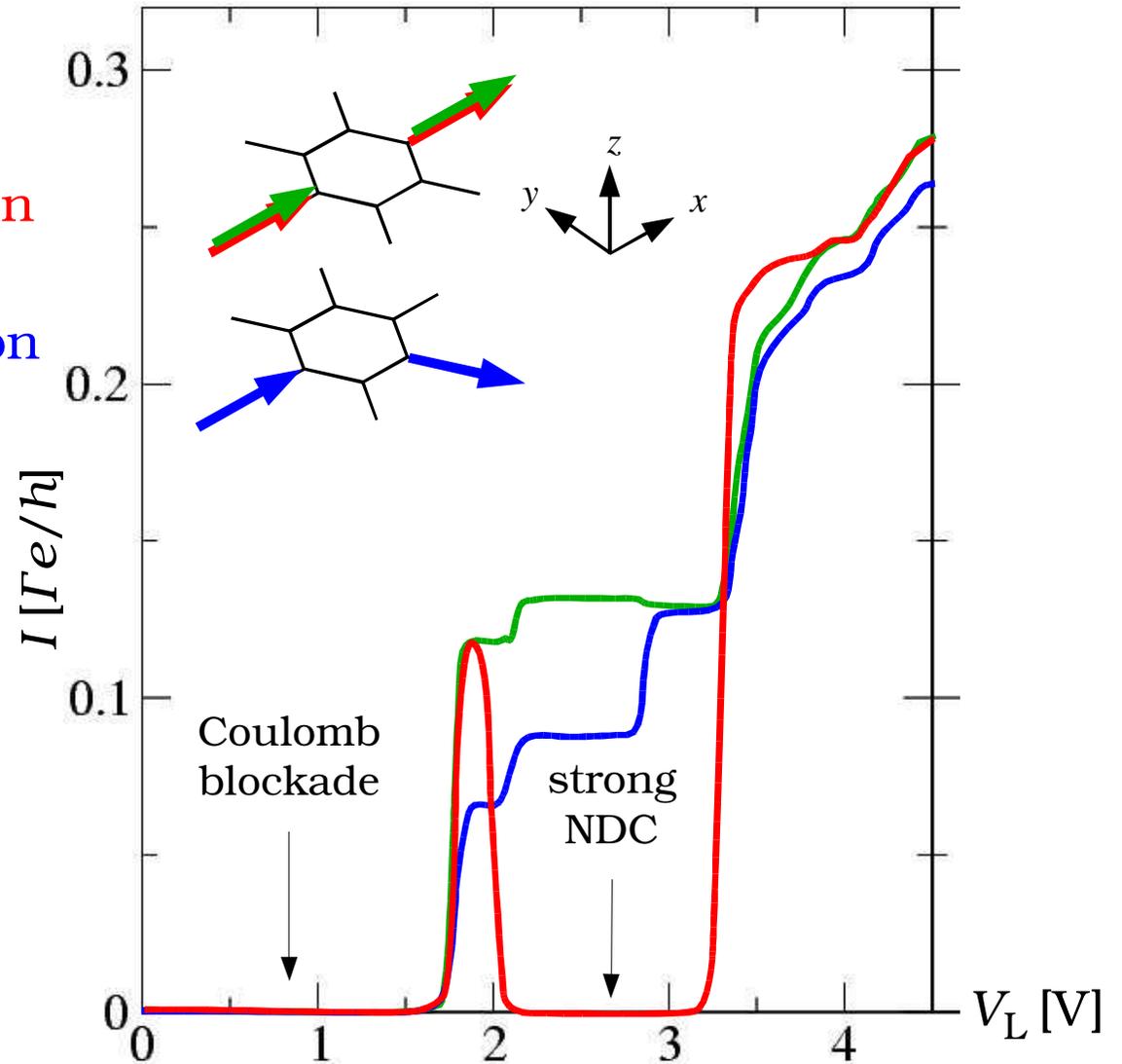
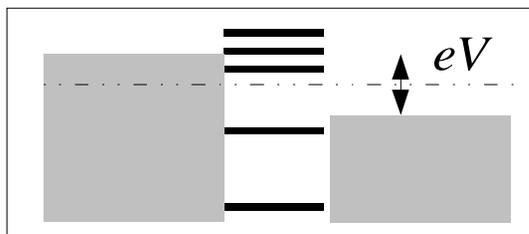
$$\Gamma_d \ll \Gamma^{\alpha p} = 10^{-4} \text{ eV} \ll kT (2.5 \cdot 10^{-2} \text{ eV @ RT})$$

