

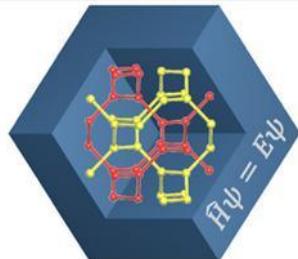


UNIVERSITÀ DEGLI STUDI DI MILANO
DIPARTIMENTO DI CHIMICA

Lucia Carlucci & Gianfranco Ciani

Davide M Proserpio
**Entanglements in
periodic structures:
old and new views**

Vladislav Blatov & Evgeny Alexandrov
Igor Baburin



Samara Center
for Theoretical Materials Science

The Geometrical Basis of Crystal Chemistry. Part 1

BY A. F. WELLS

Imperial Chemical Industries Limited (Dyestuffs Division), Hexagon House, Manchester 9, England

(Received 1 January 1954 and in revised form 1 April 1954)

A. F. Wells

1954 - 1979

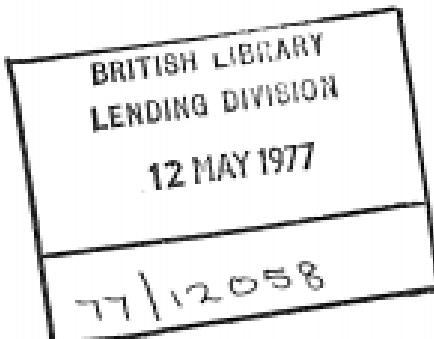
Structural
Inorganic
Chemistry

4th Edition

Three-dimensional
nets and polyhedra

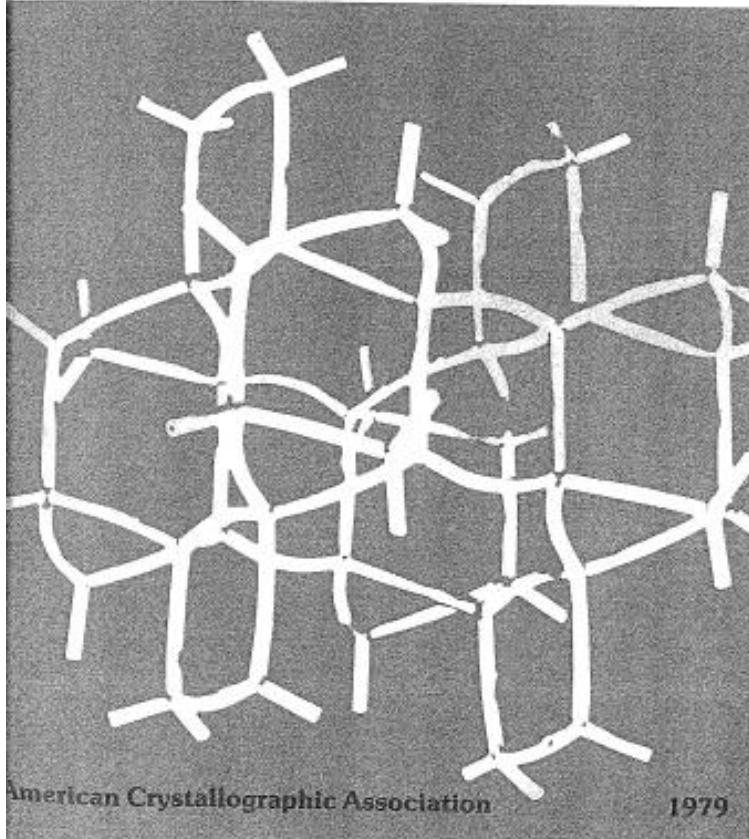
A. F. Wells

Department of Chemistry
and
Institute of Materials Science
University of Connecticut



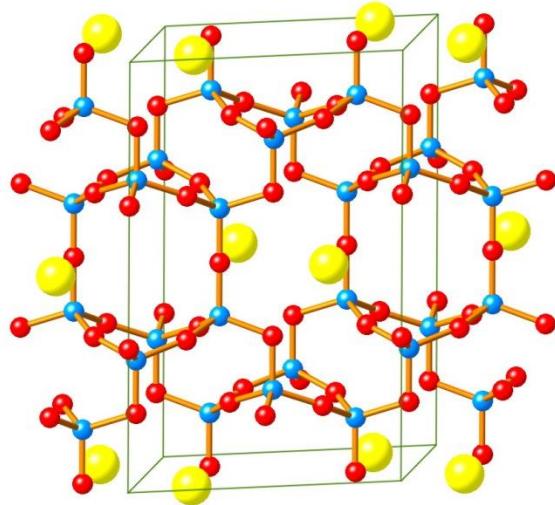
Further Studies of Three-dimensional Nets

A.F. Wells ACA Monograph No. 8

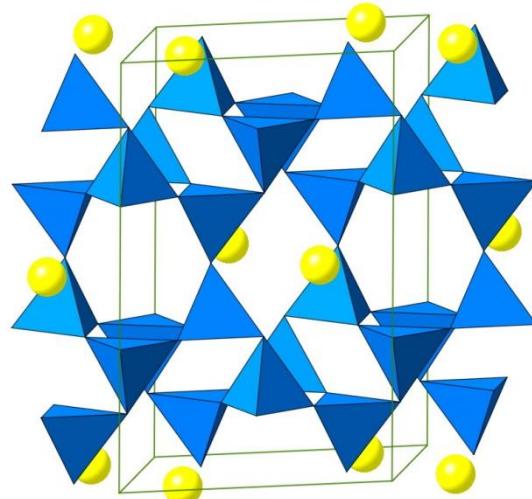


Three ways of drawing a feldspars

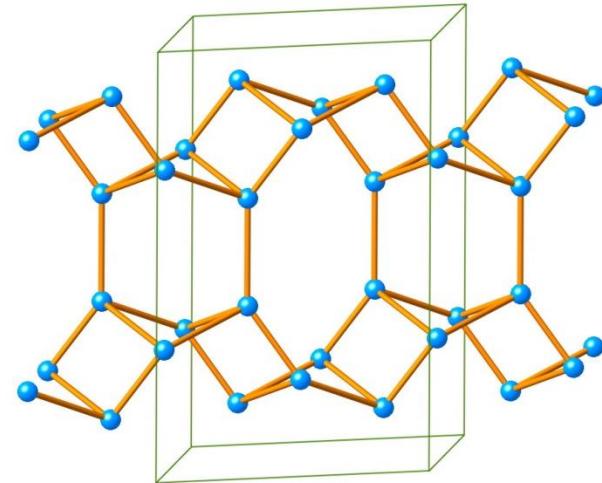
the most abundant minerals in the earth's crust $M[(Si/Al)_4O_8]$, e.g. albite, $Na(Si_3AlO_8)$, orthoclase, $K(Si_3AlO_8)$, anorthite, $Ca(Si_2Al_2O_8)$.



ball and stick



polyhedra



net

From the framework of alumino-silicates we get a **net** by
removing all 2-coordinated oxygen atoms -T-O-T-

R. Robson 1989-

(Melbourne - Australia)

J. Am. Chem. Soc. 1990, 112, 1546–1554

Design and Construction of a New Class of Scaffolding-like Materials Comprising Infinite Polymeric Frameworks of 3D-Linked Molecular Rods. A Reappraisal of the $\text{Zn}(\text{CN})_2$ and $\text{Cd}(\text{CN})_2$ Structures and the Synthesis and Structure of the Diamond-Related Frameworks

$[\text{N}(\text{CH}_3)_4][\text{Cu}^{\text{I}}\text{Zn}^{\text{II}}(\text{CN})_4]$ and
 $\text{Cu}^{\text{I}}[4,4',4'',4'''\text{-tetracyanotetraphenylmethane}] \text{BF}_4 \cdot x\text{C}_6\text{H}_5\text{NO}_2$

B. F. Hoskins and R. Robson*

> 1500 citations

Infinite Polymeric Frameworks Consisting of Three Dimensionally Linked Rod-like Segments

Bernard F. Hoskins and Richard Robson*

Department of Inorganic Chemistry
University of Melbourne
Parkville, Victoria, 3052, Australia

Received February 14, 1989

Scaffolding-Like Materials

Infinite Polymeric Frameworks

DALTON
PERSPECTIVE

A net-based approach to coordination polymers †

Richard Robson

School of Chemistry, University of Melbourne, Parkville, Victoria, 3052, Australia

Received 4th May 2000, Accepted 23rd June 2000

First published as an Advance Article on the web 9th October 2000

J. Chem. Soc., Dalton Trans., 2000, 3735–3744

early '90

Infinite Polymeric Frameworks

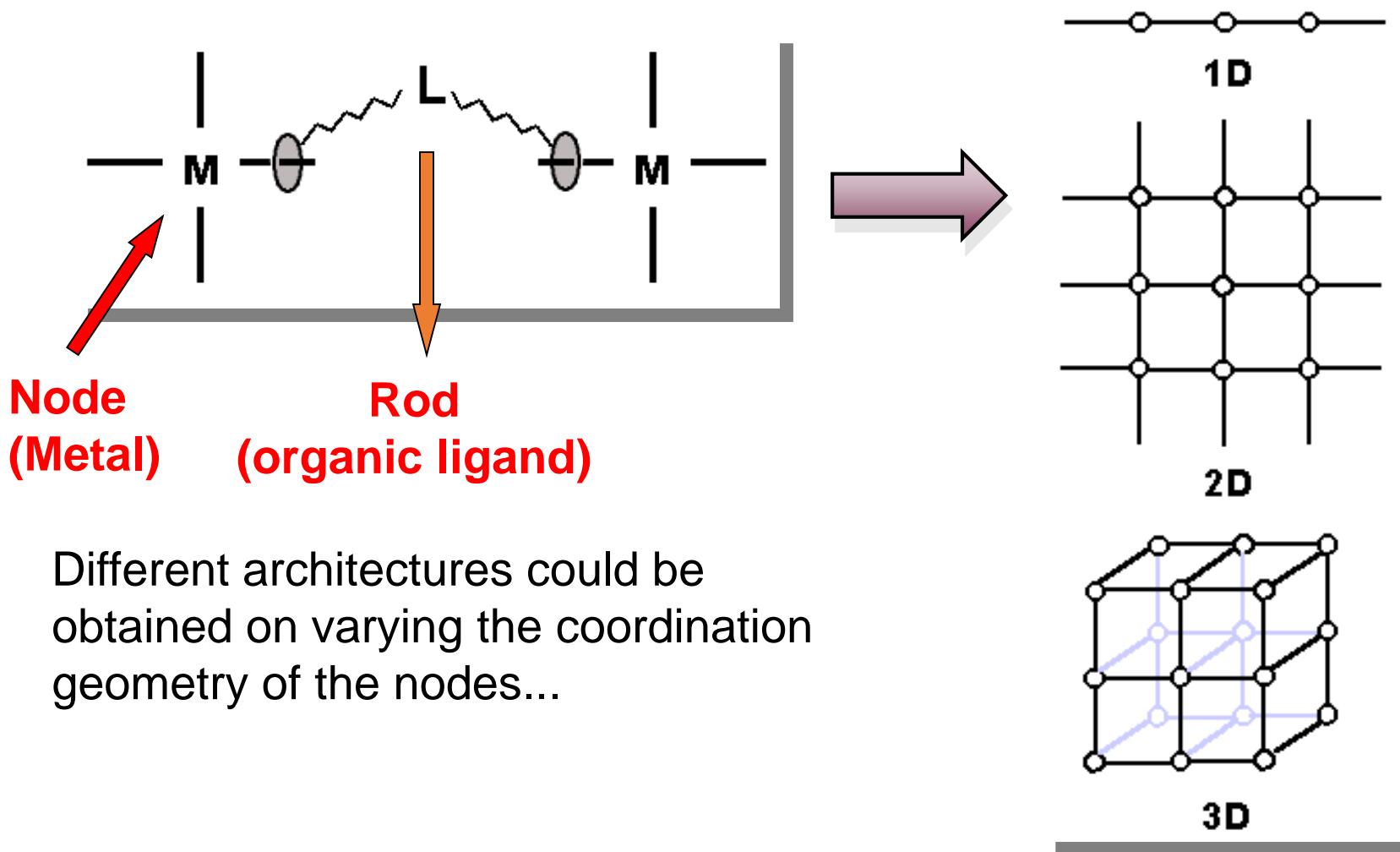
Organic/Inorganic Hybrid Materials

Coordination Polymers (*Networks*)

Metal Organic Frameworks (MOFs)

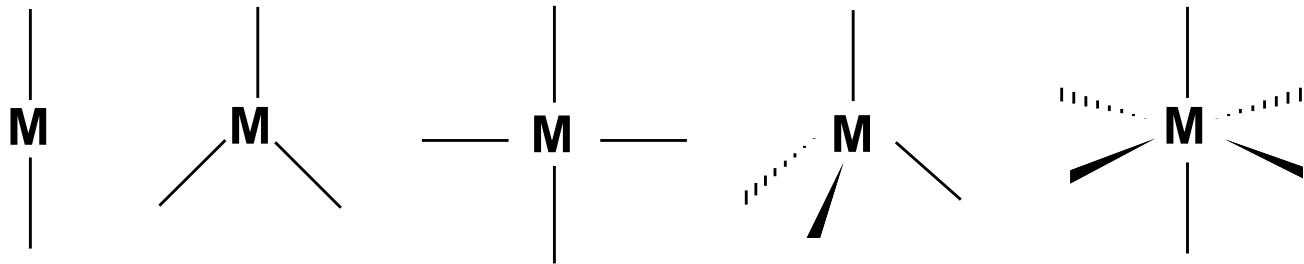
Coordination Networks

“Metal-organic Frameworks” MOF

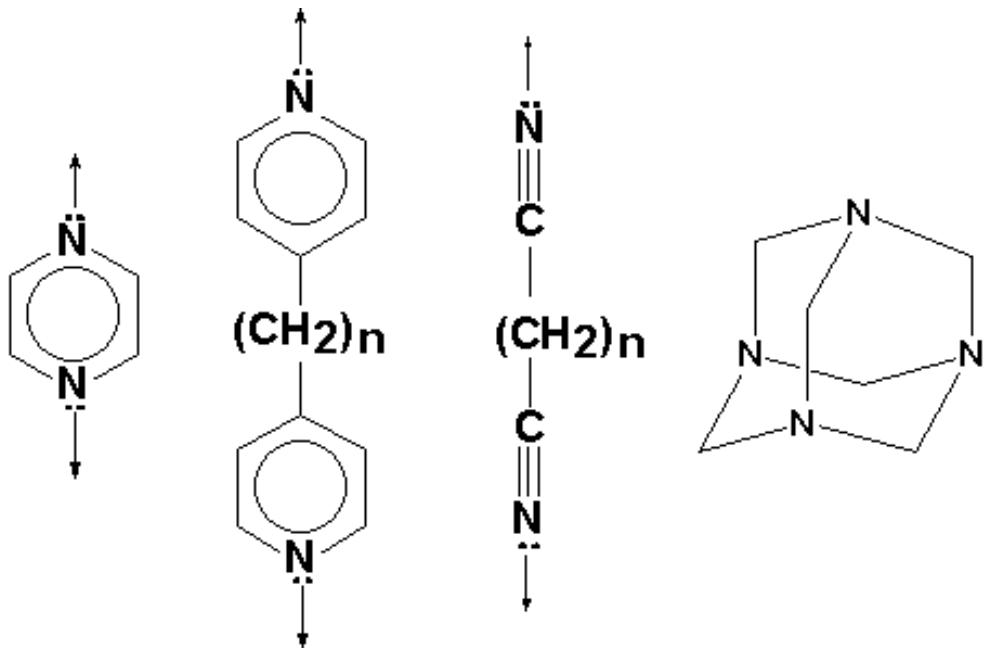


Metal ions: Ag, Cu, Ni, Co, Zn, Cd...

coordination number
and geometry



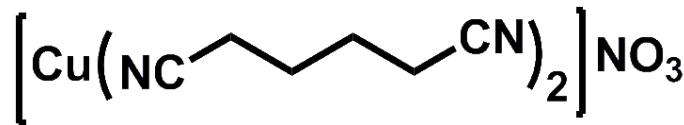
Ligands



donors: N, O, P, S
bi/polidentate
neutral/anionic
Length
rigidity/flexibility

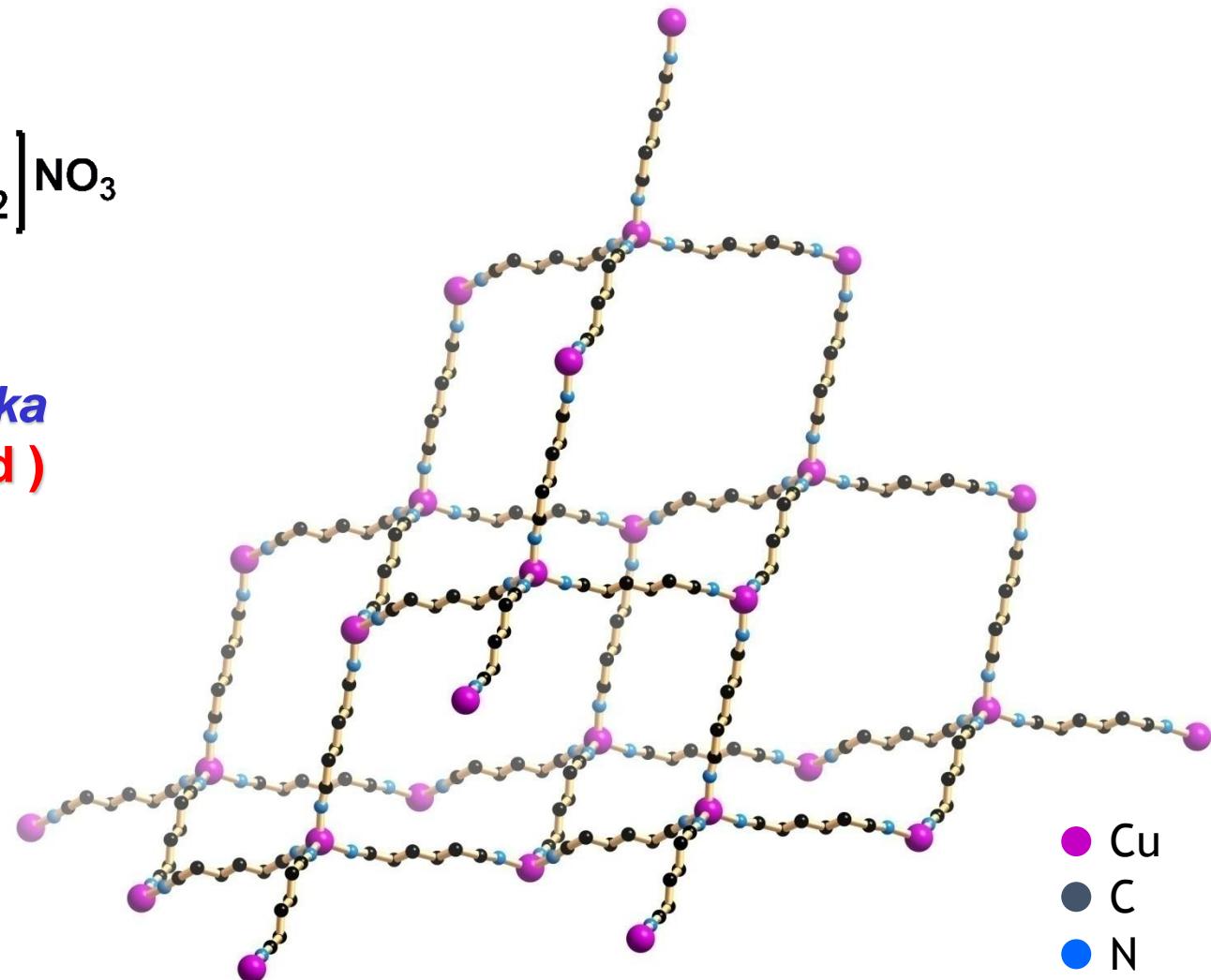
Coordination Network

1959



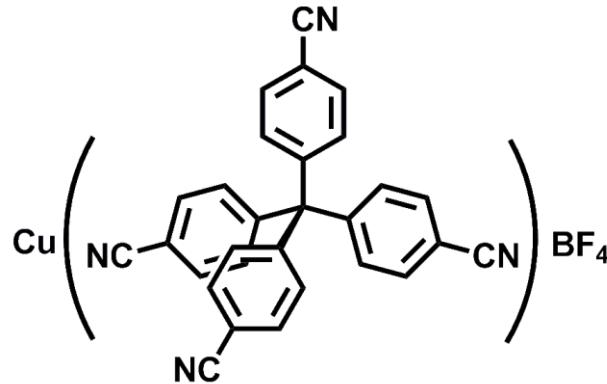
**multiply intergrown aka
interpenetrated (6-fold)**

