# Reproduction of Forecasting Methods in the M Competitions

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# Agenda

- Motivation
- Scope of this Project
- Accuracy Measures (Naive 1)
- Deseasonalisation (Naïve 2)
- Method Specifications
  - Simple Moving Averages
  - Single Exponential Smoothing
- Discussion and Further Work



### **Motivation**

Instead of imagining that our main task is to instruct a computer what to do, let us concentrate rather on explaining to *human beings* what we want a computer to do.

(Knuth, 1984)

**Reproduction** of forecasting methods is not possible unless a method is *fully* explained. This includes the simplest forecasting methods.



# **Definition of Reproducibility**

If results are reproducible, then independent researchers are able to obtain the same numerical results by repeating the original study using the same methods on the same data.

(Boylan et al, IJF, 2015)

#### Comment

It should be possible for independent researchers to reproduce or replicate *without* any additional information from the author(s) of the original study.



# **Objectives of this Study**

#### **M-Competitions**

- Attempt to reproduce M-competition results
- Uncover any hidden assumptions
- Specify methods so fully that all simpler methods are reproducible
- Make available as a resource to researchers

#### More generally

- Identify areas to focus on in making forecasting results reproducible.
- Stimulate debate about journal policy in this area.



# **Clarification of Terminology**

	Same methods	Different methods
Same data	Reproduction Numerical Results	<b>Re-Analysis</b>
Different data	Replication Qualitative Conclusions	



# Why Reproduction?

#### Why should we reproduce?

- Increases reliability of numerical results
- Increases confidence in qualitative conclusions
- Reproduction is a necessary condition for replication

#### Why don't we reproduce?

- Data not available
- Methods not sufficiently clearly specified
- Considered too dull!



### **M-Competitions**

#### M1 and M3 competitions

- Landmark forecasting competitions.
- Established agenda for empirical research.
- "Can result in replicability and objectivity". (Fildes and Makridakis, 1995)

#### **Research Question: Are the studies reproducible?**

- Data has always been available.
- Are methods sufficiently well specified?
- Surely, not too dull to reproduce!



## Scope of Simple Methods to be Reproduced

Name of Method	M1	M3	
Naive 1			
Naïve 2		$\checkmark$	
Simple Moving Averages			
Single Exponential Smoothing			
Adaptive Response Rate ES			
Holt's Method			
Brown's Linear Method	$\checkmark$		
Linear Regression Trend	$\checkmark$		
Damped Trend		$\checkmark$	
Holt-Winters (Multiplicative)	$\checkmark$		
Combining Single-Holt-Damped		$\checkmark$	
Theta Method		$\checkmark$	



### Sources for Methods and Measures

#### Methods

- M1 (JF, 1982) and M3 (IJF, 2000) papers
- Sources cited by M1 or M3 papers
  - Makridakis & Wheelwright (Book, 1978)
  - Gardner & McKenzie (MS, 1985)
- Simmons (IJF, 1986) Naïve 2
- Ledolter & Abraham (1984) Backcasting

#### **Accuracy Measures**

• M1, M3 papers, and Armstrong & Collopy (IJF, 1992) (MSE, MAPE, MedAPE, sMAPE)



# Methodology

#### Two independent teams

- One team uses MATLAB, the other Visual Basic
- Each works using same sources of information
- Each documents any additional assumptions

### Chairperson

- Exchange results via 'chairperson' (JB)
- Iterate process until agreement on results

*Similar process as in Miller & Williams reproduction study (IJF, 2015)* 



## Accuracy Measures (Naïve 1)

### Median of all APEs or median of median (per series) APEs?

- Agreement with M1 for in-sample MedAPE if use "overall median" rather than "median of medians".
- Two methods give quite different results in-sample: MedAPE = 5.9% (Overall Median) v MedAPE = 5.4% (Median of Medians)
- Out-of-sample Overall Median (New) very close to M1 results but not exact. Occasional results do not agree to the first decimal place.



### Naïve 2 Method (Deseasonalisation)

#### What is Naïve 2?

"... as Naïve 1 but the data are deseasonalized and then seasonalized. The seasonal indices for deseasonalizing and seasonalizing the data were done by the decomposition method of the ratio-to-moving averages. The specifics of this method can be seen in Makridakis and Wheelwright (1978) pp 94-100."

(Makridakis et al, 1982)



# Early Attempt to Reproduce M1 Results for Naïve 2

Simmons (1986) found that:

- The seasonal indices used in Naïve 2 could not be reproduced using the procedure defined in the paper.
- The median was not calculated as one may have expected.

Simmons clarified, through written correspondence with Spyros Makridakis:

- A pre-processing procedure is executed before employing the decomposition method.
- Avoids losing second half of the last seasonal cycle.