# Current vs. Bias Voltage

para-position

para-position + relaxation

meta position + relaxation



# NDC: simplest case

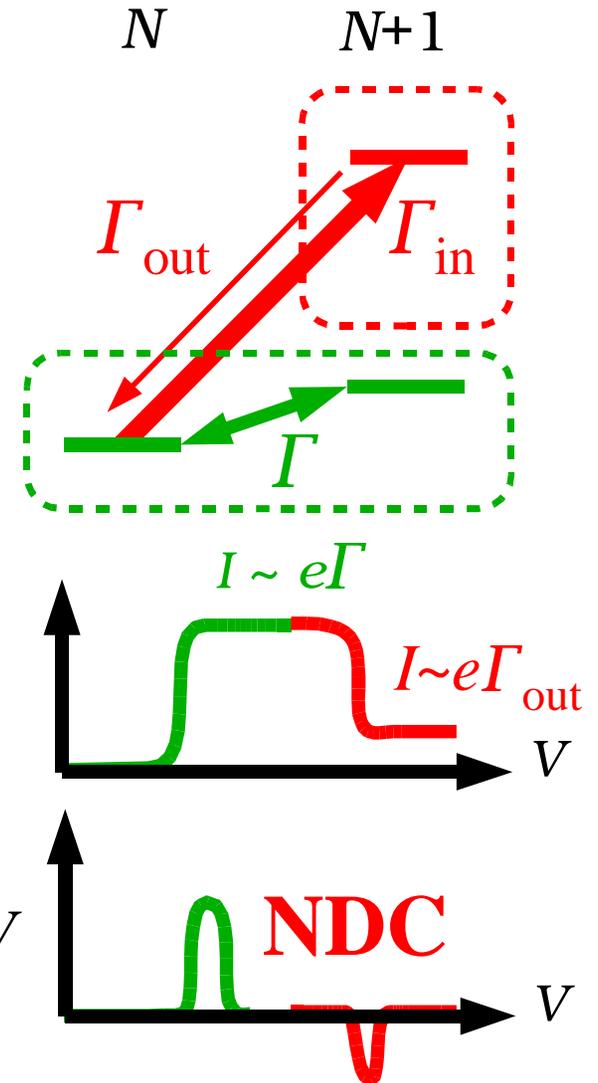
Hettler, Schoeller and Wenzel, EPL **57** (2002)

**Blocking state:**  $\Gamma_{\text{in}} \gg \Gamma_{\text{out}}$

populated fast – decays slowly

- occupation probability  $\approx 1$   
“occupied most of the time”  
(compare: population inversion)
- **slow process dominates current**

NDC occurs when a transition to a blocking state becomes energetically allowed



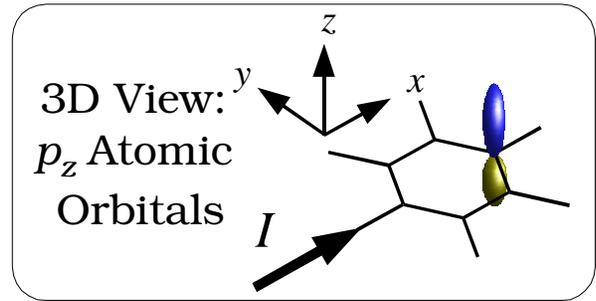
NDC with  $\pi$  electrons in benzene?