**underlying net:
diamondoid
(dia)**

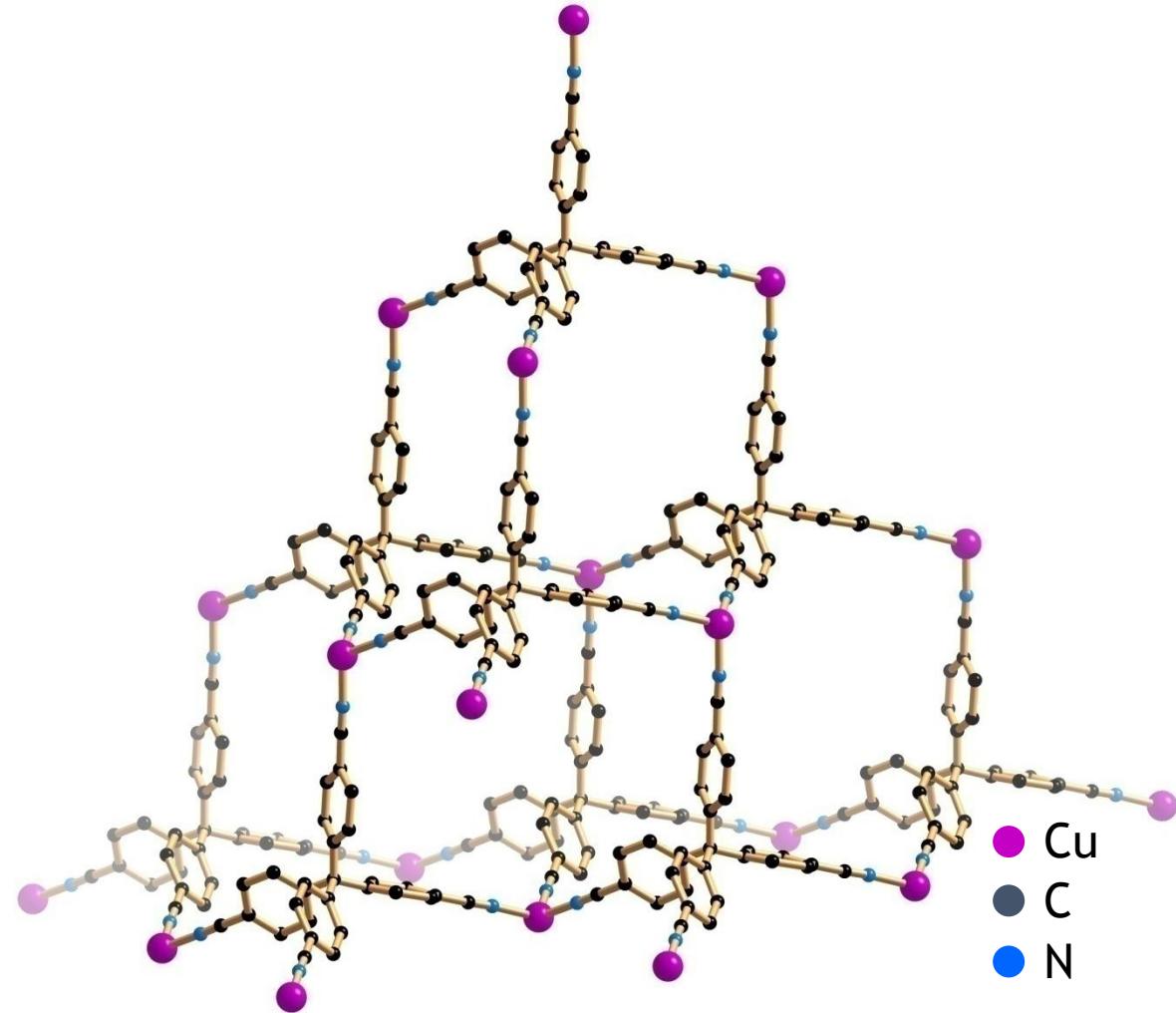


Coordination Network with polytopic links

1989

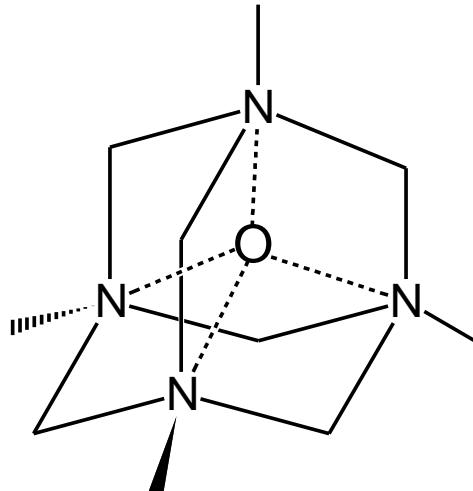
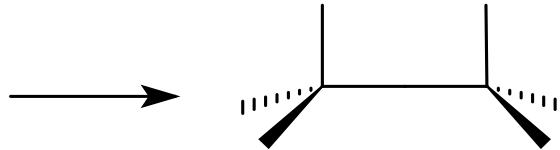
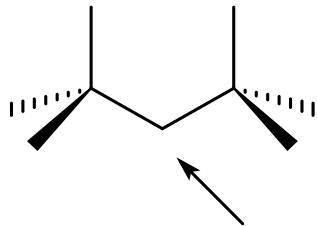


underlying net: dia

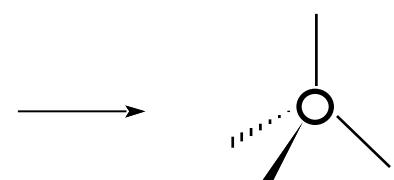


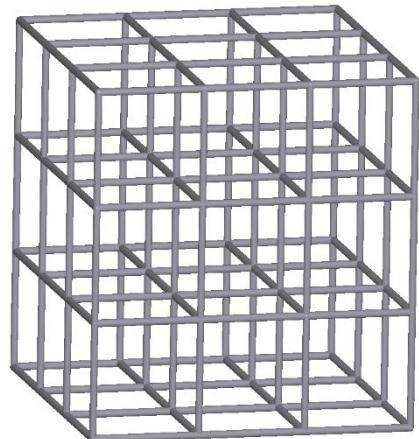
Simplifications:

Keep only atoms with coordination/connectivity > 2
→ Nodes/Vertex of the Net



Simplification of polydentate groups with centres of the same coord/conn





H. Li, M Eddaoudi, M. O'Keeffe, O.M. Yaghi

Nature 1999 MOF-5

(Metal-Organic Framework-5)

underlying net: pcu

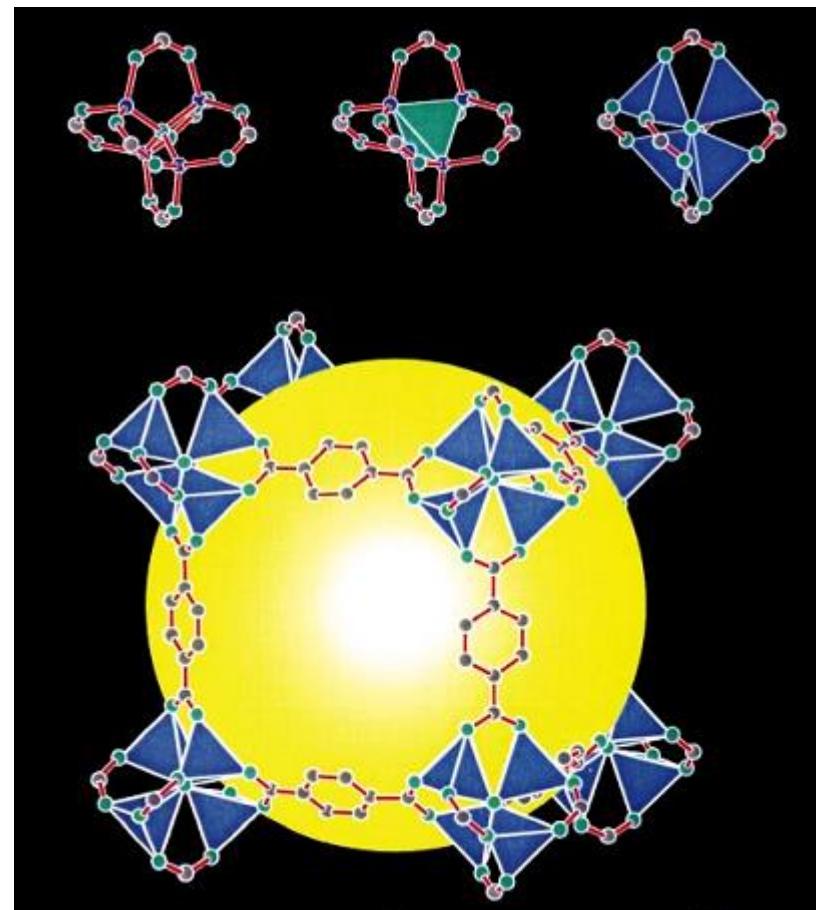
.....

Design and synthesis of an exceptionally stable and highly porous metal-organic framework

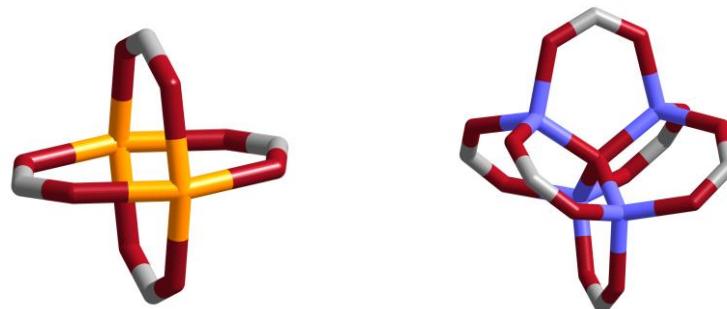
Hailian Li*, Mohamed Eddaoudi†, M. O'Keeffe* & O. M. Yaghi†

NATURE | VOL 402 | 18 NOVEMBER 1999 | w

> 5000 citations

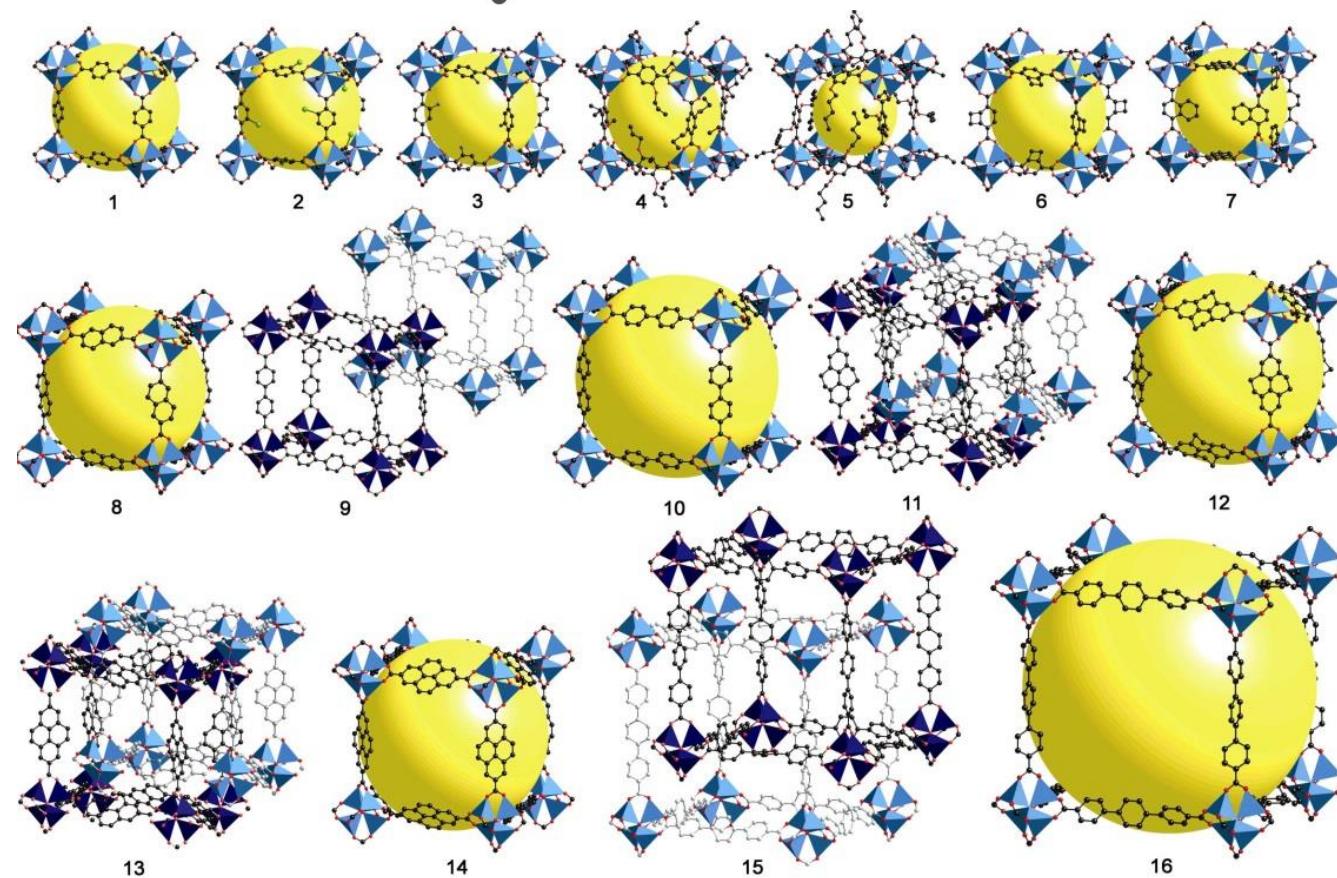


Reticular Chemistry



≈ 2000

O.M.Yaghi, M. O'Keeffe
Nature 2003 > 6500 citations



Why interest in Coordination Networks (MOFs) ?

Doubling time 3.9 yrs compared with 9.3 yrs for all CSD!

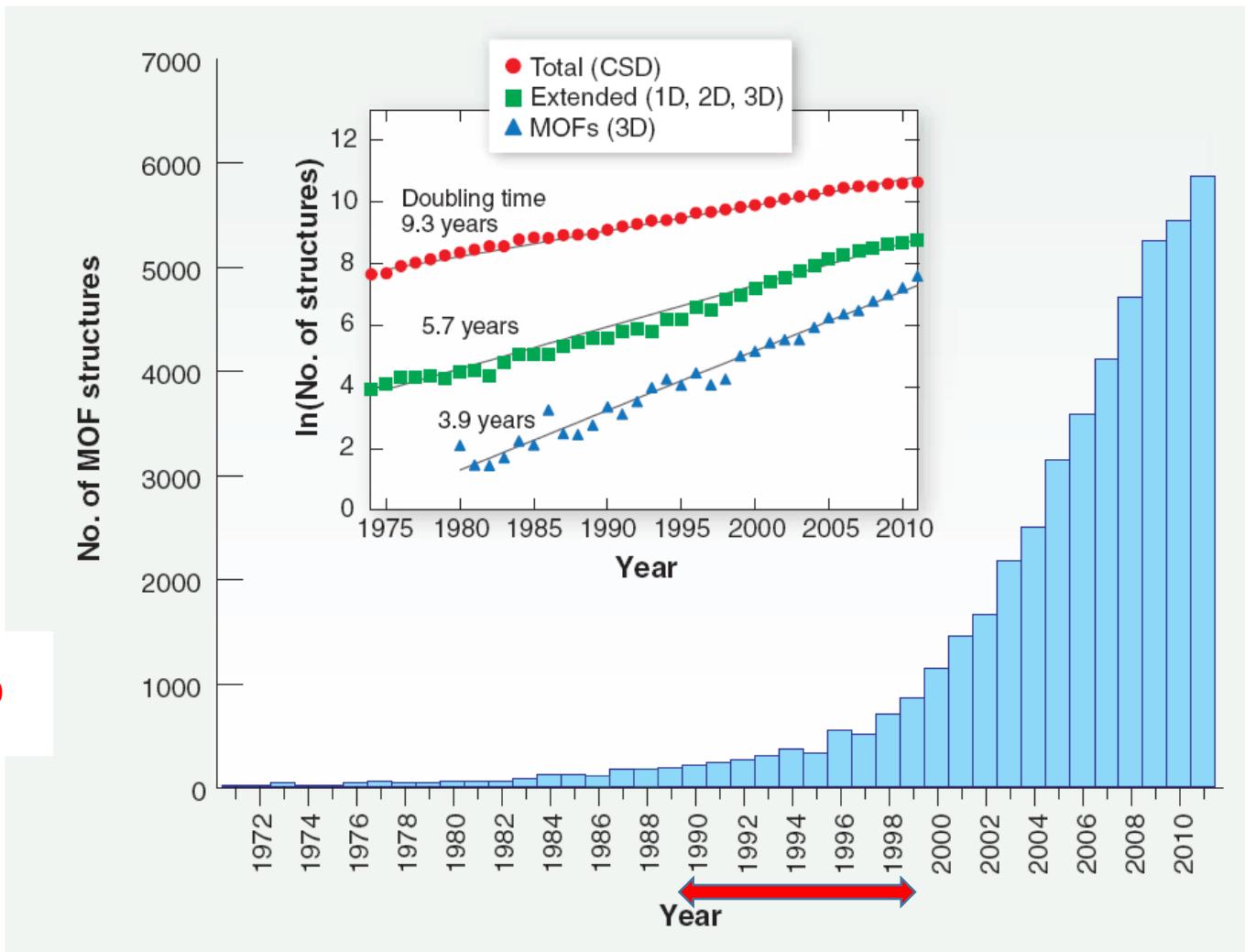


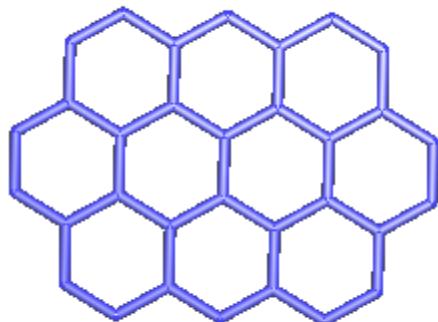
Fig. 1. Metal-organic framework structures (1D, 2D, and 3D) reported in the Cambridge Structural Database (CSD) from 1971 to 2011. The trend shows a striking increase during this period for all structure types. In particular, the doubling time for the number of 3D MOFs (inset) is the highest among all reported metal-organic structures.