### Pre-Processing Procedure (Simmons, 1986)

Let  $X_t$  (t=1,..., N) be defined as the original time series, L be defined as the number of seasons, and K be defined as the number of whole years in the data. Thus, K is the largest whole number less that or equal to N/L. Then  $Z_t$   $\{t=1,..., M$ ; where  $M = (K+1)L\}$ , the actual series used by the centered ratio-to-moving average decomposition method, is defined in the following steps:

(1) 
$$Z_t = (X_{N-3} + X_{N-2} + X_{N-1} + X_N)/4$$
, for  $t = M - L/2 + 1, ..., M$ ,  
(2)  $Z_t = X_{t+N-M+L/2}$ , for  $t = L/2 + 1, ..., M - L/2$ ,  
(3)  $Z_t = (X_1 + X_2 + X_3 + X_4)/4$ , for  $t = 1, ..., L/2$  with the following exceptions  
 $Z_t = X_{t-0}$  if  $N - KL \ge L/2 - 0$ , for  $t = 1, ..., L/2$ ,  
 $Z_t = X_{t-1}$  if  $N - KL \ge L/2 - 1$ , for  $t = 2, ..., L/2$ ,  
 $\vdots$   
 $Z_t = X_{t-1}$  if  $N - KL = L/2 - (L/2 - 1)$ , for  $t = L/2, ..., L/2$ .

Step (2) means that the new series is the same as original series shifted forward by N-M+L/2 periods.



# Example of 'Shifting' of Series

Series QNM1 (13 in-sample observations)



Pre-processing shifts the data forward by one period .

Seasonal indices, based on the pre-processed data, should be applied to the previous period of the original data



### **Issues not Clarified by Simmons**

- Length of data for pre-processing should be based on in-sample series.
- Inclusion of series with insufficient data to calculate medial (Winsorized) average – use straight average
- Application of seasonal indices to shifted data

• Having clarified these aspects of the method, seasonal indices agreed with M1 indices.



### Specification of SMA in the M1 Paper

(2) Simple moving average.

Model fitting: 
$$\hat{X}_{t+1} = \frac{X_t + X_{t-1} + X_{t-2} + \dots + X_{t-N+1}}{N}$$
, (6)

where N is chosen so as to minimize  $\sum e_t^2$ , again summing over t from 1 to n - m

Forecasts: 
$$X_{n-m+k} = \frac{X_{n-m+k-1} + X_{n-m+k-2} + \dots + X_{n-m+k-N}}{N}$$
. (7)

When the subscript of X on the right-hand side of (7) is larger than n - m, the corresponding forecasted value is substituted.

- This is not a 'flat forecast' throughout the horizon, based on the last N periods. The forecast for t+2 includes the forecast for t+1 in the Moving Average.
- Clarifications: minimise MSE (not SSE);  $N \ge 2$ .



### SMA Comparison (M1 Competition)

MAPE					
Horizon	1	3	6	12	18
M1	13.0	17.6	25.0	17.8	31.3
M1Reproduced	13.0	18.0	25.0	18.5	30.3
M1Re-ananlysed	13.0	18.2	25.4	19.0	30.3
MedAPE					
Horizon	1	3	6	12	18
M1	6.8	9.0	13.1	11.8	15.4
M1 Reproduced	7.6	9.3	12.8	12.1	15.3
M1 Re-analysed	7.6	9.5	13.1	12.6	16.2

- Reproduction: some differences remain.
- Re-analysis using 'flat forecast' shows further differences.

## Specification of SES in the M1 Paper

(3) Single exponential smoothing.

Model fitting: 
$$\hat{X}_{t+1} = \alpha X_t + (1 - \alpha) \hat{X}_t$$
, (8)

where  $\alpha$  is chosen so as to minimise  $\sum e_t^2$ , the mean square error where again summing is over t from 1 to n - m.

Forecasts: 
$$\hat{X}_{n-m+k} = \alpha X_{n-m} + (1-\alpha) \hat{X}_{n-m+k-1}.$$
 (9)

- Again, this is not a 'flat forecast' throughout the horizon.
- According to Equation (9), the forecast for t+2 includes the forecast for t+1 in the update of SES.



## Backcasting

- Backcasting as defined in Ledolter and Abraham (1984) is based on within-sample:
  - Same smoothing constant as for forecasting,
  - The initial value for backcasting is the last observation,
  - The last available smoothed value is used as the initial value for SES forecasting.
- This is the version of backcasting used to produce our results.



### SES Comparison (M1 Competition)

MAPE					
Horizon	1	3	6	12	18
M1	11.2	16.2	24.1	17.5	31.2
M1 Reproduced	11.2	16.5	24.8	16.6	30.9
M1 Re-analysed	11.2	16.3	24.2	17.5	30.1
MedAPE					
Horizon	1	3	6	12	18
M1	6.0	8.6	12.5	11.3	14.9
M1 Reproduced	6.1	8.7	13.0	10.3	16.0
M1 Re-analysed	6.0	8.5	12.6	11.3	15.0

- Reproduction: some differences at longer horizons.
- Re-analysis using 'flat forecast' close to M1 results.

## Discussion

- M Competitions represented a major advance in empirical forecasting and data transparency. Since then, method transparency has not developed as fast as it should.
- Re-examination of the M-competitions illustrates the need for greater clarity on:
  - Error measures across series
  - Seasonal adjustment procedures
  - Forecasting methods employed out-of-sample
  - IMA Jnl of Management Mathematics introduced a 'kite mark' for reproducible papers. Time for others to follow?



#### Thank you for your attention!

#### Q&A?

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