Molecular orbitals

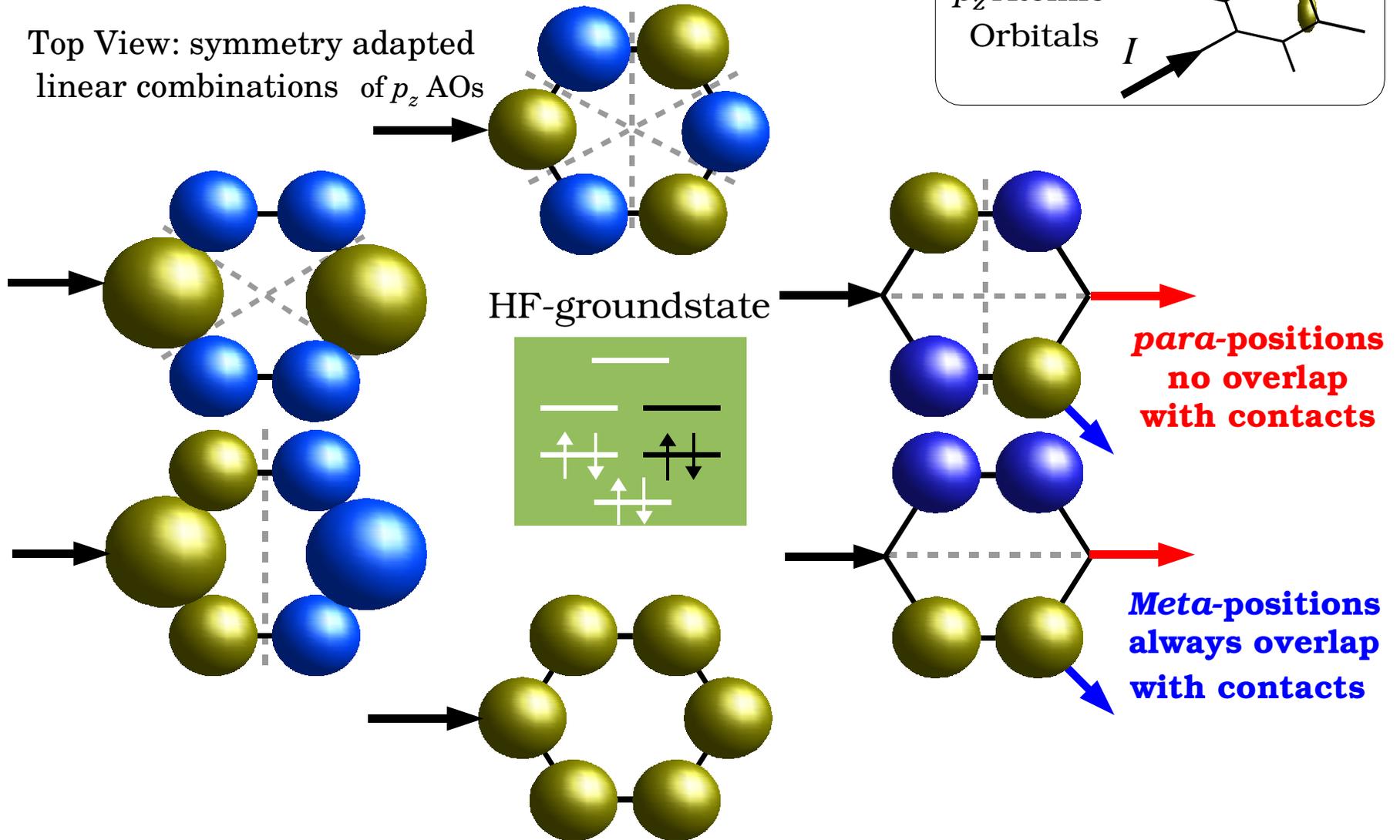


Many-electron states

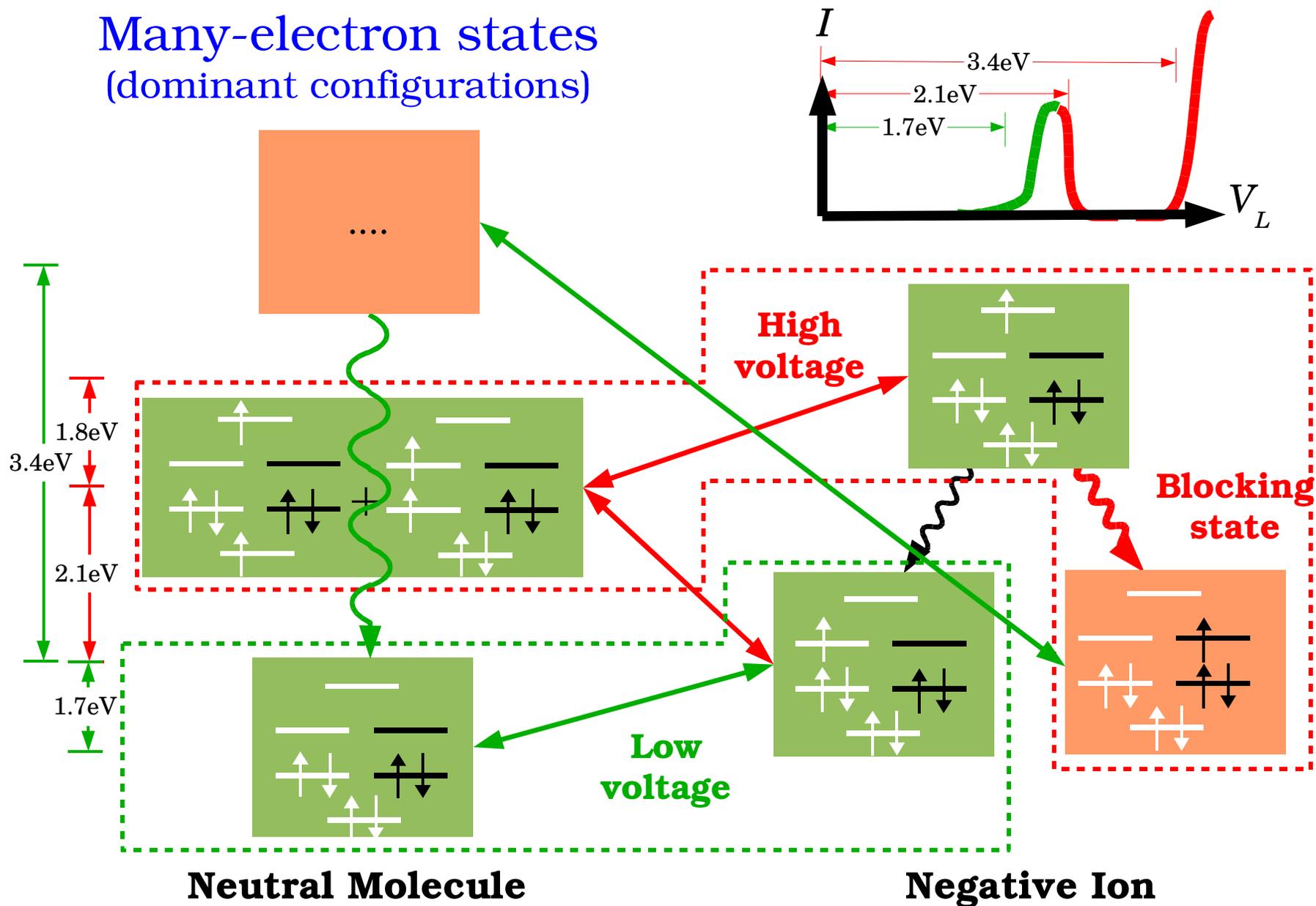
# Single-particle states Molecular $\pi$ -orbitals