A **Net**, as used in solid state chemistry, is a
n-periodic connected simple graph

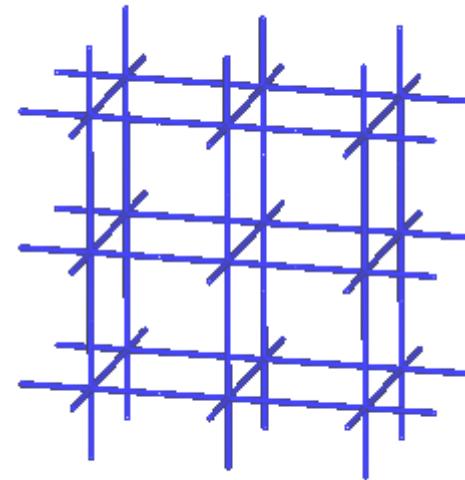
n-periodic = has translational symmetry in *n*-independent directions

connected = there is a continuous path between every pair of vertices

simple = contains only simple edges



2-p

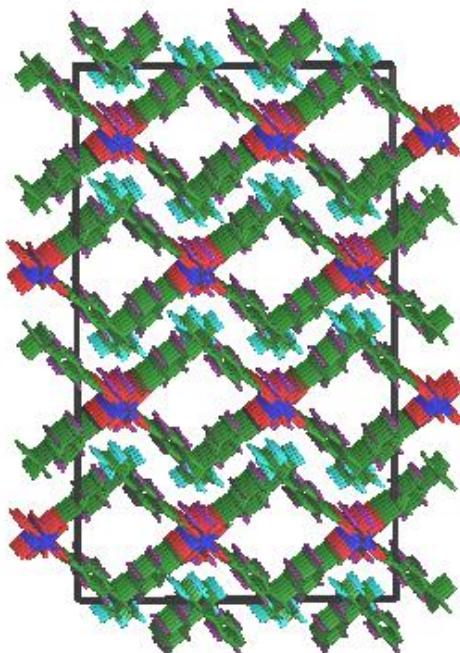


3-p

Periodic Structures and Crystal Chemistry

n-Periodic Structures

structures (as nets) that have **translational symmetry** in exactly *n* independent directions.



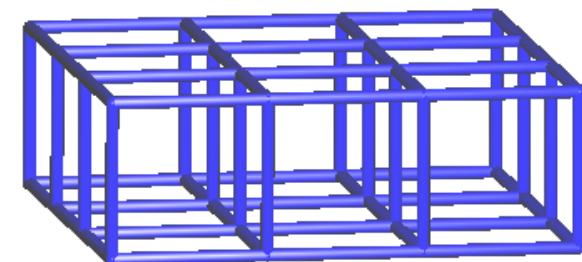
Any crystalline material is a 3D ordered arrangement of atoms

any crystal is a 3D supramolecular entity

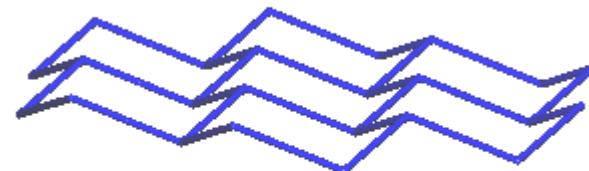
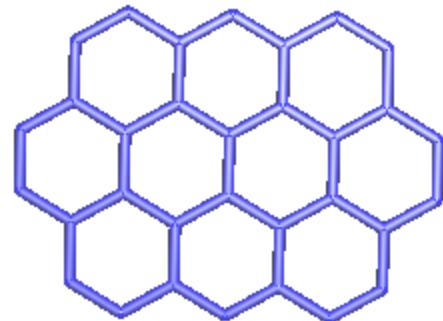
depending on the interactions considered we may “see” chains 1-periodic, layers 2-periodic or 3-periodic networks

Double-layers are 3D 2-periodic

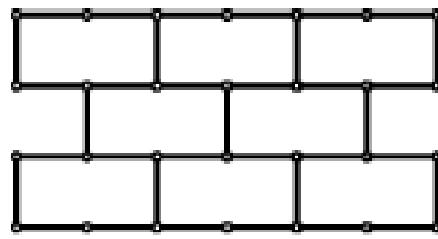
2-p 3D



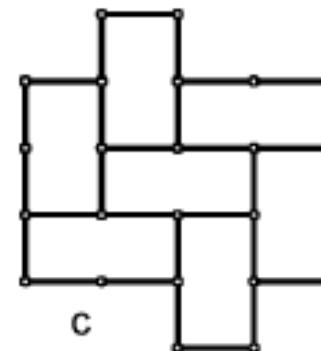
2-p 2D honeycomb layer



$6^3\text{-}hcb$



brick wall



parquet

Crystal Structures

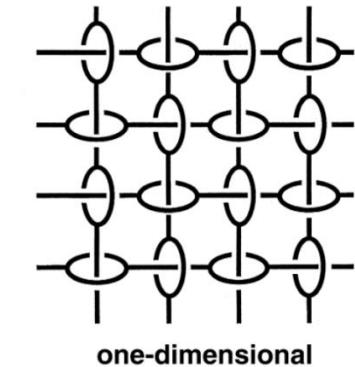


Underlying Net

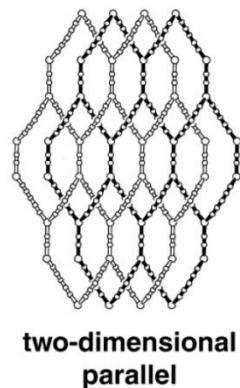
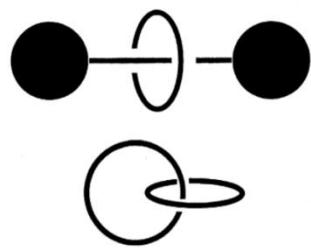


Entanglements

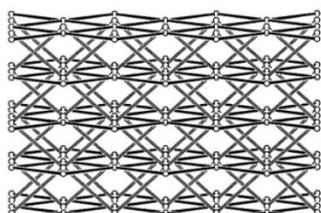
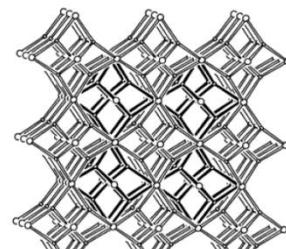
Stuart R. Batten and Richard Robson*



one-dimensional

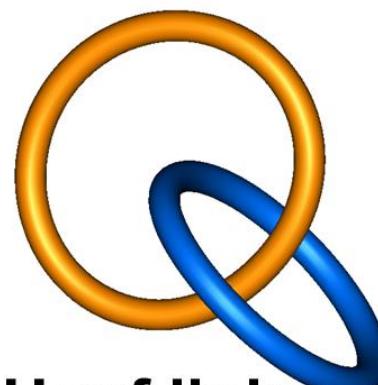
two-dimensional
parallel

zero-dimensional

two-dimensional
inclined

three-dimensional

Interpenetrating structures, are characterized by the presence of infinite structurally **regular motifs** that must contain **rings** through which independent components are inextricably entangled and that can be disentangled only by breaking internal connections

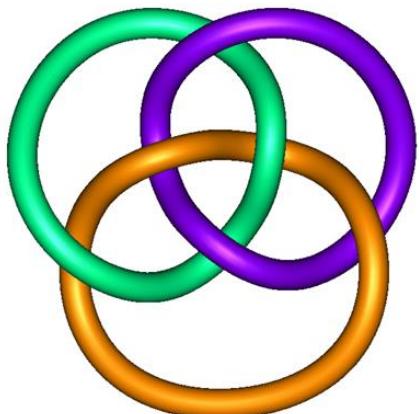


Hopf link

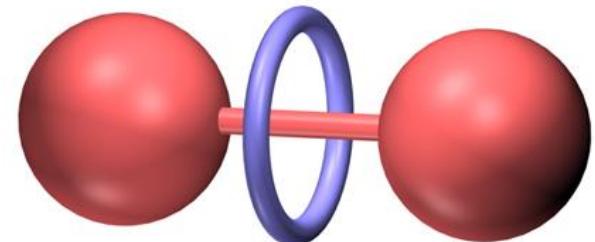
Geometrical requirement for Inextricable Entanglement



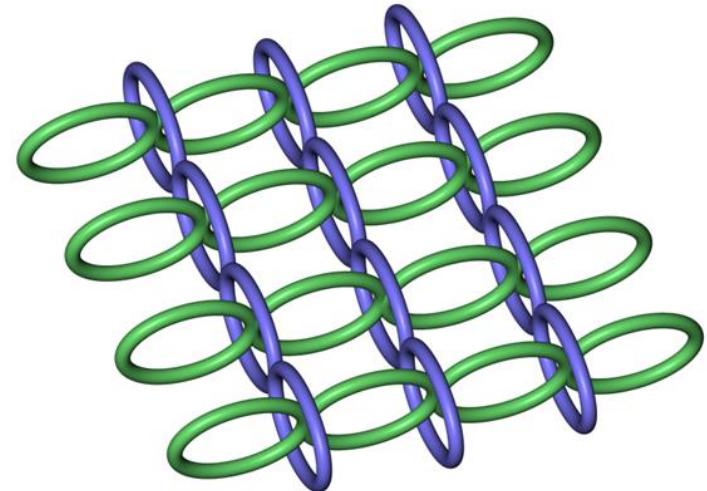
Hopf link



Borromean



[2]-rotaxane



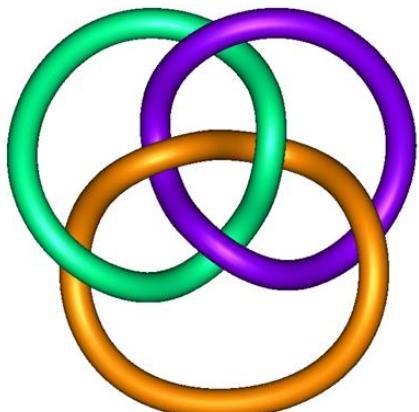
***“Topological”
Entanglement***

***“Euclidean”
Entanglement***

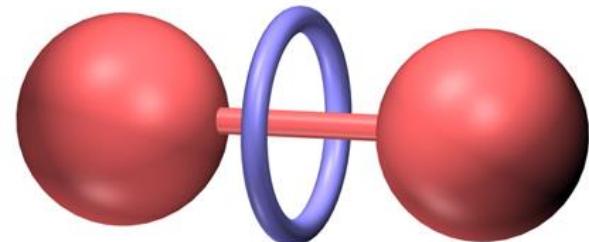
Geometrical requirement for Inextricable Entanglement



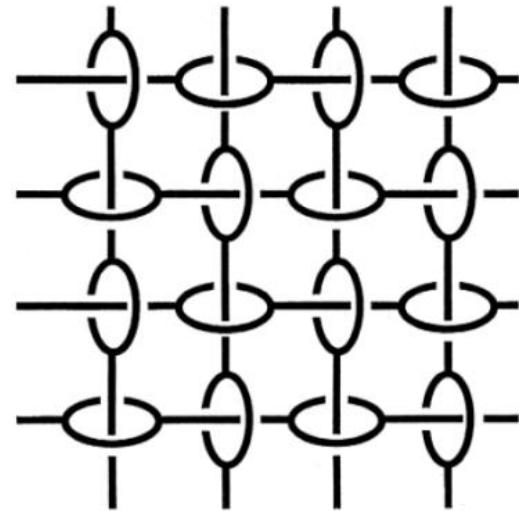
Hopf link



Borromean



[2]-rotaxane



***“Topological”
Entanglement***

***“Euclidean”
Entanglement***

1954

The Geometrical Basis of Crystal Chemistry. Part 4

BY A. F. WELLS

Imperial Chemical Industries Limited (Dyestuffs Division), Hexagon House, Manchester 9, England

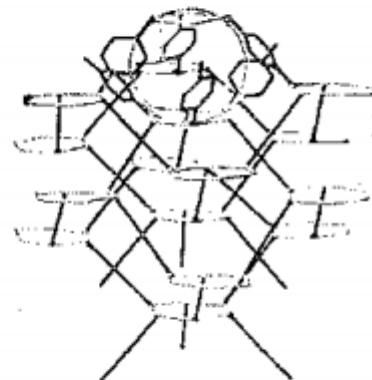
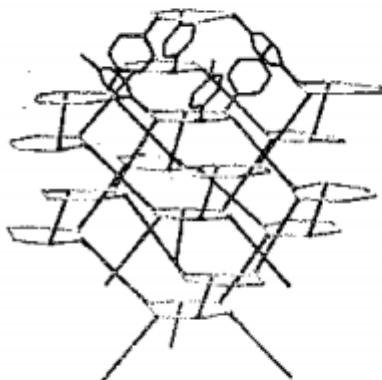
(Received 7 May 1954)

Structures based on a single net of low coordination number are unlikely to occur owing to their low densities. A study has therefore been made of systems of two or more interpenetrating three-dimensional networks. Some of the possible structure types are illustrated.

50. *The Structure of Molecular Compounds. Part III. Crystal Structure of Addition Complexes of Quinol with Certain Volatile Compounds.*

By D. E. PALIN and H. M. POWELL.

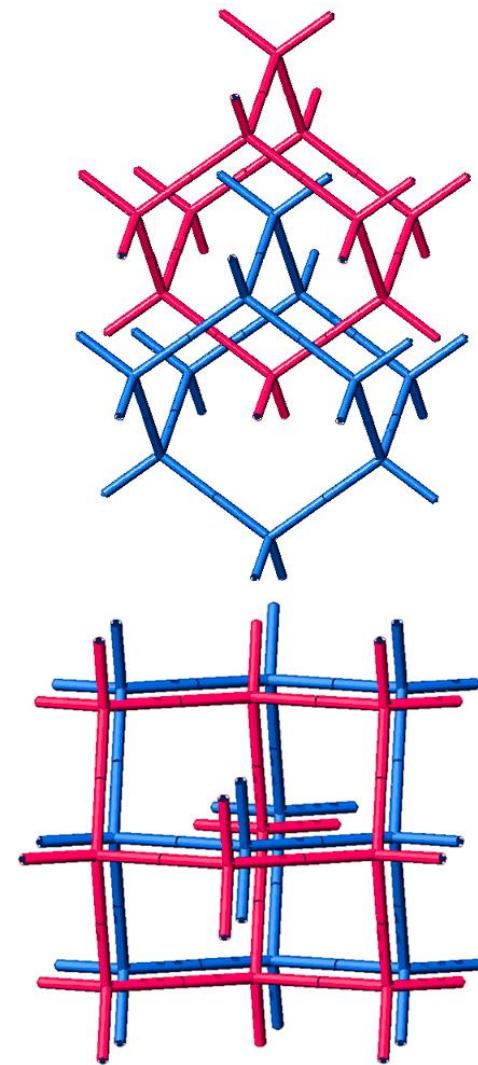
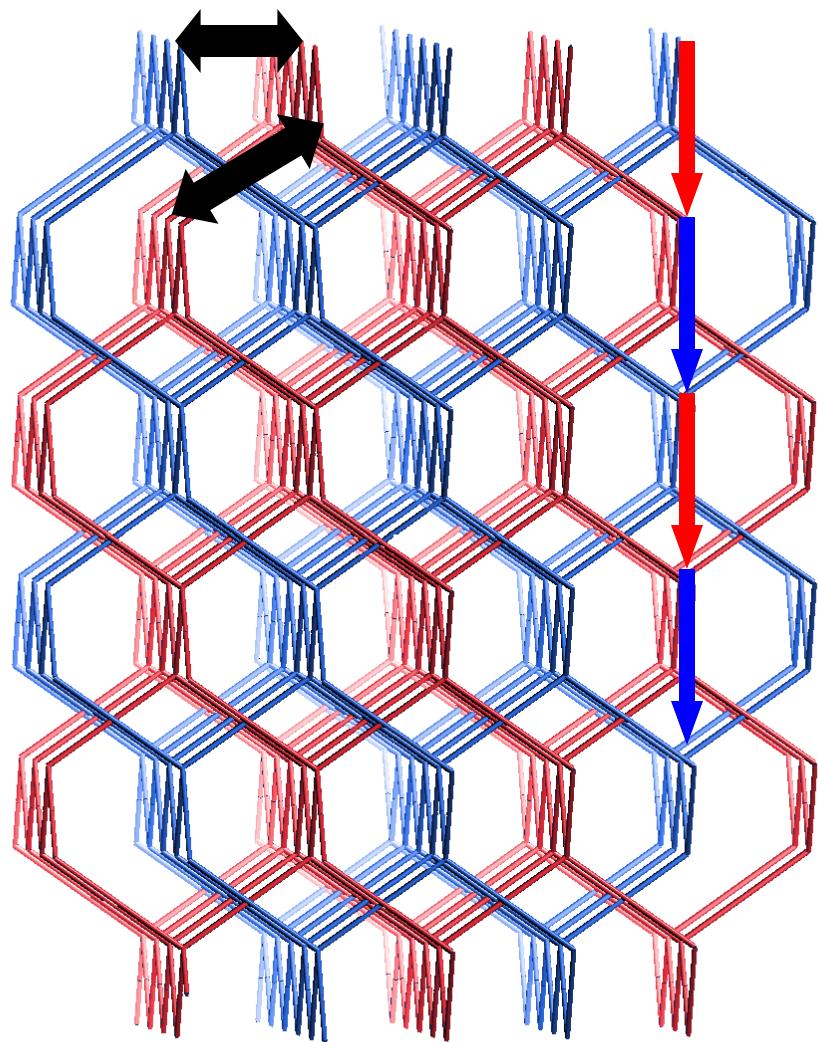
1947
quinol