Top View: symmetry adapted  
linear combinations of  $p_z$  AOs



# Many-electron states (dominant configurations)



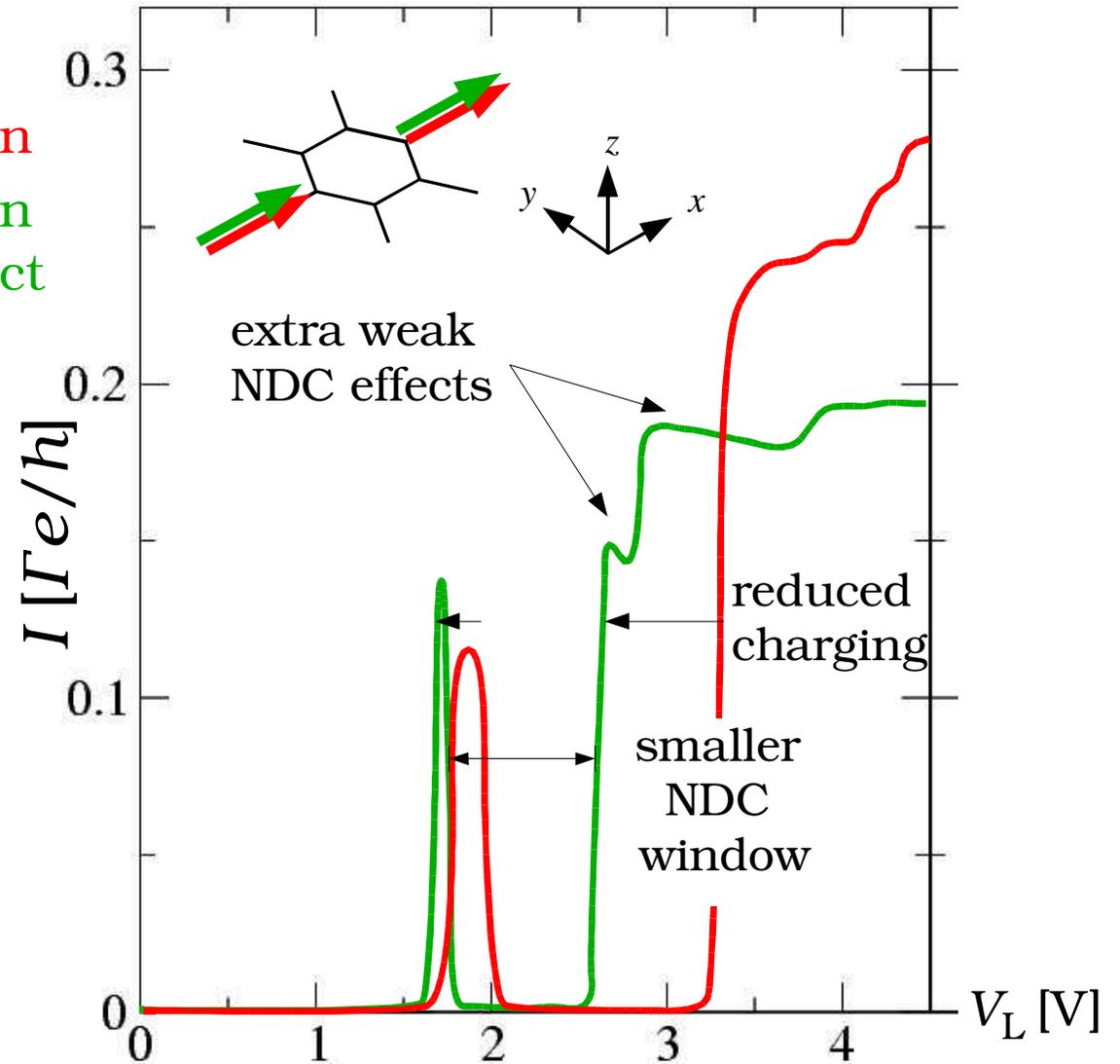
# Robustness

- Tunneling in and out of  $\sigma$ -orbitals?  
channel “in series” : *slowest process dominates*
- Slow rotations about  $\sigma$ -bonds to the buffer groups?  
 $\pi$  orbitals not involved in bonding  $\Rightarrow$  rotation possible
- Redistribution of  $\pi$  electrons to due to bias potential?  
smaller but sizable NDC voltage window

# Response to the external bias

para-position + relaxation  
para-position + relaxation  
+ bias effect

“Worst case”  
bias effect



# “Message”

In *weakly* coupled molecules

- e-e interactions
- Relaxation
- symmetry (side groups)

can lead to the occurrence of **blocking states**.

## Possible spoilers : (

- **Molecule not orthogonal to electrode**  
**Electric field not // to transport axis**  
Mixing of  $y$ -symmetric and  $y$ -antisymmetric states  
*Will have at least quantitative effect*
- **Low-lying anionic Rydberg states**  
Extra electron occupies a *diffuse  $\sigma$  orbital* ?  
Spontaneous relaxation to lower Rydberg many-particle state ?  
*Manipulate with symmetric side groups*
- **Vibrations**  
Could provide processes to help escape blocking state
- **Adiabatic change of nuclear lattice in blocked state**  
*Slower than electron motion*

# Conclusions

- Molecular Electronics – Approach
- Strong vs. weak coupling picture
- Weakly coupled benzene - Effective  $\pi$  electron model
- Current-Voltage Characteristics
- Blocking state and spatial symmetry
- Spoilers/Loopholes

Thanks to the organizers and a great audience!