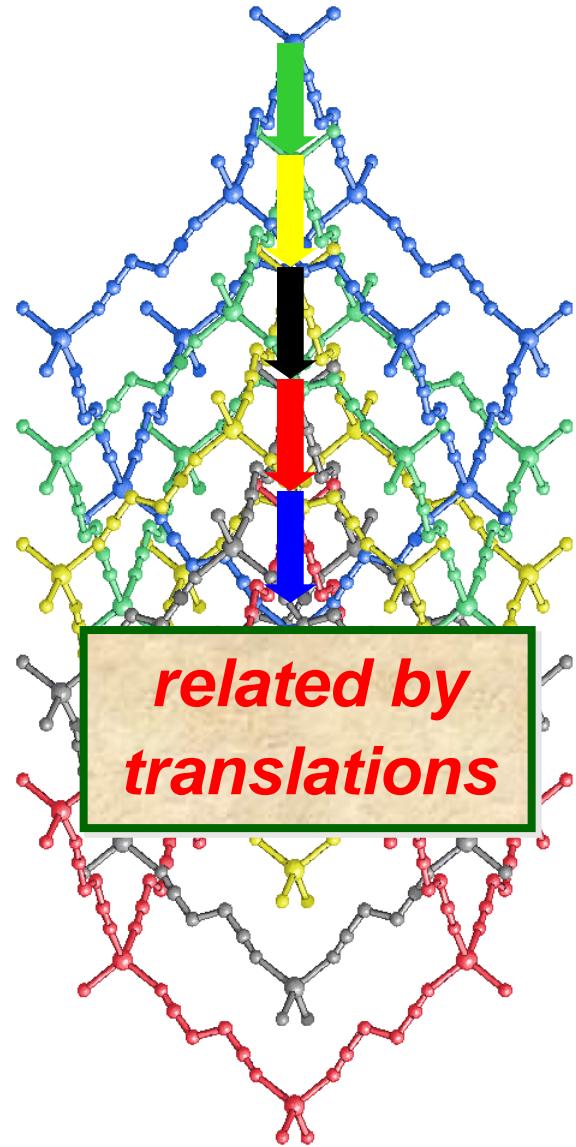
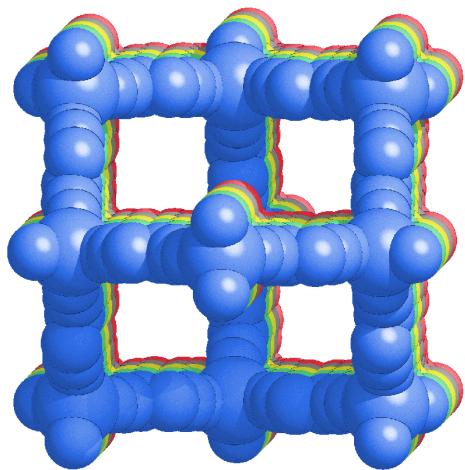
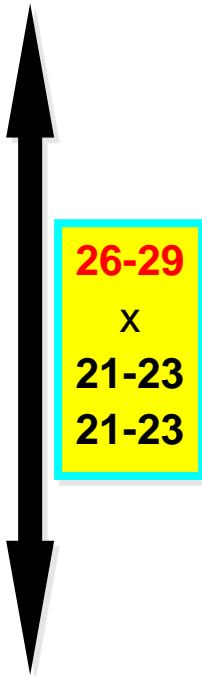
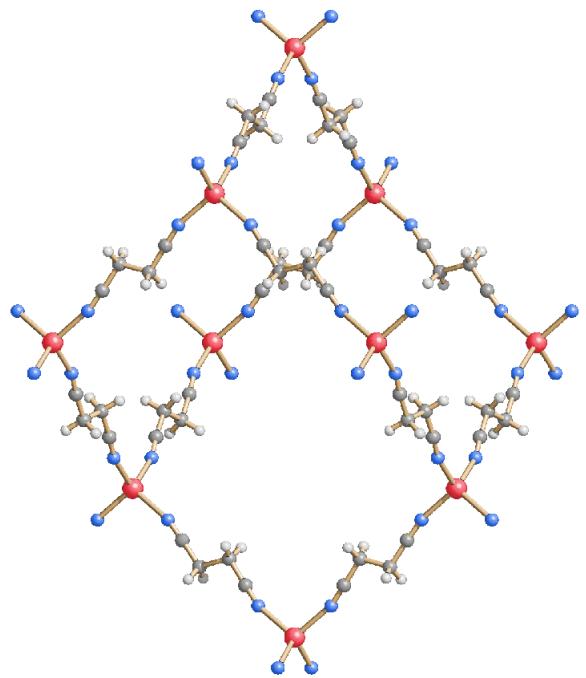
Cuprite
 Cu_2O
Niggli
1922

Stereoscopic representation of interpenetration of two similar hydrogen-bonded cageworks each identical with that shown in Fig. 13. Benzene rings are shown by small hexagons in the upper part of the figure but are elsewhere omitted for clarity. The larger hexagons represent the hydrogen bonds. The roughly spherical space enclosed between the two cageworks is also shown.

interpenetration of diamondoid nets



$[\text{Ag}(1,4\text{-butanedinitrile})_2](X)$ X= BF_4^- , ClO_4^- , PF_6^- , AsF_6^- , SbF_6^-



Diamondoid-5f

Class I (a,b)

Nets related only by translation

Class II (a,b)

Nets related only by non-translational symmetry elements

Class III (a,b,c,d)

Nets related by translational and non-translational symmetry elements

world records of Interpenetration

2000 11-fold dia H-bond

2002 10-fold dia CNet (Ia)

2005

18-fold srs H-bond (IIIb)

2008

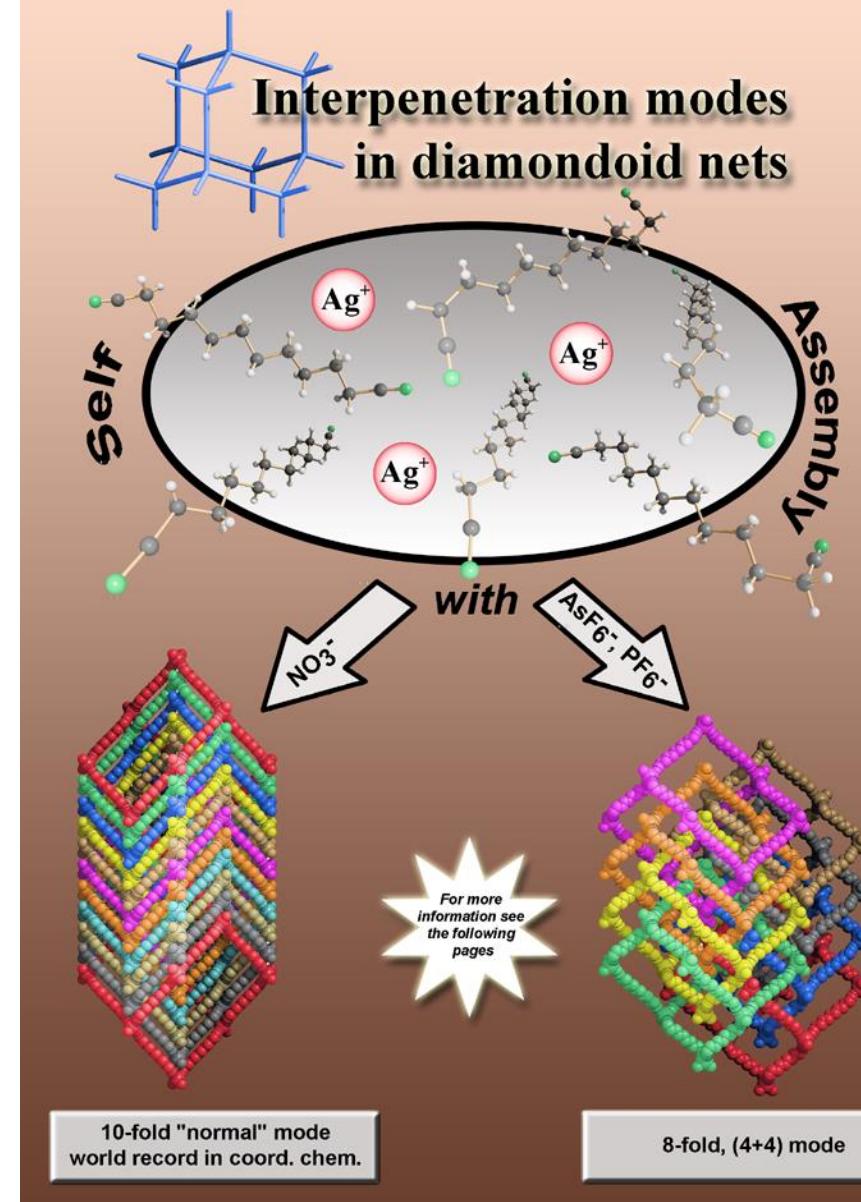
12-fold dia/ths CNet (IIIa)

2009

18-fold dia H-bond (IIIb)

2011

54-fold srs CNet (IIIb)



Applied Topological Analysis of Crystal Structures with the Program Package ToposPro

Published as part of the *Crystal Growth & Design* Mikhail Antipin Memorial virtual special issue

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[‡]Chemistry Department, Faculty of Science, King Abdulaziz University, P.O. Box 80203, Jeddah 21589, Saudi Arabia

[§]Università degli Studi di Milano, Dipartimento di Chimica, Via C. Golgi 19, 20133 Milano, Italy



rogram package for multipurpose
crystallochemical analysis

ToposPro

Version 5.0

PRACTICAL MANUAL 1.1.1

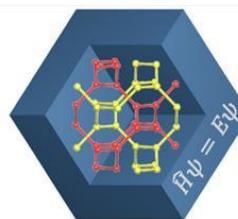
V.A. Blatov & D.M. Proserpio

Revision summer 2014

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www.topospro.com

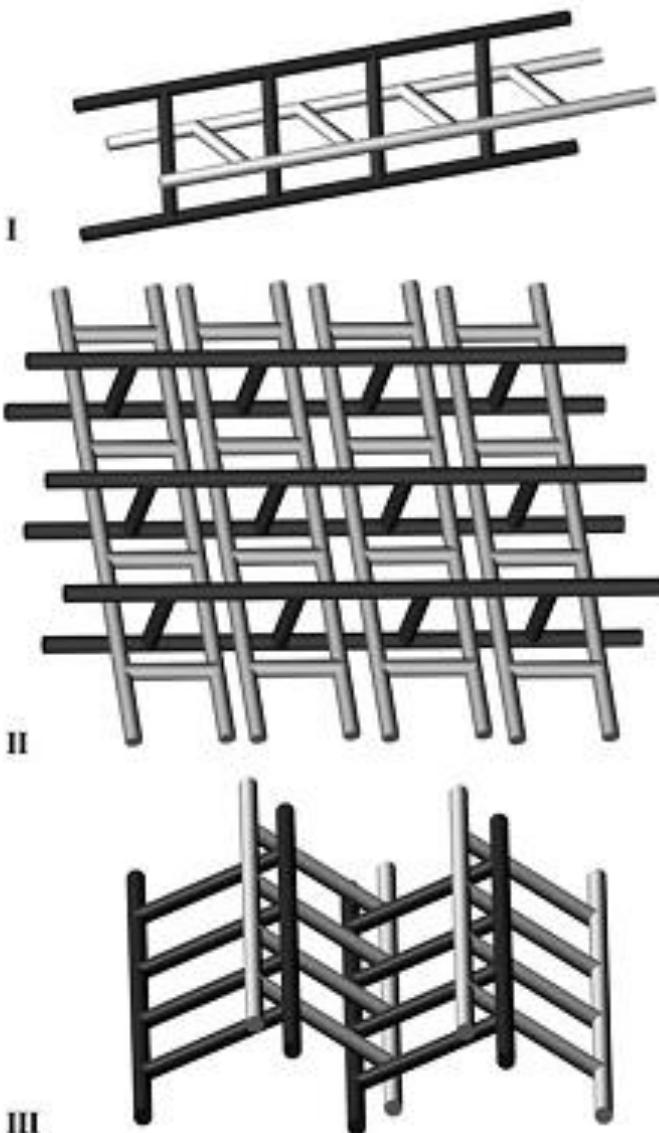


**Samara Center
for Theoretical Materials Science**

**Can we entangle 1-p or 2-p nets
in a different way (topological)?**

**Interpenetration
vs.
Polycatenation**

***1-p
Ladders
+
Hopf
Links***



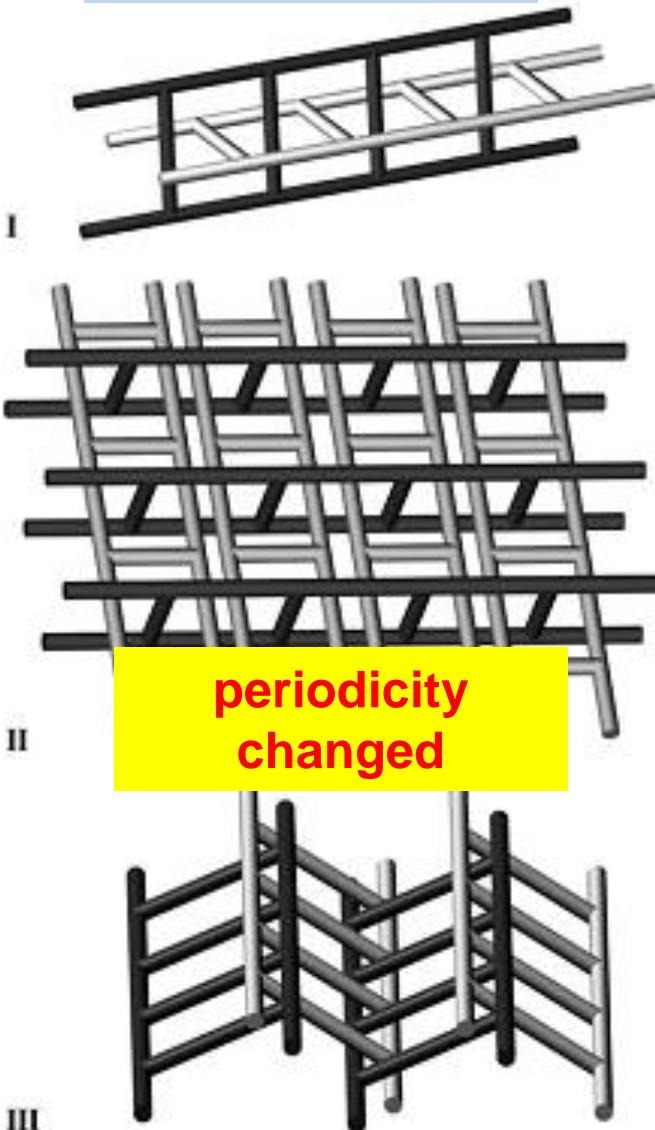
***1-p \Rightarrow 1-p
2-fold 2007***

***1-p \perp 1-p \Rightarrow 2-p
2004***

***1-p // 1-p \Rightarrow 2-p
1997***

**1-p
Ladders
+
Hopf
Links**

periodicity
unchanged



**1-p \Rightarrow 1-p
2-fold 2007**

**1-p \perp 1-p \Rightarrow 2-p
2004**

**1-p // 1-p \Rightarrow 2-p
1997**

Inextricable Entanglement via Hopf links

periodicity
unchanged

$1\text{-}p+1\text{-}p \Rightarrow 2\text{-}p/3\text{-}p$
 $2\text{-}p \text{ parallel} \Rightarrow 2\text{-}p$
 $2\text{-}p \text{ incline-}p \Rightarrow 3\text{-}p$
 $3\text{-}p \Rightarrow 3\text{-}p$

increase of
periodicity

Interpenetration

Polycatenation

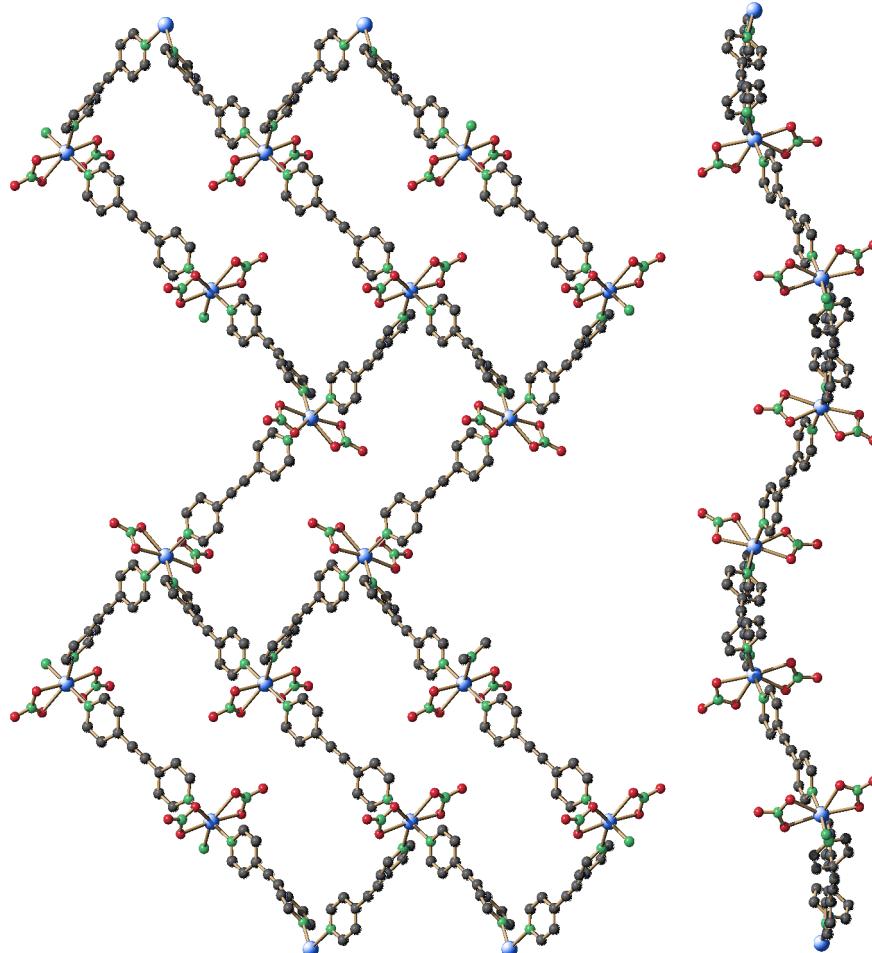
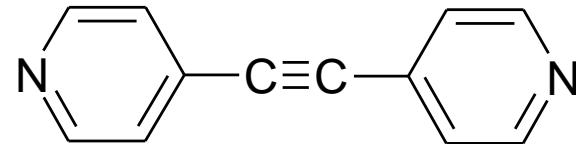
“Topological” Entanglement