LONG

# Hartree-Fock + Frozen core

augmented double-zeta atomic natural orbitals (ANO)  
truncated beyond 2p shell

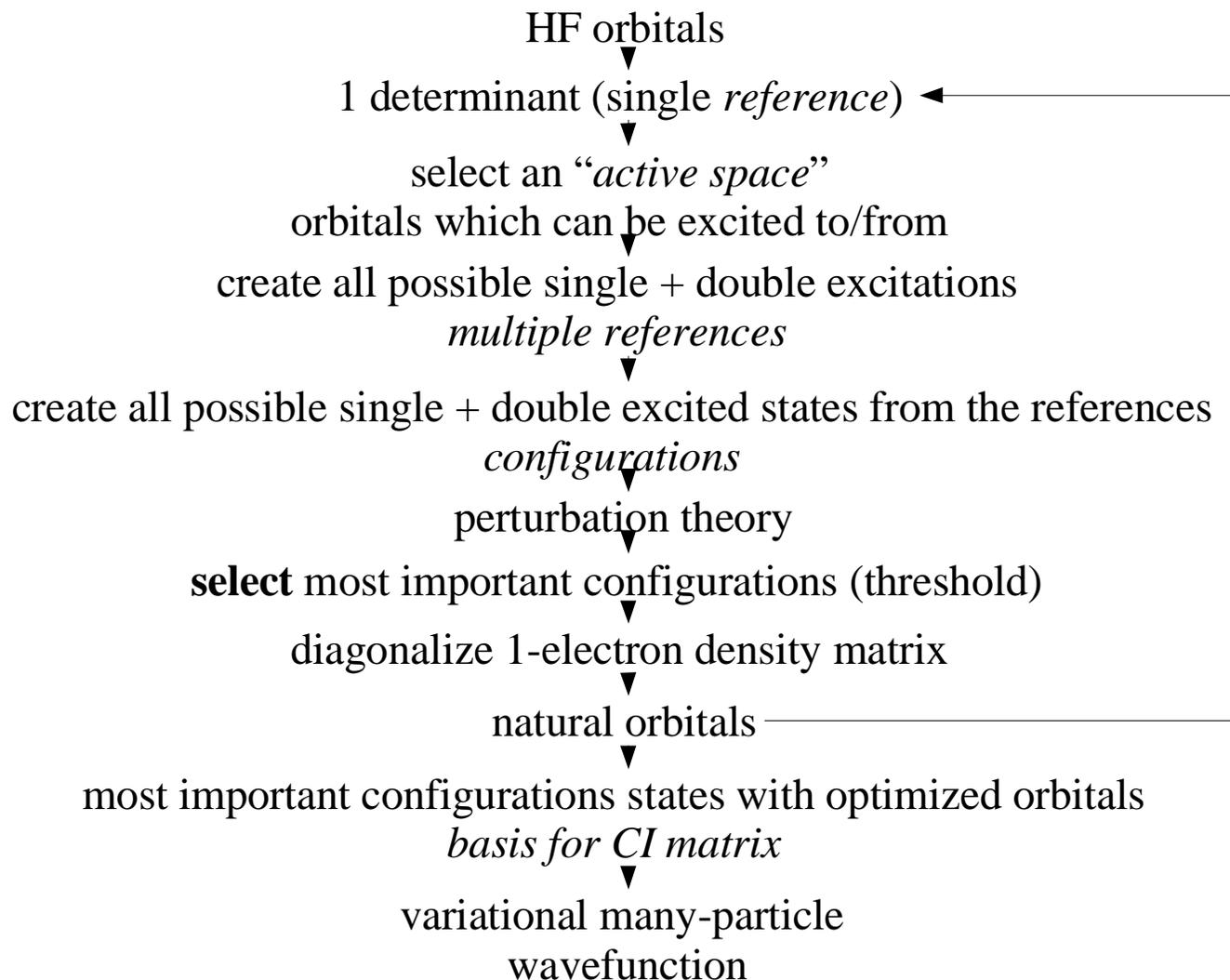
$\sigma$ - $\pi$  e-e interaction  $\Rightarrow$  effective potential for  $\pi$  electrons

“freeze”/integrate out  $\sigma$  states

Excitation spectrum up to 5 eV well described by *interacting*  $\pi$  electron model

# State Selecting MRD-CI Method

(Multi-Reference Double-excitation Configuration-Interaction)



# EXTRA Comparison of many-particle “ $\pi$ states”

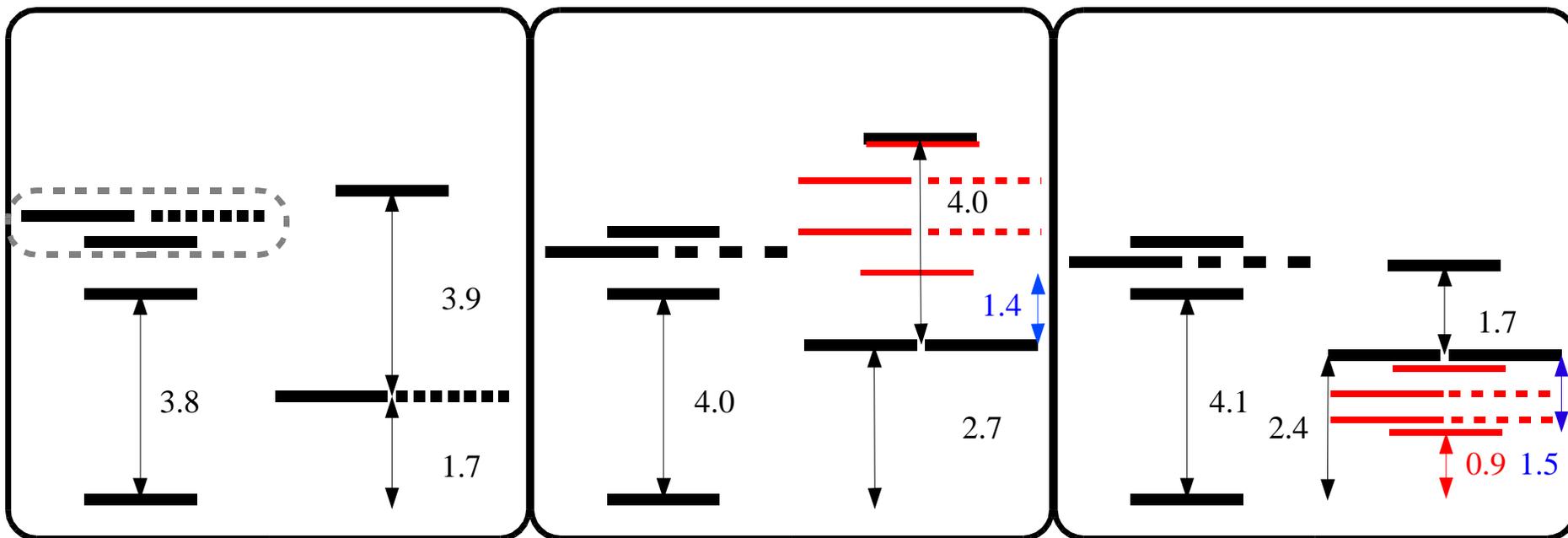
Molecule    2<sup>nd</sup> Triplet 1<sup>st</sup> Singlet opposite order  
Electron Affinity to small