$[\text{Cd}_2(\text{bpethy})_3](\text{NO}_3)_4$

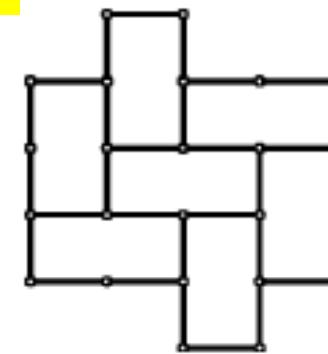
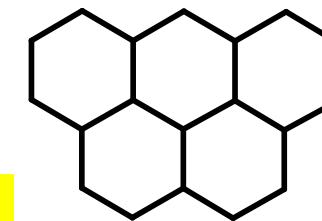
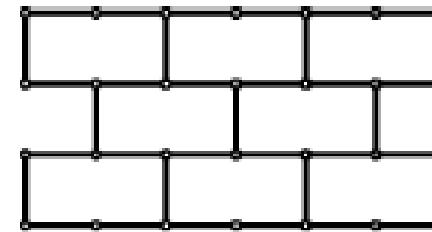
$2-p // 2-p \Rightarrow 2-p-3f$

DEKQOZ, DEKQUZ

Interpenetration



$6^3\text{-}hcb$

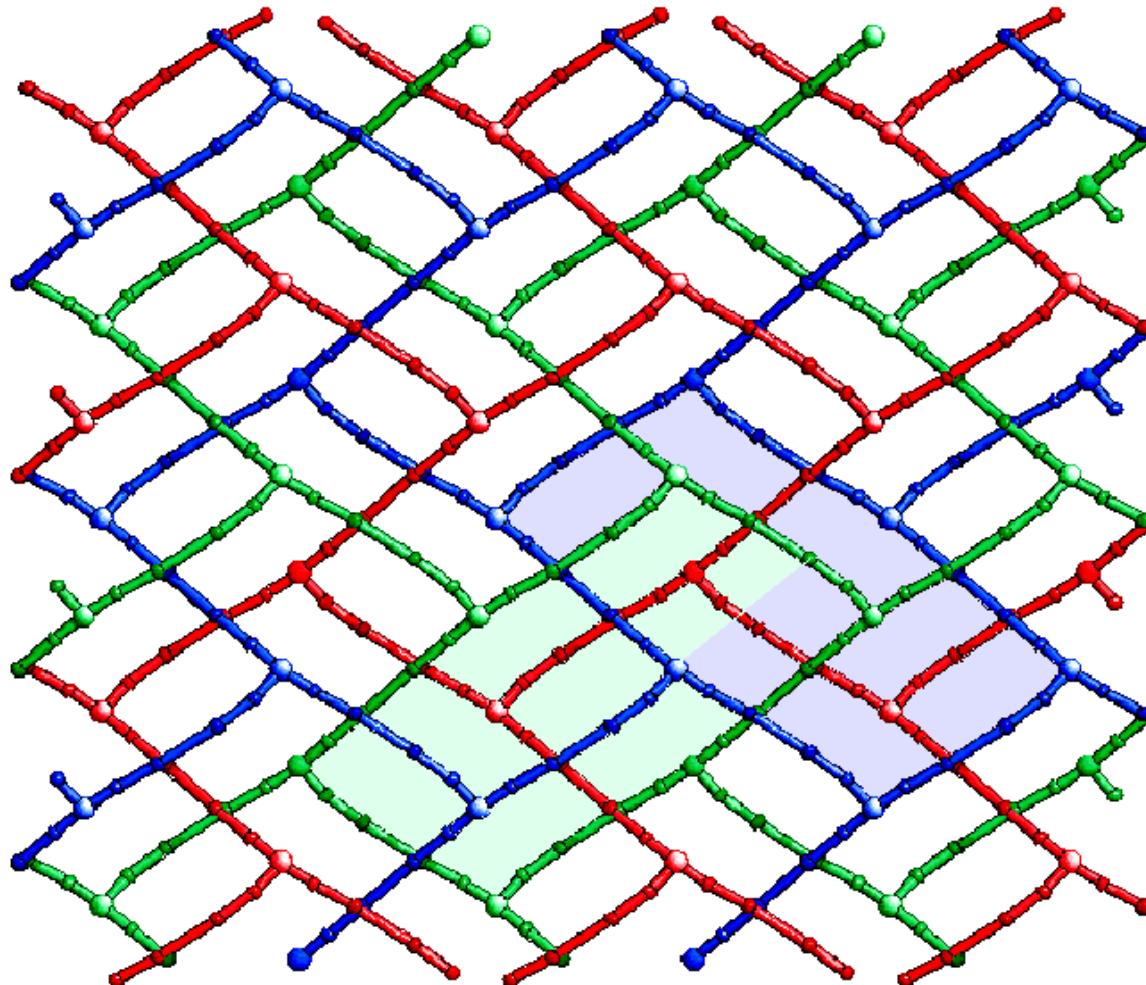
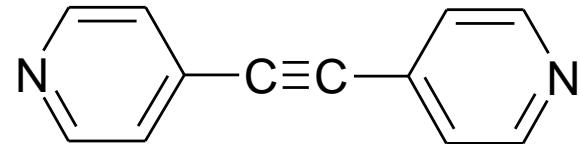


$[\text{Cd}_2(\text{bpethy})_3](\text{NO}_3)_4$

$2-p // 2-p \Rightarrow 2-p-3f$

DEKQOZ, DEKQUZ

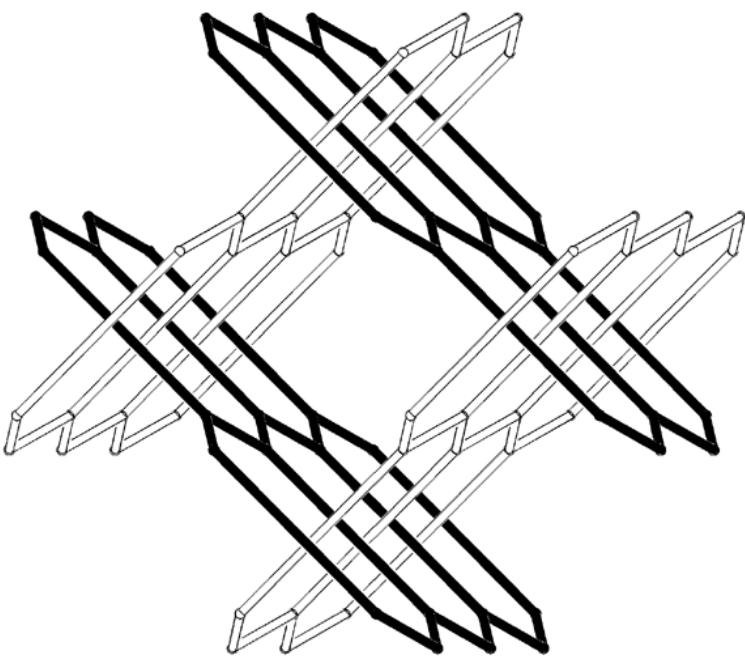
Interpenetration



'inclined' polycatenation $2\text{-}p \perp 2\text{-}p \Rightarrow 3\text{-}p$

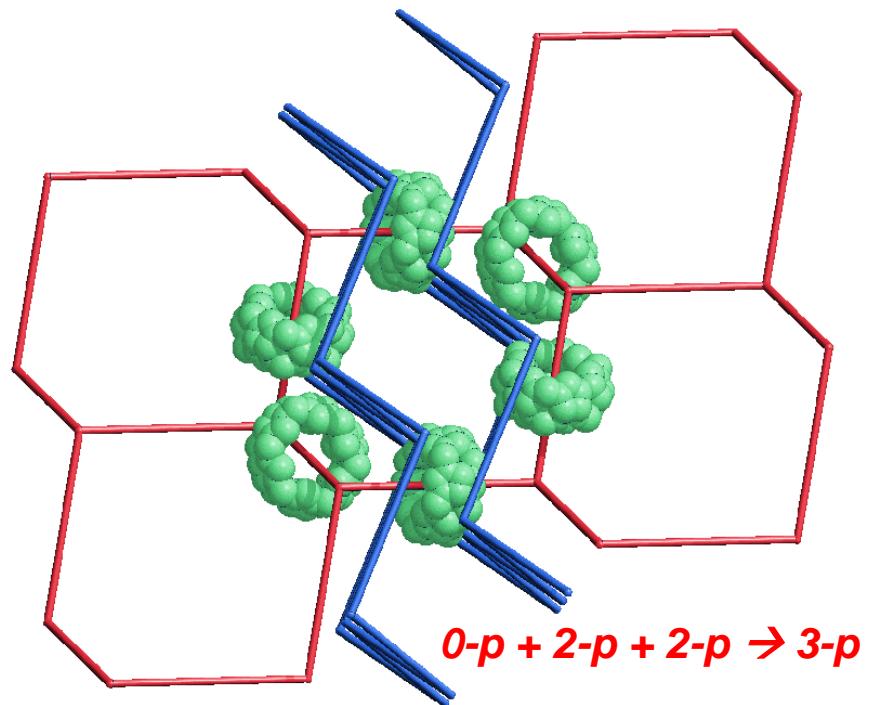
$[\text{Cu}_2(\text{pyz})_3](\text{SiF}_6)$

Zaworotko group, 1994



$[\text{Ag}_2(\text{H}_2\text{L})_3(\text{cucurbituril})_3](\text{NO}_3)_8$

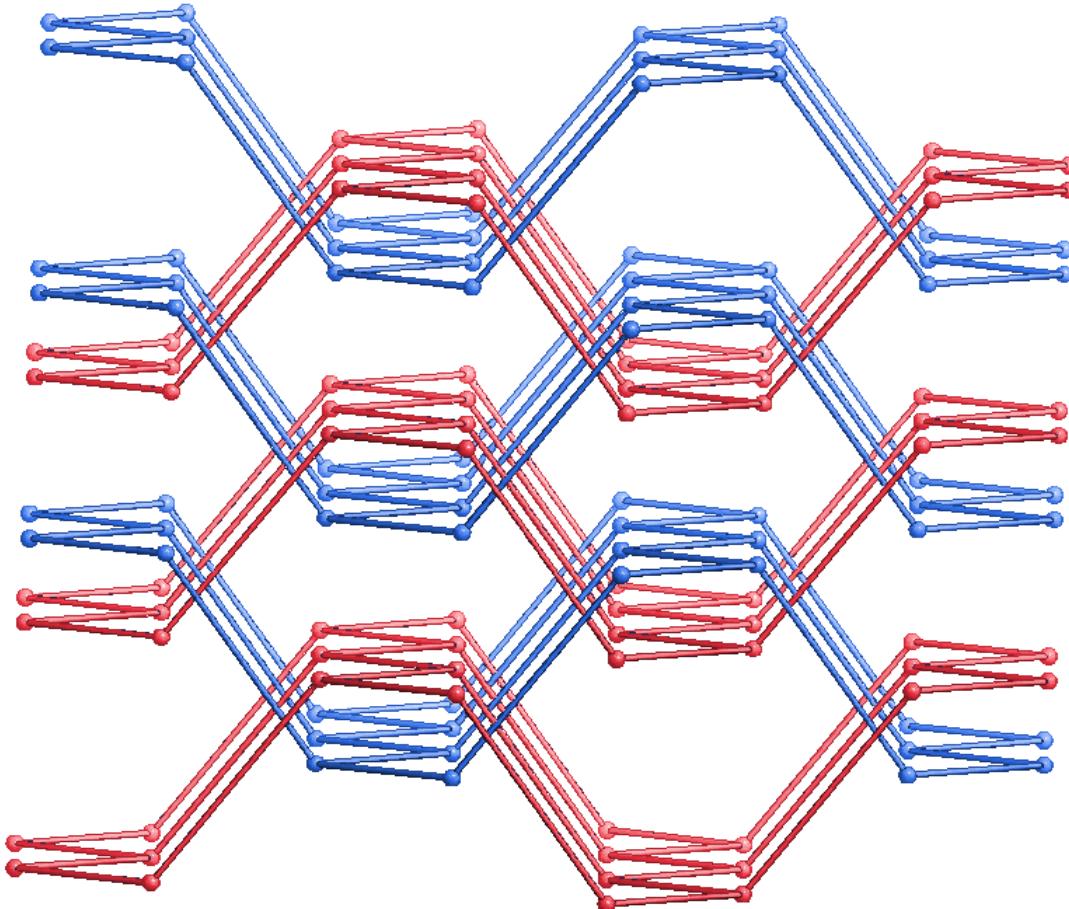
K. Kim group, 1997



hexagonal (6^3) layers, hcb

2D 'parallel' polycatenation
3-p // 3-p \Rightarrow 3-p

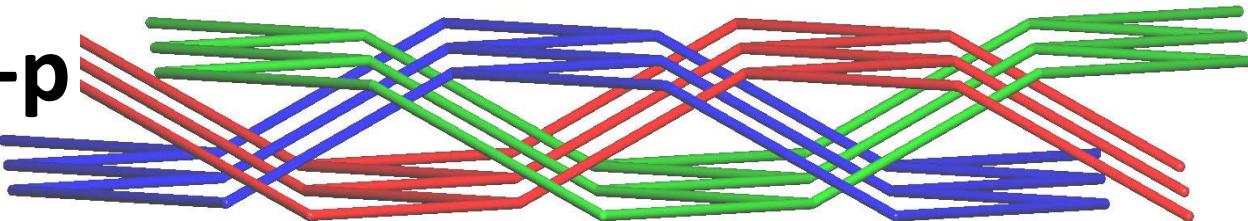
[Cu(bpethe)_{1.5}(PPh₃)](PF₆)
S.W. Keller group, 2001