Anion        1<sup>st</sup> Excitation to big

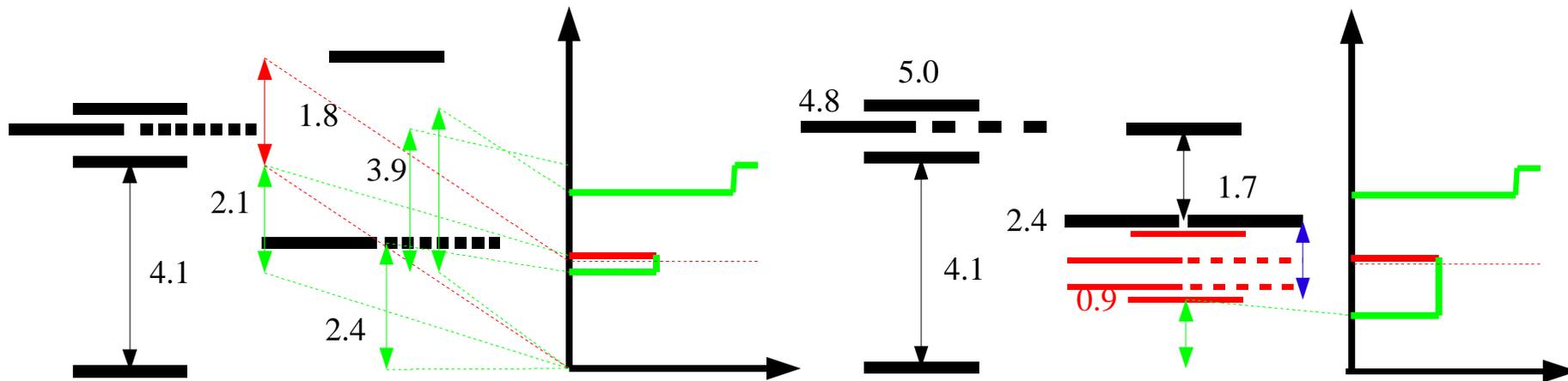
Effective  $\pi$  model

MRD-CI /cc-pVDZ  
(without diffuse functions)

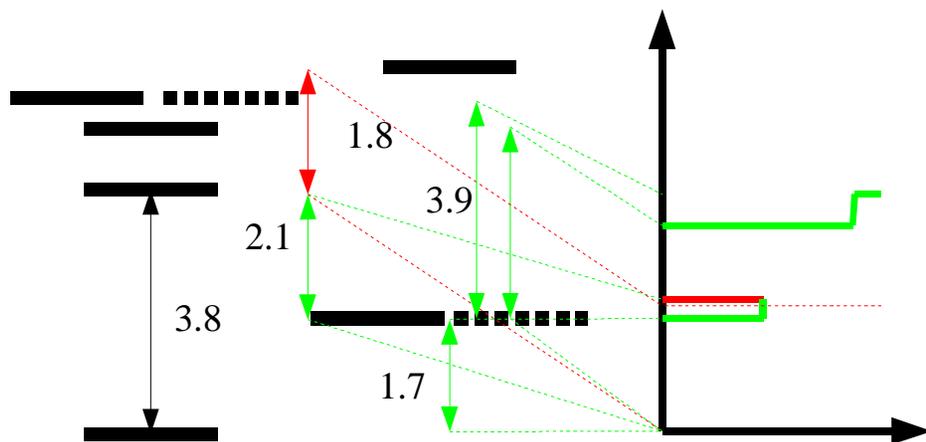
MRD-CI /aug-cc-pVDZ  
(with diffuse functions)