SCHAKAL

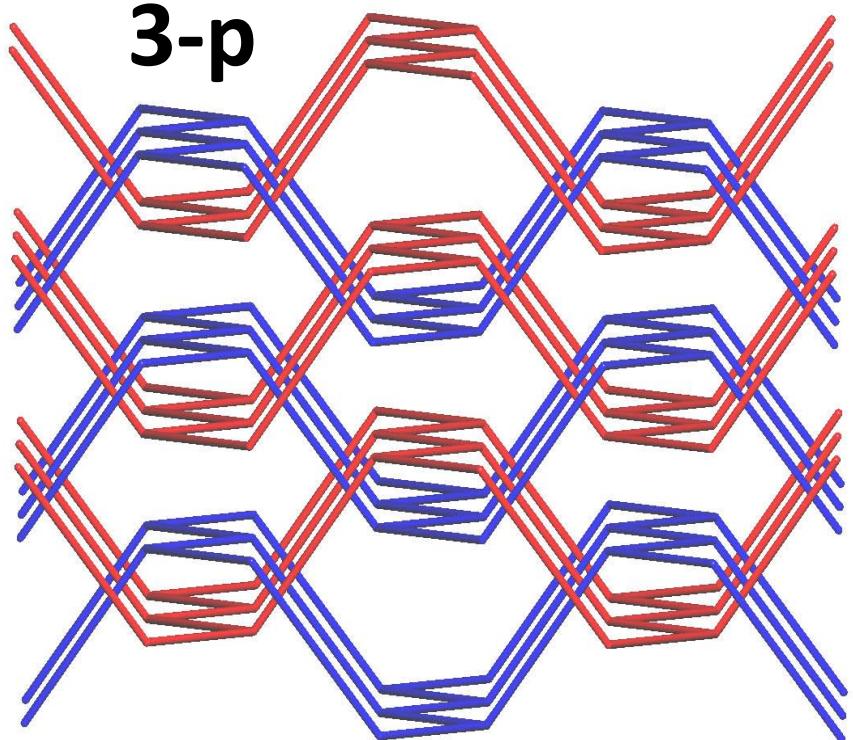
undulated hexagonal (6³) layers

2-p + 2-p → 2-p



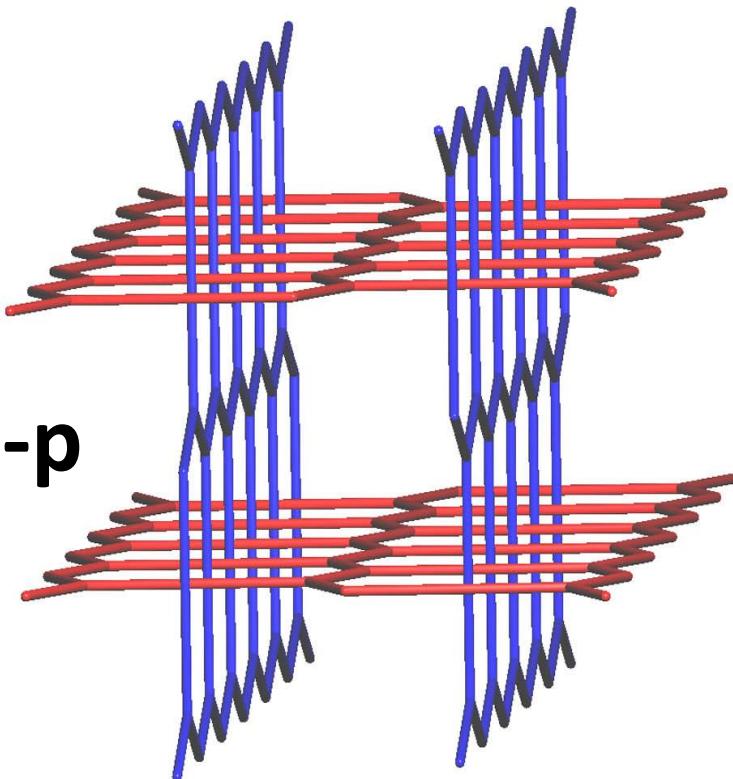
interpenetrated 3-fold

3-p



polycatenated parallel

3-p



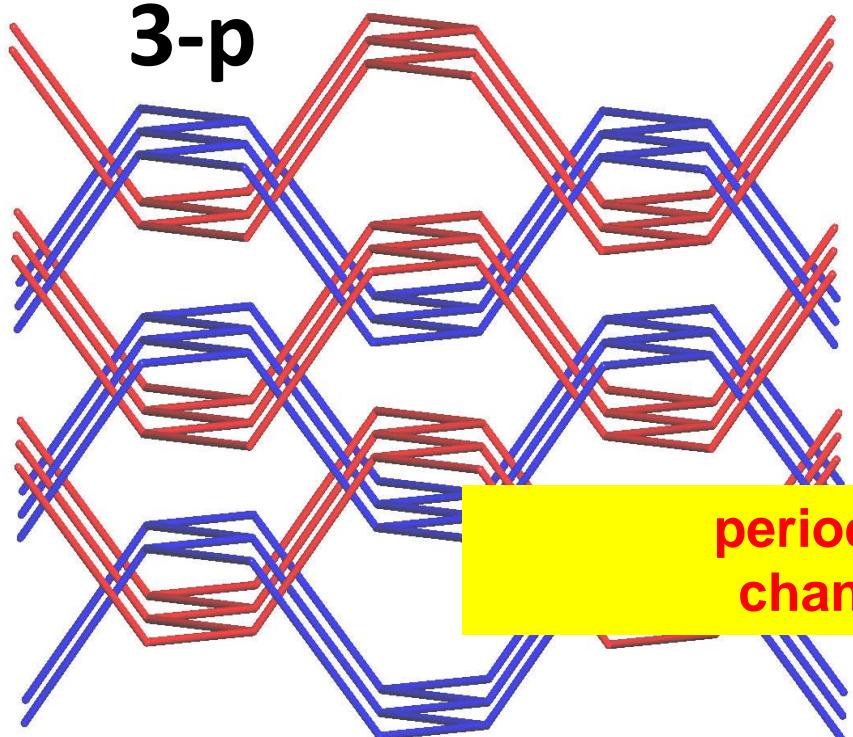
polycatenated inclined

2-p + 2-p → 2-p



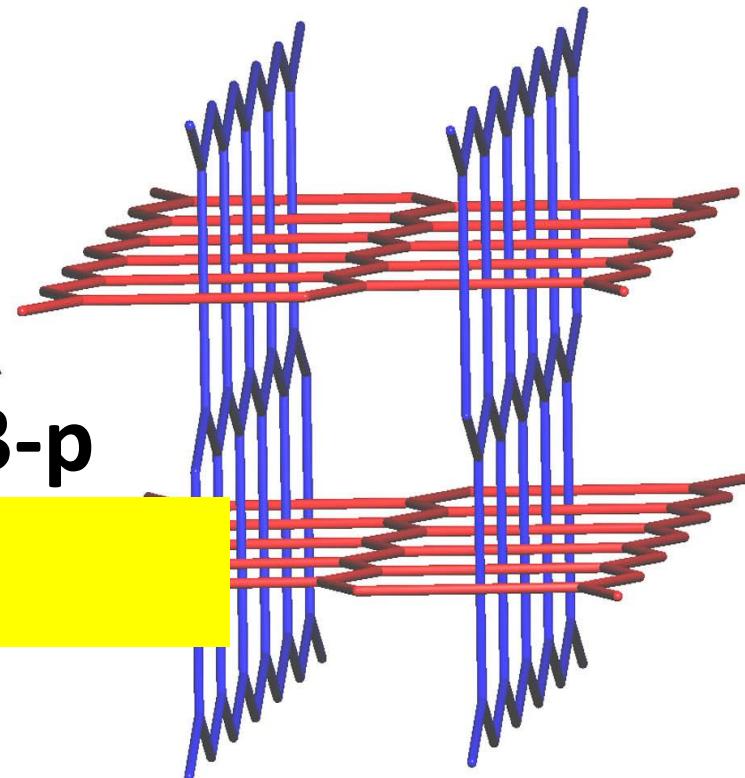
interpenetrated 3-fold

3-p



polycatenated parallel

3-p



polycatenated inclined

**periodicity
unchanged**

**periodicity
changed**

Inextricable Entanglement via Hopf links

periodicity unchanged:

INTERPENETRATION

$$\begin{aligned}0-p + 0-p &\Rightarrow 0-p \\1-p + 1-p &\Rightarrow 1-p \\2-p + 2-p \text{ (parallel)} &\Rightarrow 2-p \\3-p + 3-p &\Rightarrow 3-p\end{aligned}$$

Only 4 possibilities



components 0-p, 1-p, 2-p or 3-p

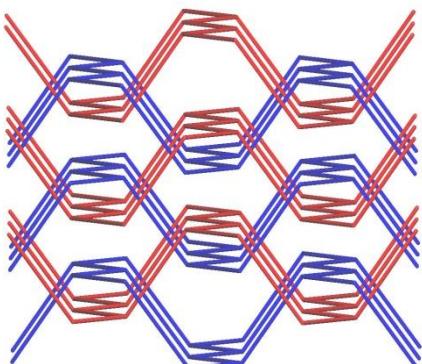
the whole has the SAME periodicity of the components

the number of entangled components is finite (**n-fold**)

each component is interlaced with ALL the others (*)

the whole is an infinite k -periodic architecture

$$\begin{aligned}k-p + k-p &\Rightarrow k-p \\m-p + n-p &\Rightarrow k-p \\m < k; n \leq k\end{aligned}$$



increase of periodicity:

POLYCATION

$$\begin{aligned}0-p + 0-p &\Rightarrow 1-p, 2-p \text{ or } 3-p \\0-p + 1-p &\Rightarrow 1-p, 2-p \text{ or } 3-p \\0-p + 2-p &\Rightarrow 2-p \text{ or } 3-p \\0-p + 3-p &\Rightarrow 3-p \\1-p + 1-p &\Rightarrow 2-p \text{ or } 3-p \\1-p + 2-p &\Rightarrow 2-p \text{ or } 3-p \\1-p + 3-p &\Rightarrow 3-p \\2-p + 2-p \text{ (inclined)} &\Rightarrow 3-p \\2-p + 2-p \text{ (parallel)} &\Rightarrow 3-p \\2-p + 3-p &\Rightarrow 3-p\end{aligned}$$

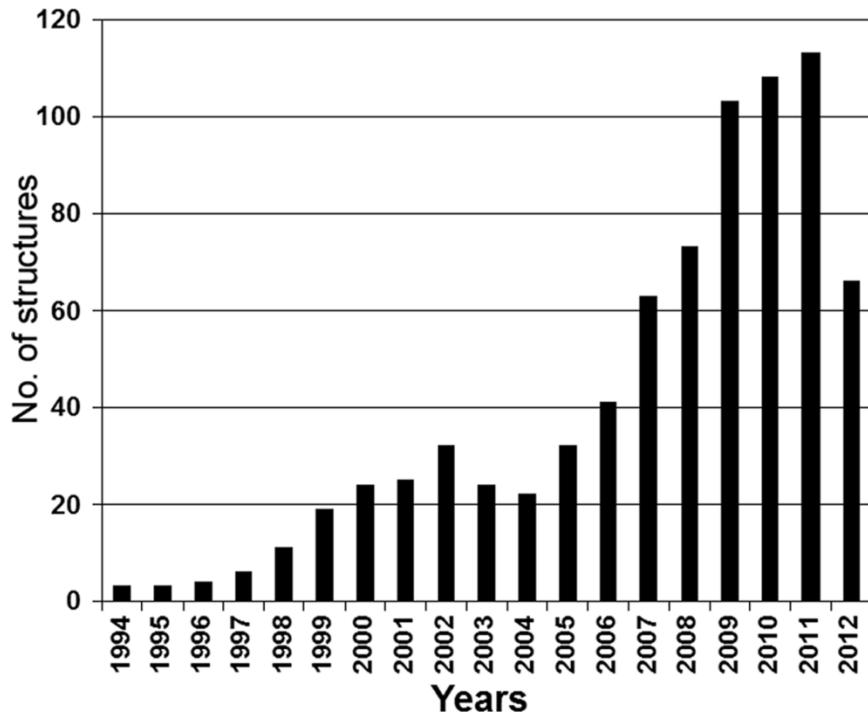
components 0-p, 1-p, 2-p or 3-p

the whole has HIGHER periodicity of at least one component

the number of entangled components is infinite

at least one component is not interlaced with all the others

2-periodic coordination networks

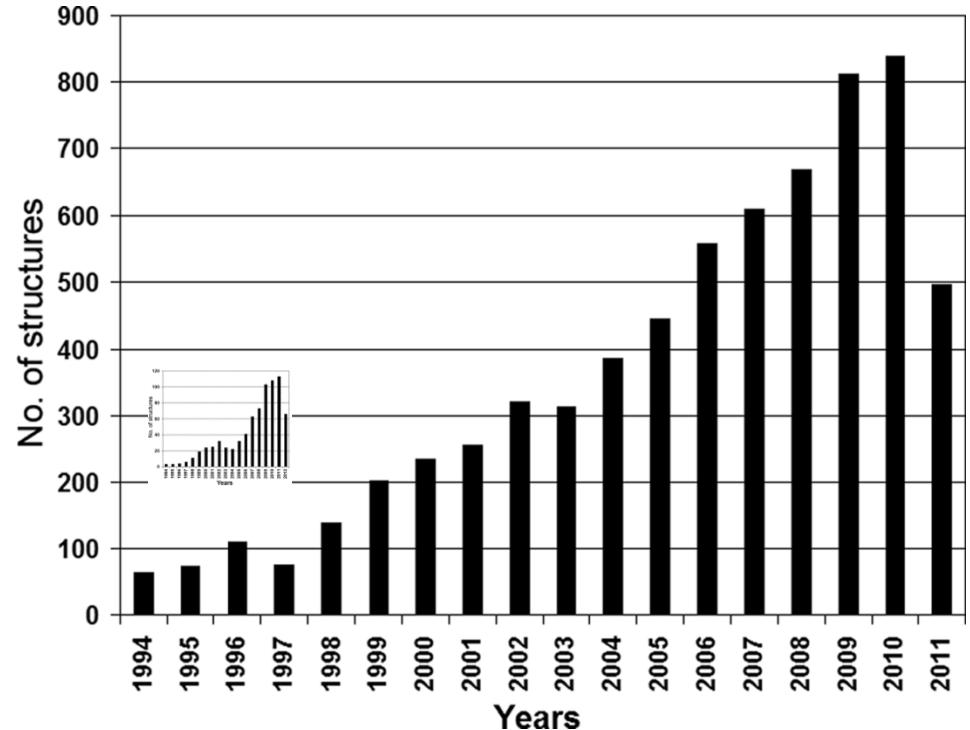


entangled

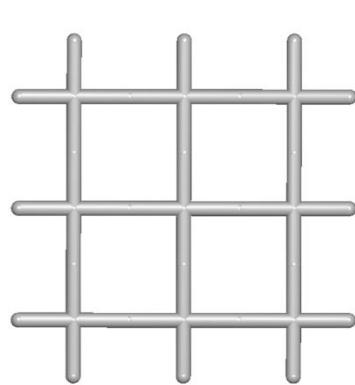
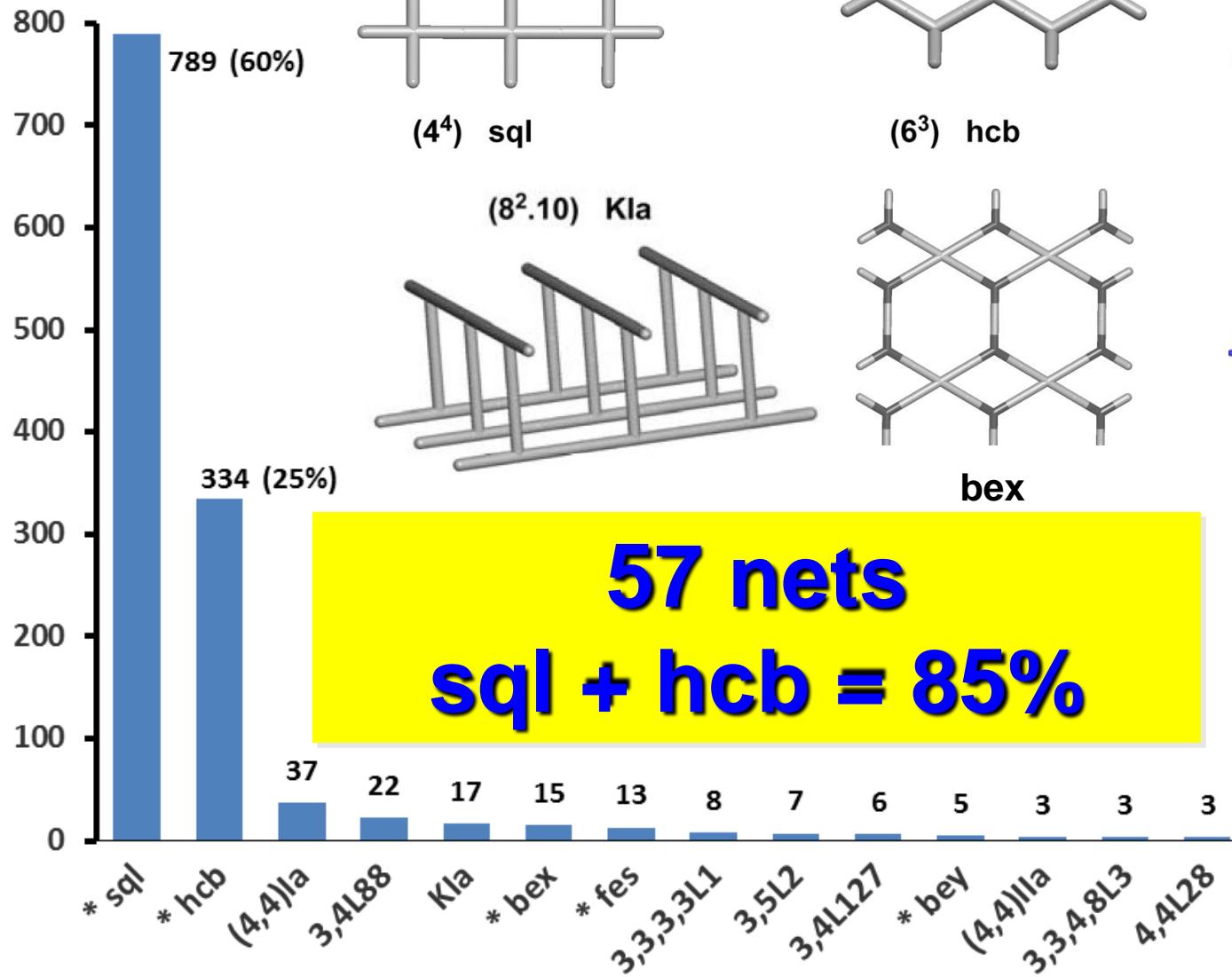
1319

vs.
1/9

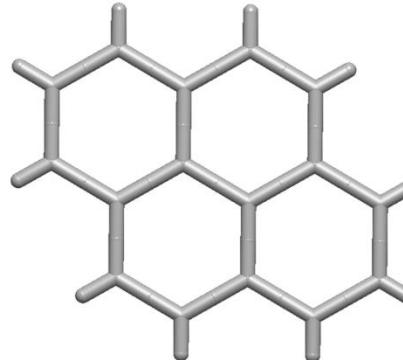
single



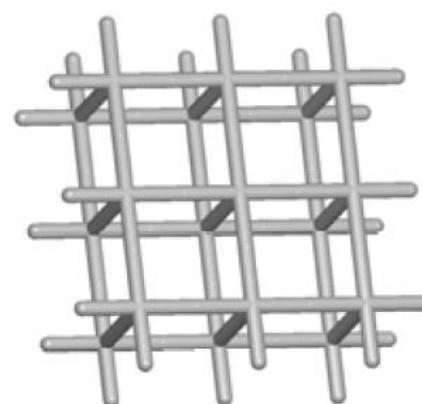
1319



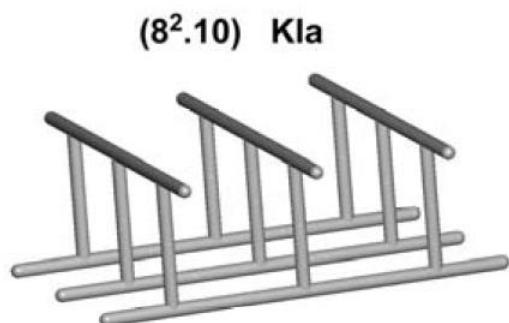
(4^4) sql



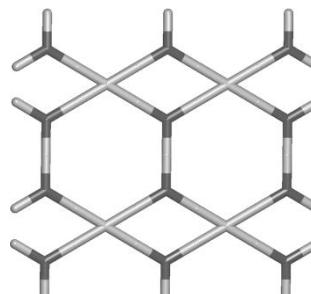
(6^3) hcb



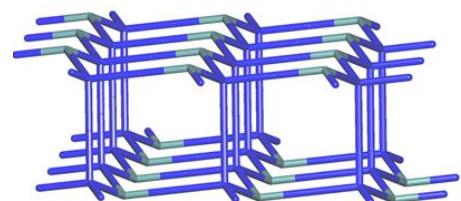
$(4^4.6^2)$ (4,4)la



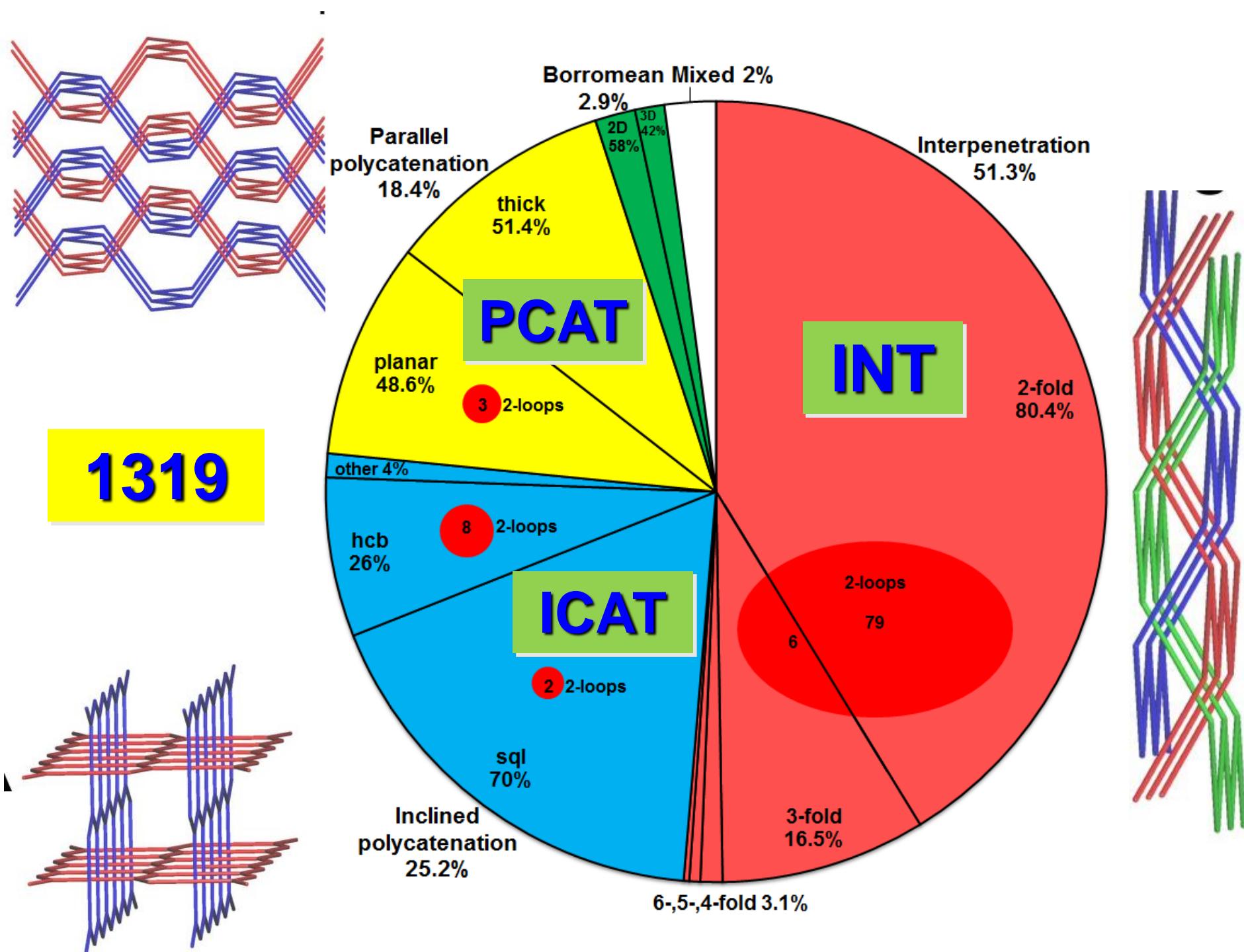
$(8^2.10)$ Kla



bex



3,4L88



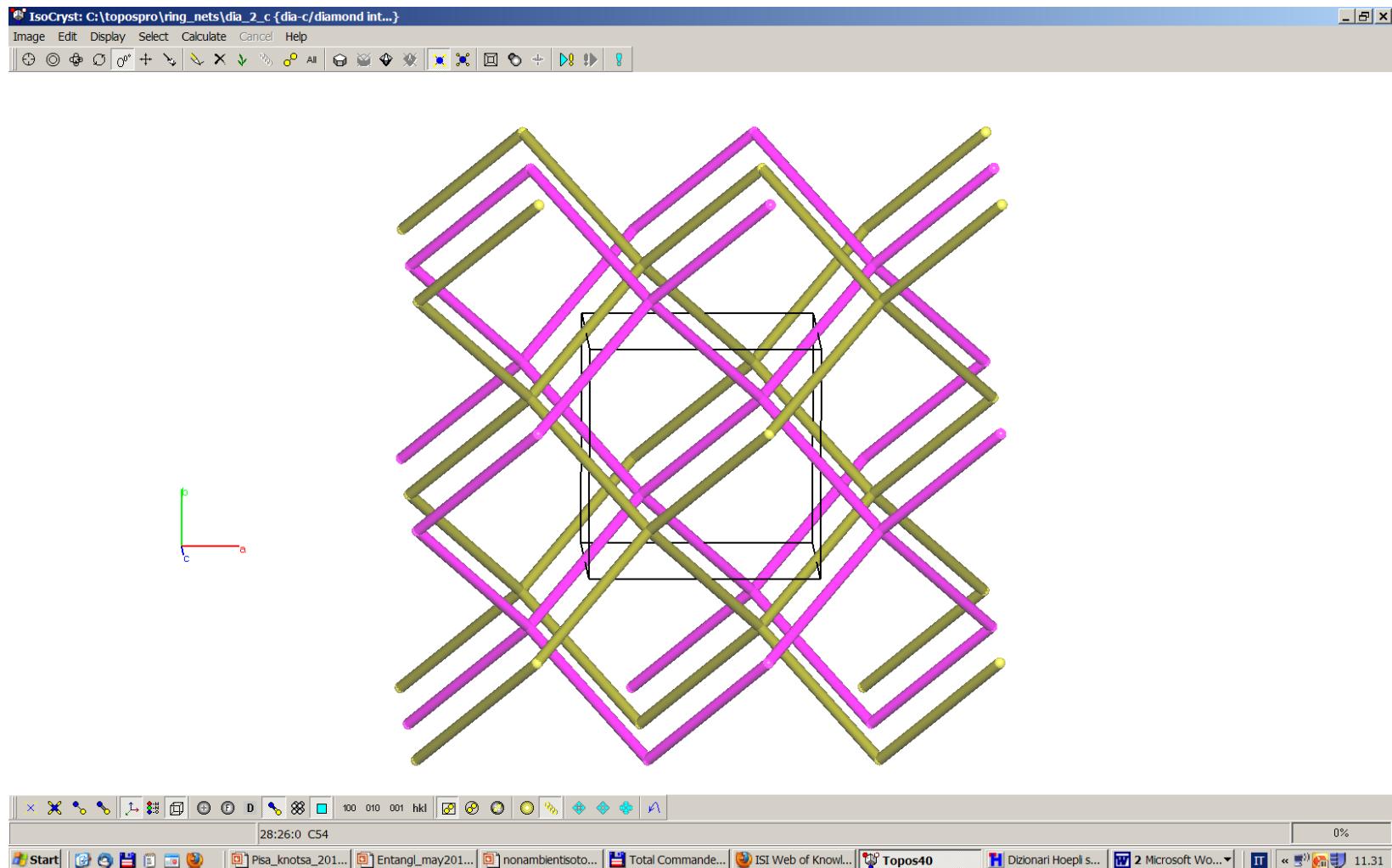
... and now a natural question:

Are these classes topologically related?

i.e. can we deform one member of a class into a member of another class?

For instance we know many examples of diamondoid coordination network that are 2-fold interpenetrated....

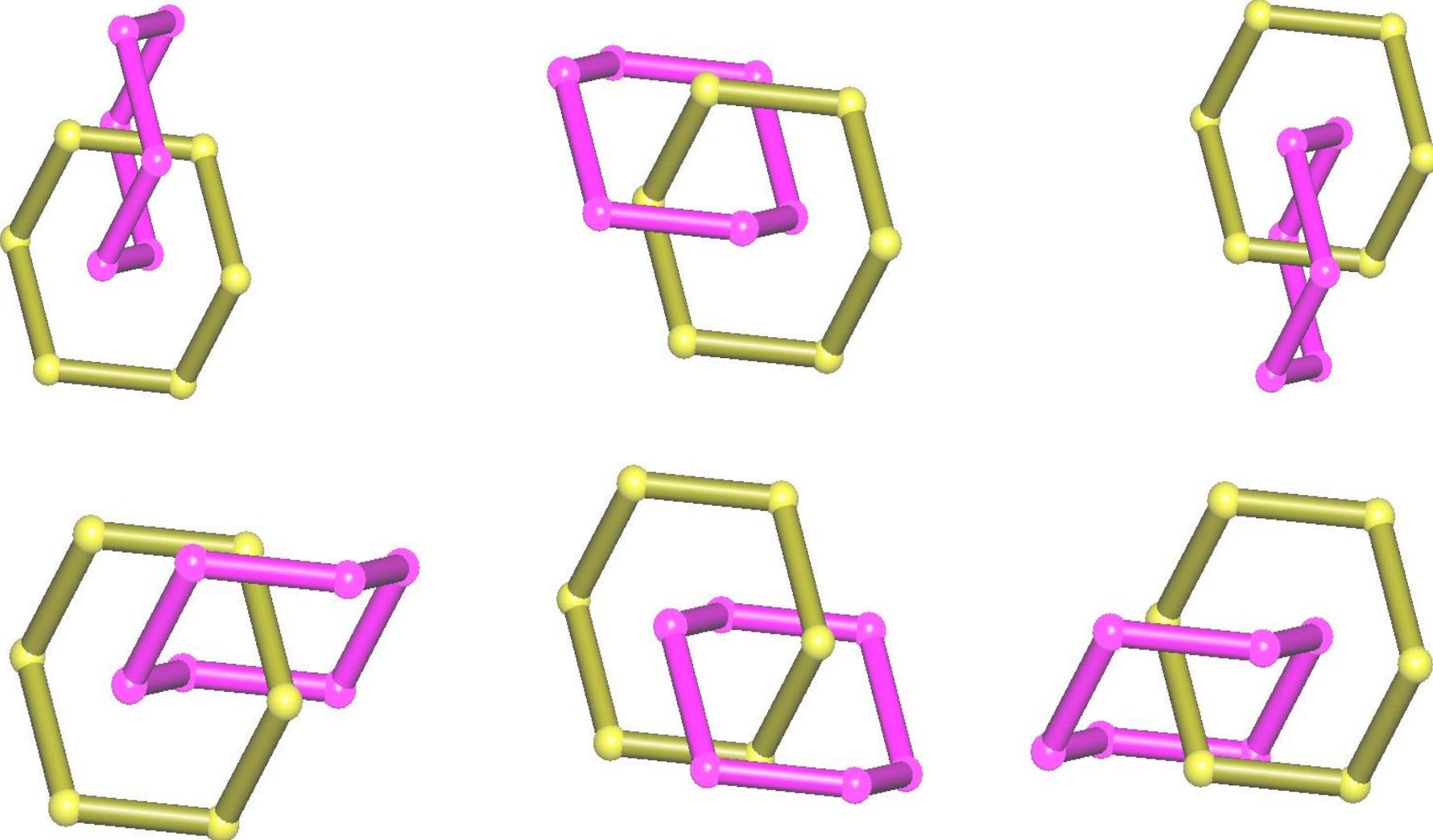
How many are topologically distinct?