# EXTRA I-V scenarios



1.5



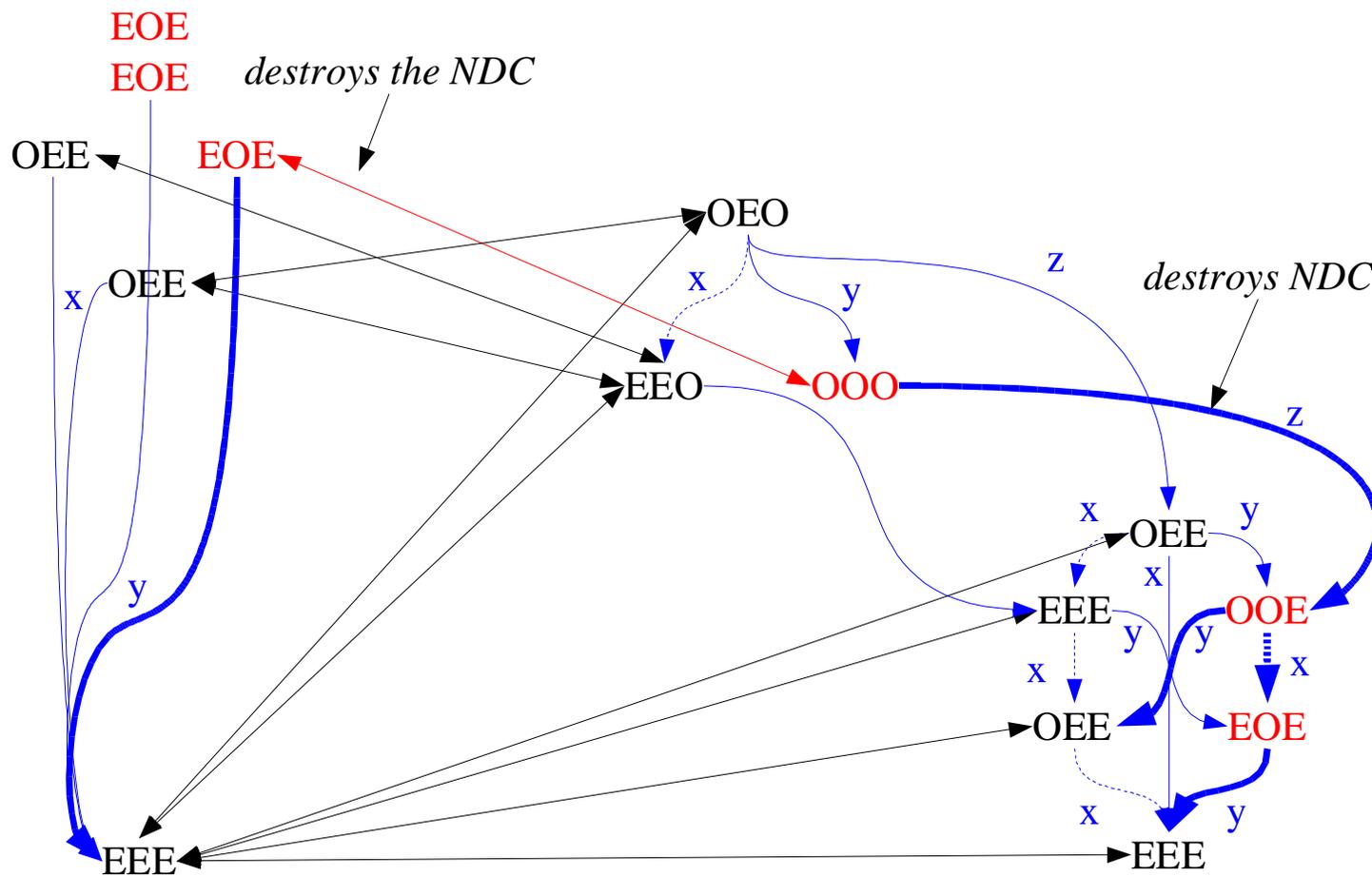
- $y$  1 photon transition
- $x$  dipole perpendicular to transport  $x$ -axis
- 1 photon transition
- dipole parallel to transport  $x$ -axis

# EXTRA States

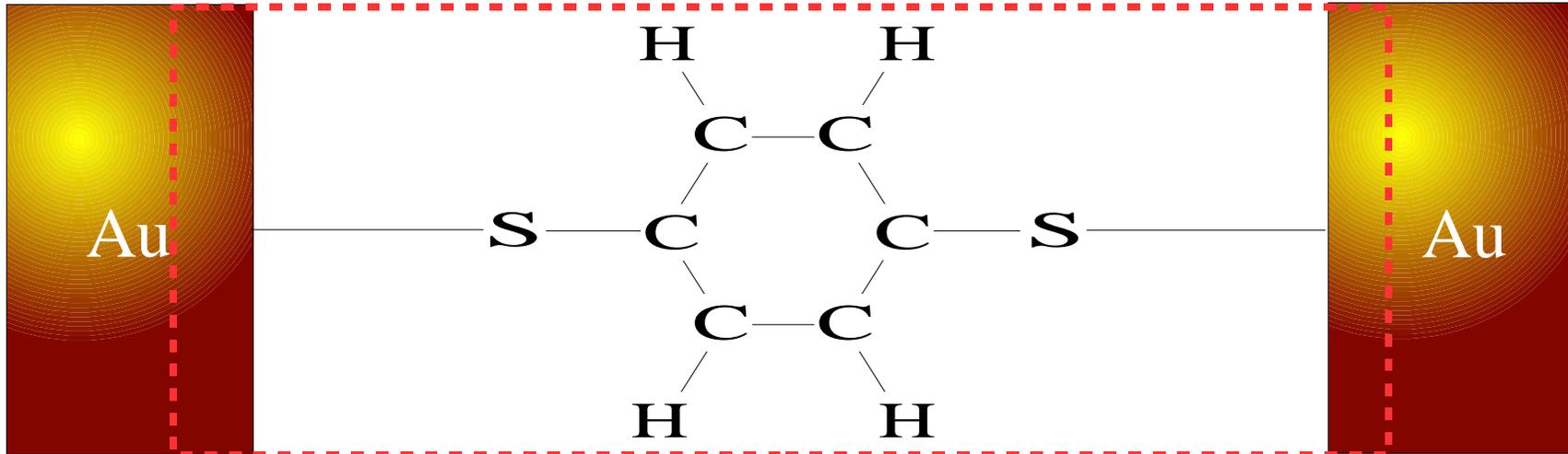
- EOE anti-symmetric w.r.t.  $x$ - $z$  plane refl.
- OEE symmetric w.r.t.  $x$ - $z$  plane refl.

## Molecule Many Particle States

## Anion Many Particle States



## Strongly coupled benzene



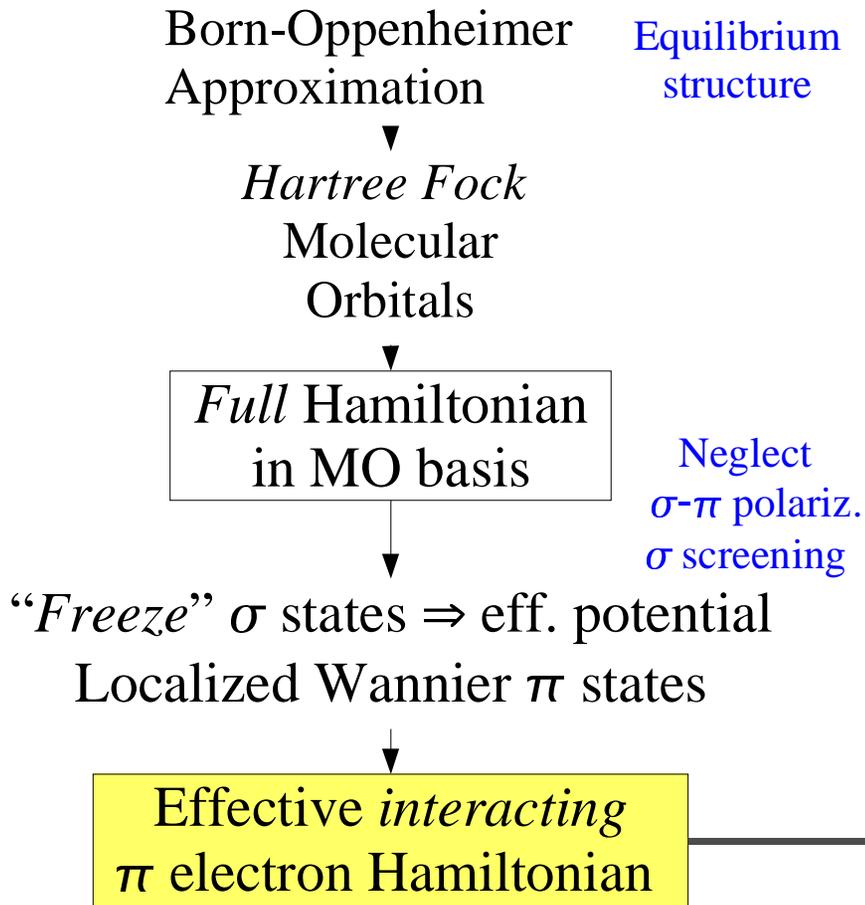
Effective “extended” molecule

- Orbitals extended over device + electrodes
- Interface effects are dominant

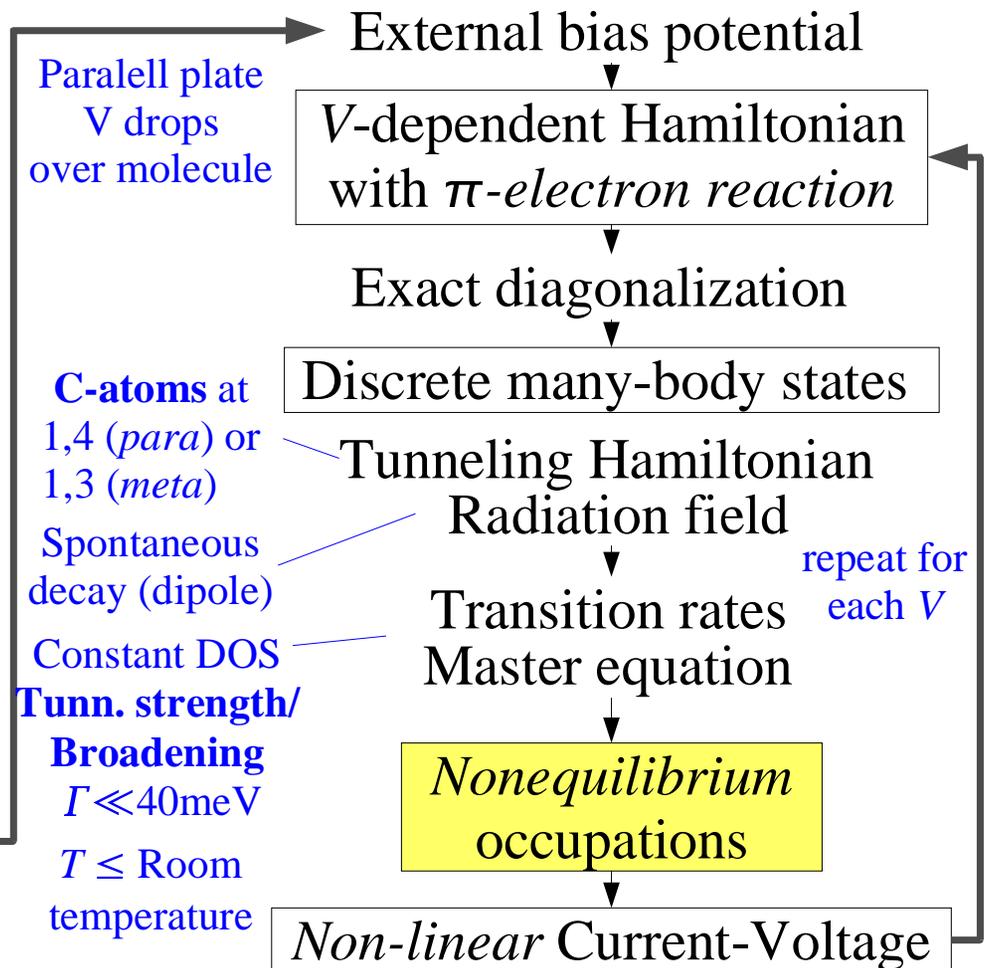
Transmission through *coherent channels* (Landauer Approach)

# Method & Assumptions

## Electronic structure



## Quantum transport



# Recovery of transport