Ring links

Cycle 1 | Cycle 2 | Chain | Cross | Link | Hopf | Mult

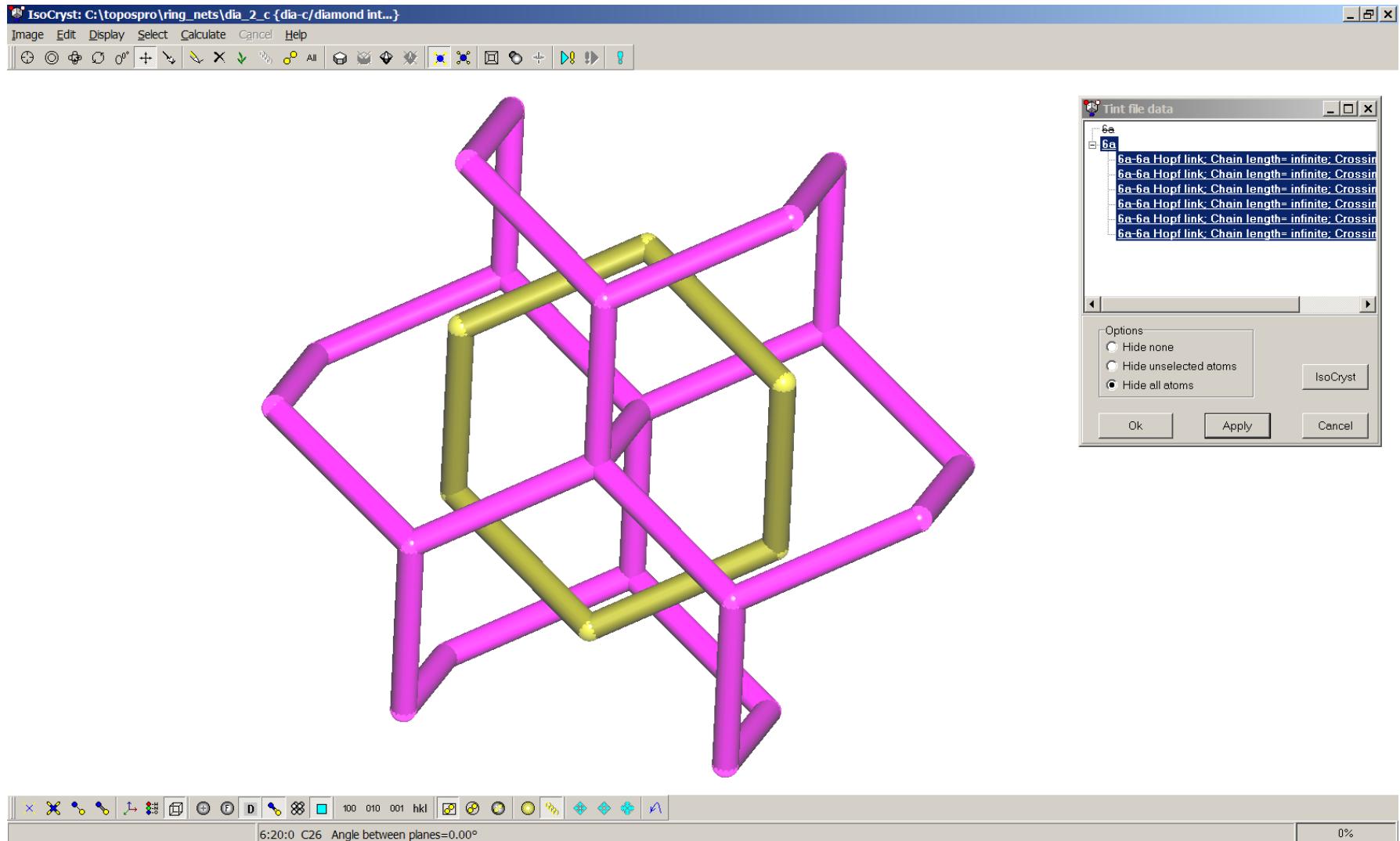
6a | 6a | inf. | 1 | 1 | * | 6

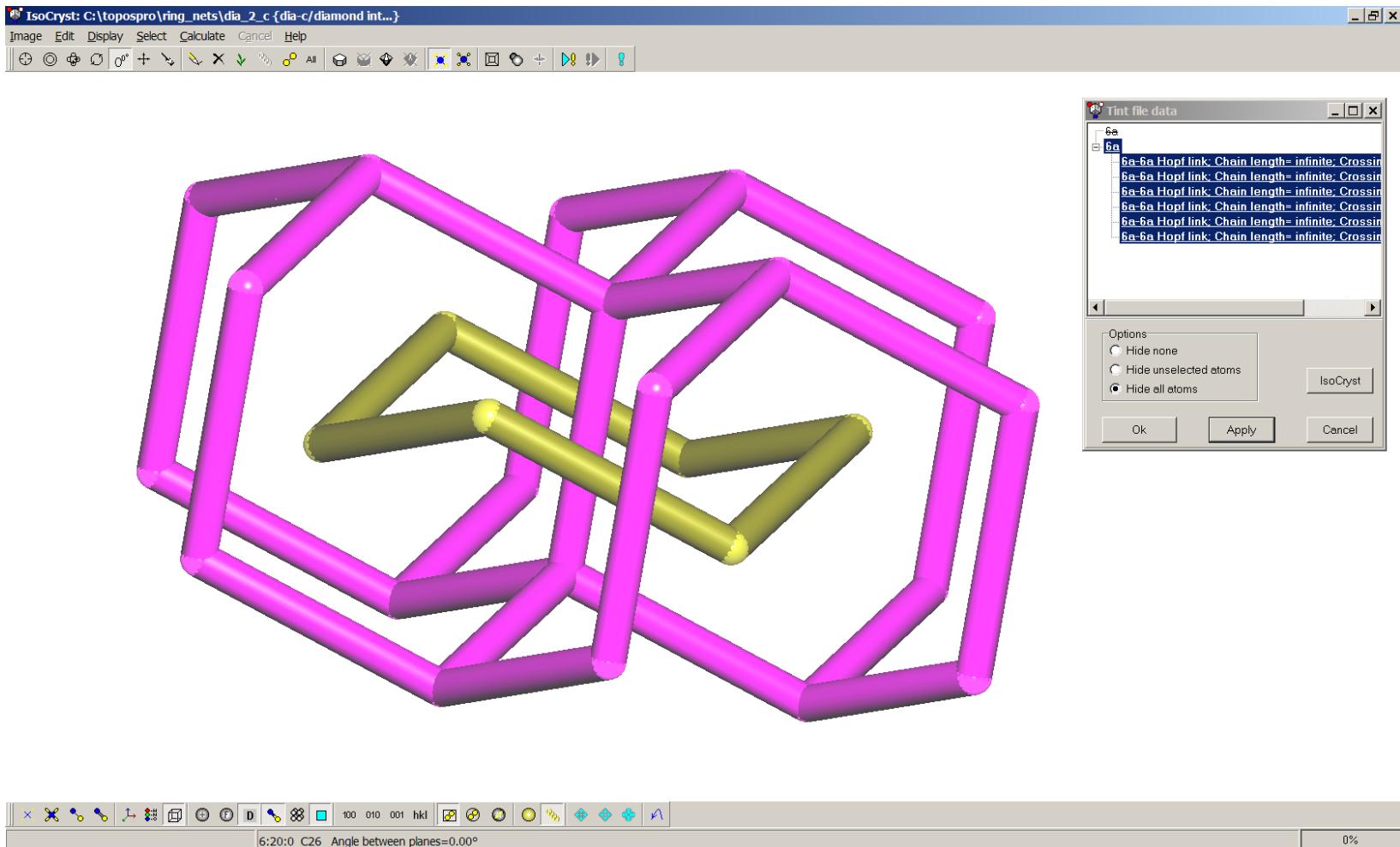


Ring links

Cycle 1 | Cycle 2 | Chain | Cross | Link | Hopf | Mult

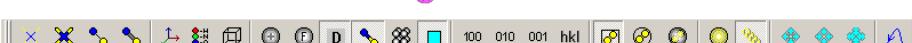
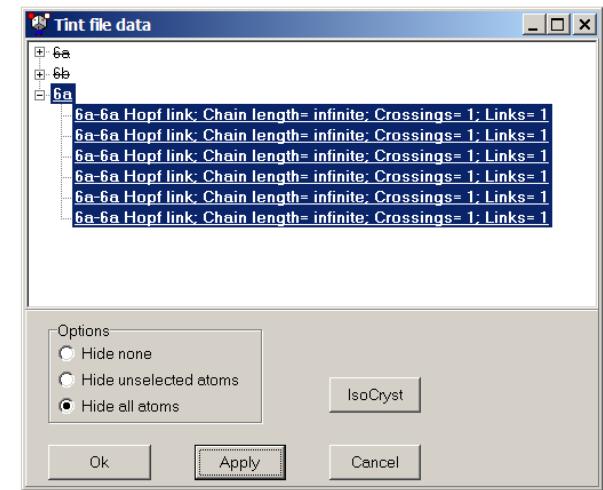
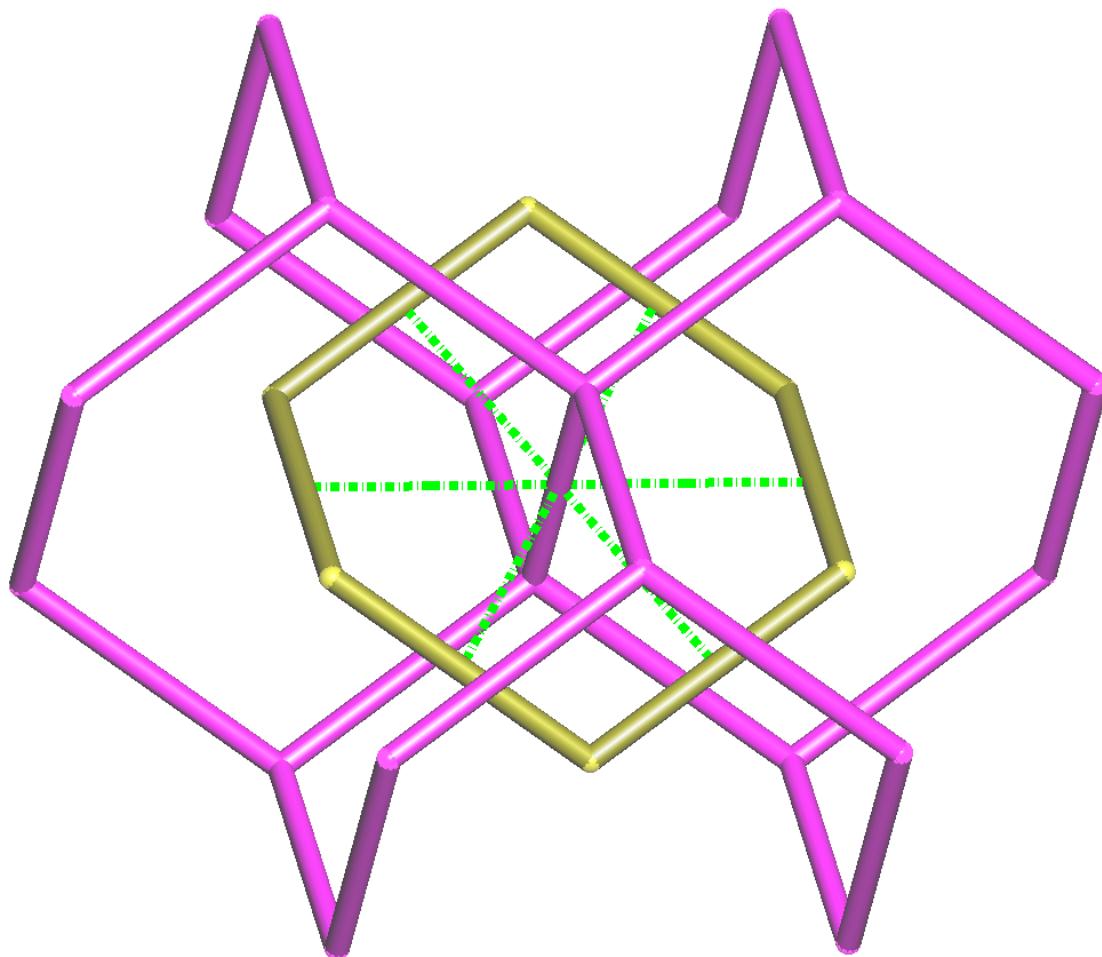
6a | 6a | inf. | 1 | 1 | * | 6





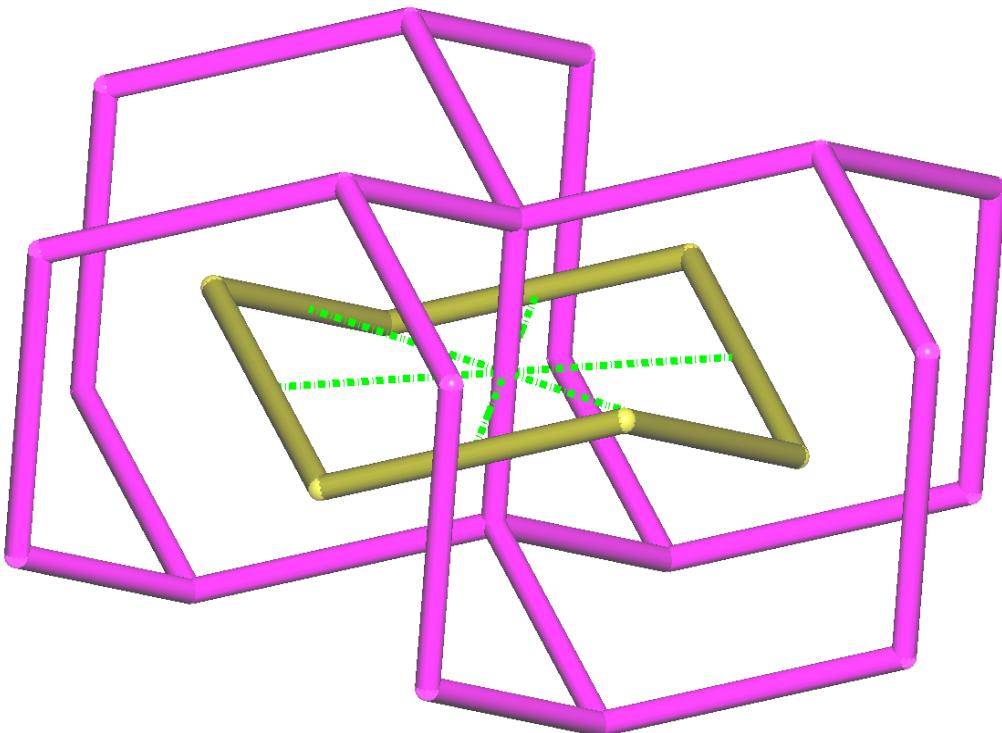
IsoCryst: C:\topospro\ring_nets\dia_2_c_c {dia-c/diamond int...}

Image Edit Display Select Calculate Cancel Help



6:20:0 C26 Angle between planes=0.00°

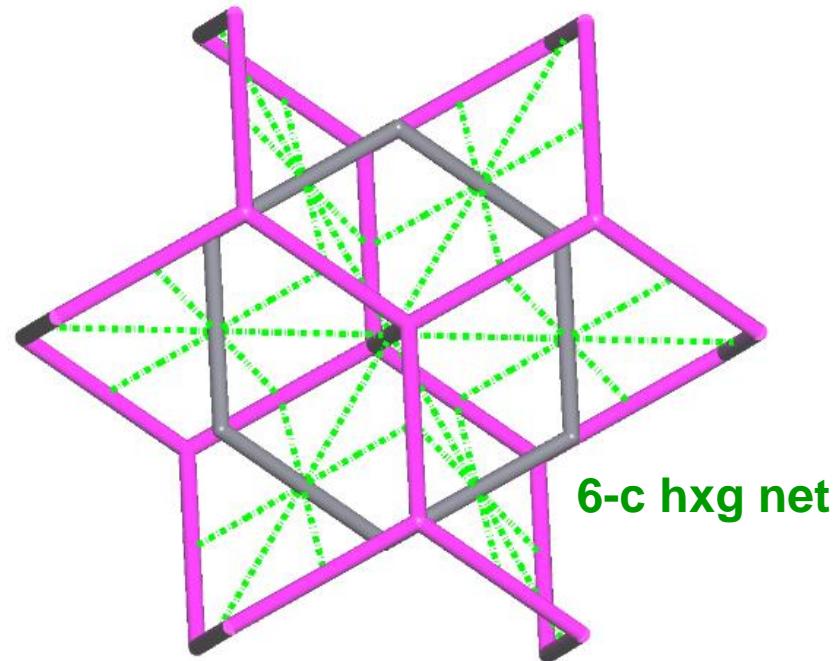
0%



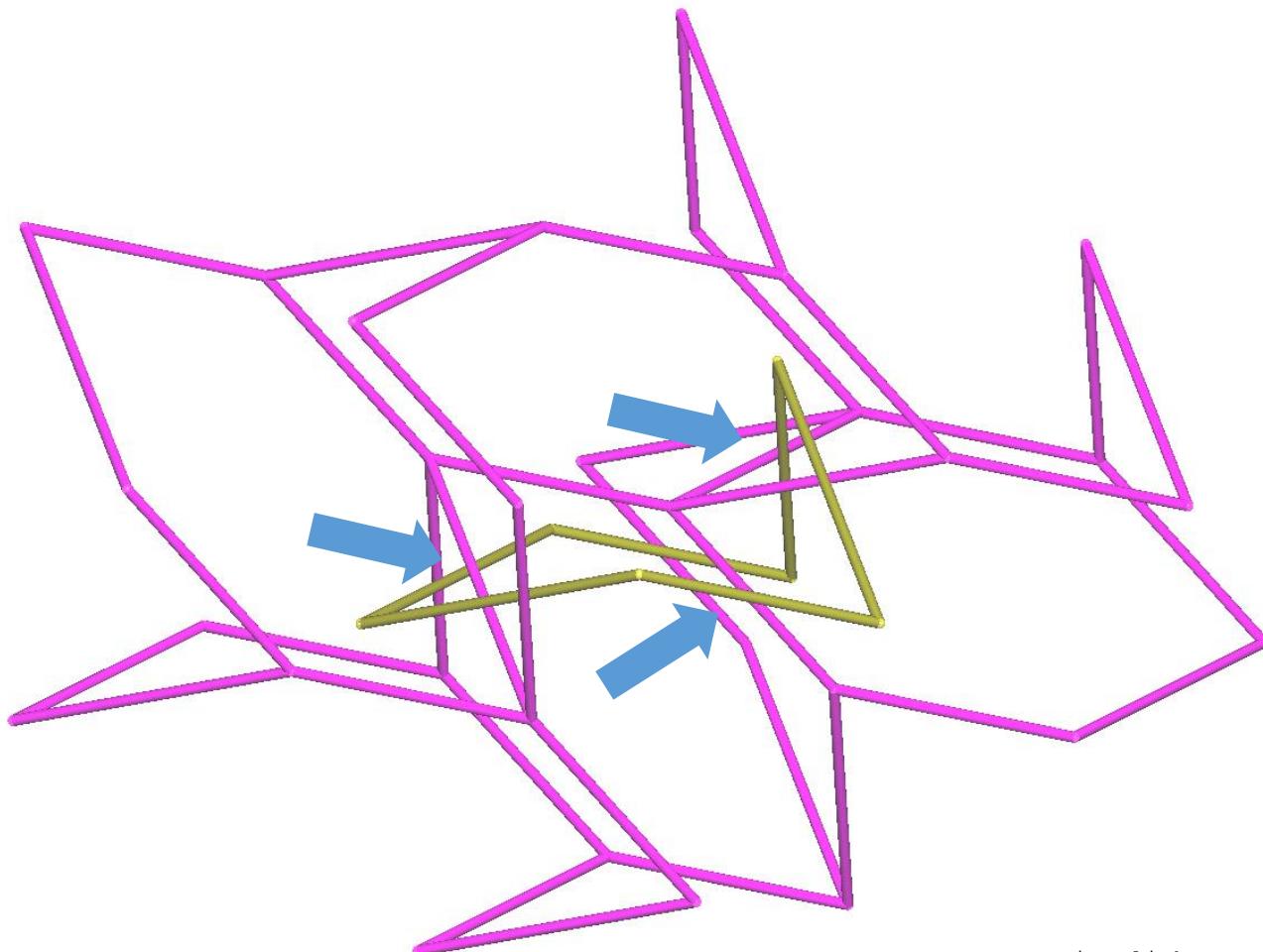
The resulting single net (green dotted lines) represent the “net-of-catenated-links” **Hopf Ring Net HRN** and is independent of the symmetry/space group.

Q: dia 2fold class Ia can be transformed to class IIa ??

**A: YES, for all known cases!
only one example is different**



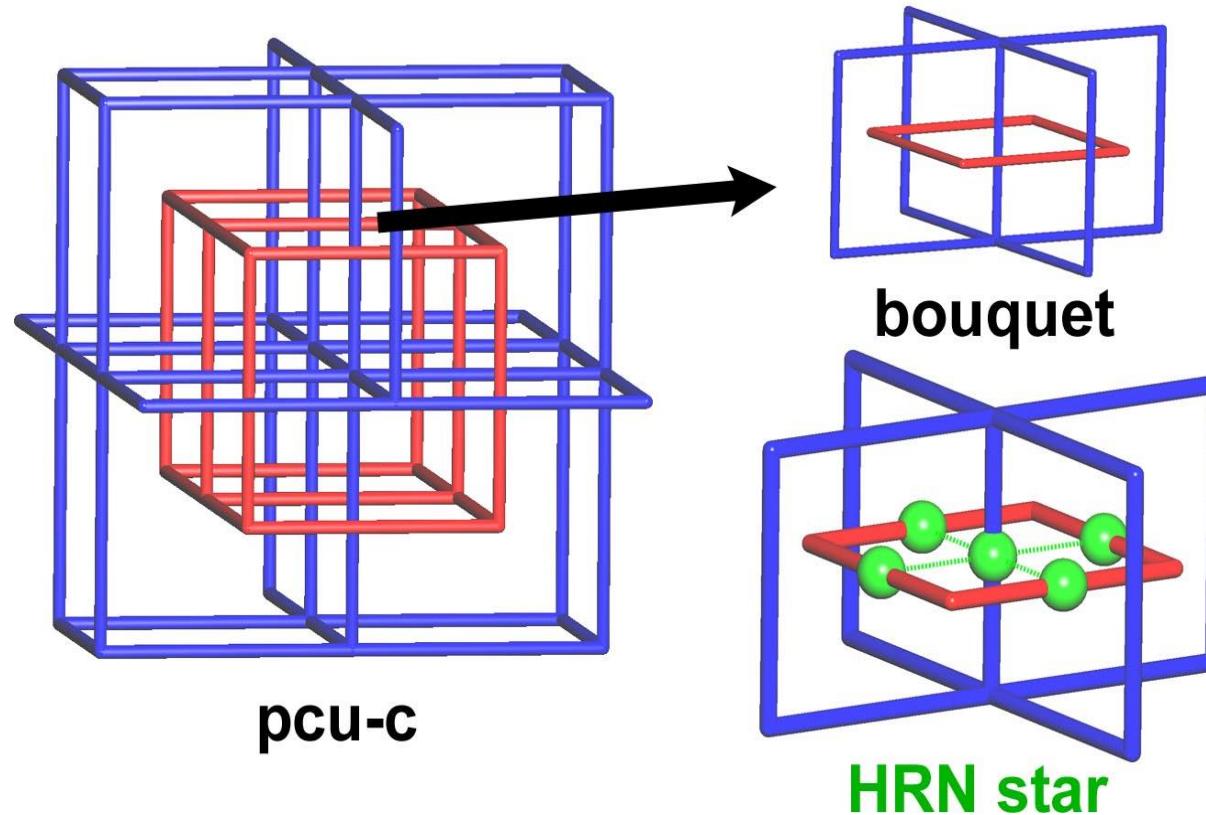
... and the difference for is due to extra crossings : 3 vs. 1



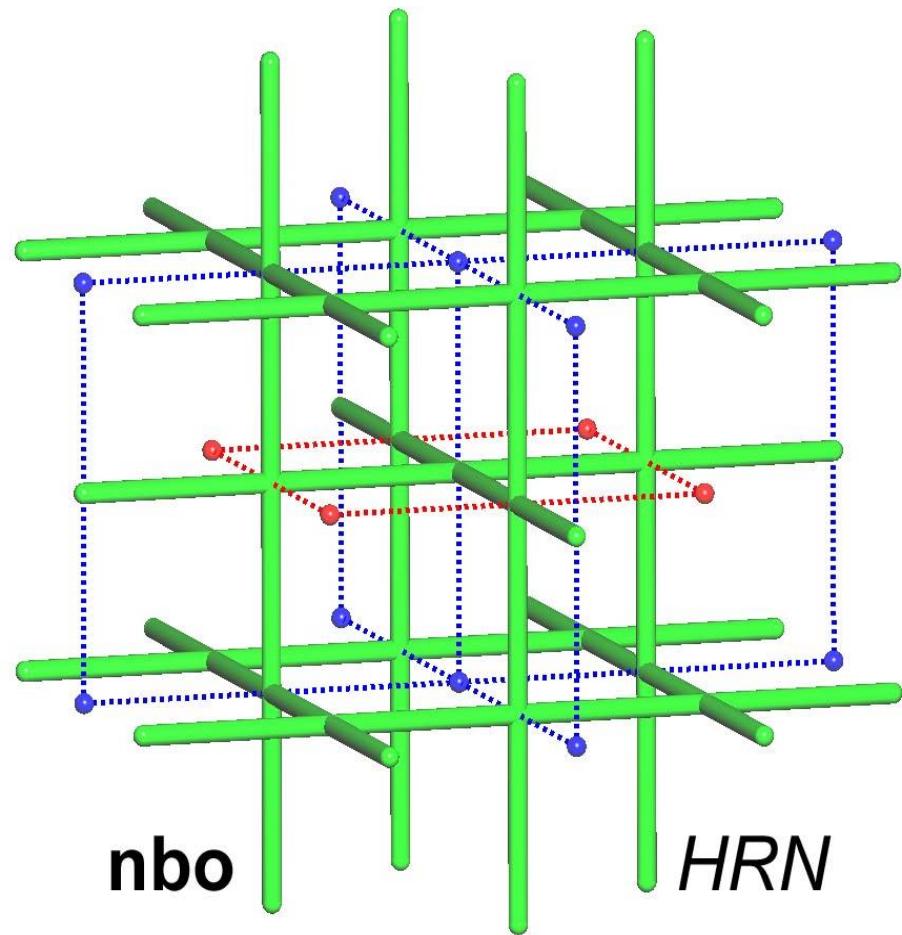
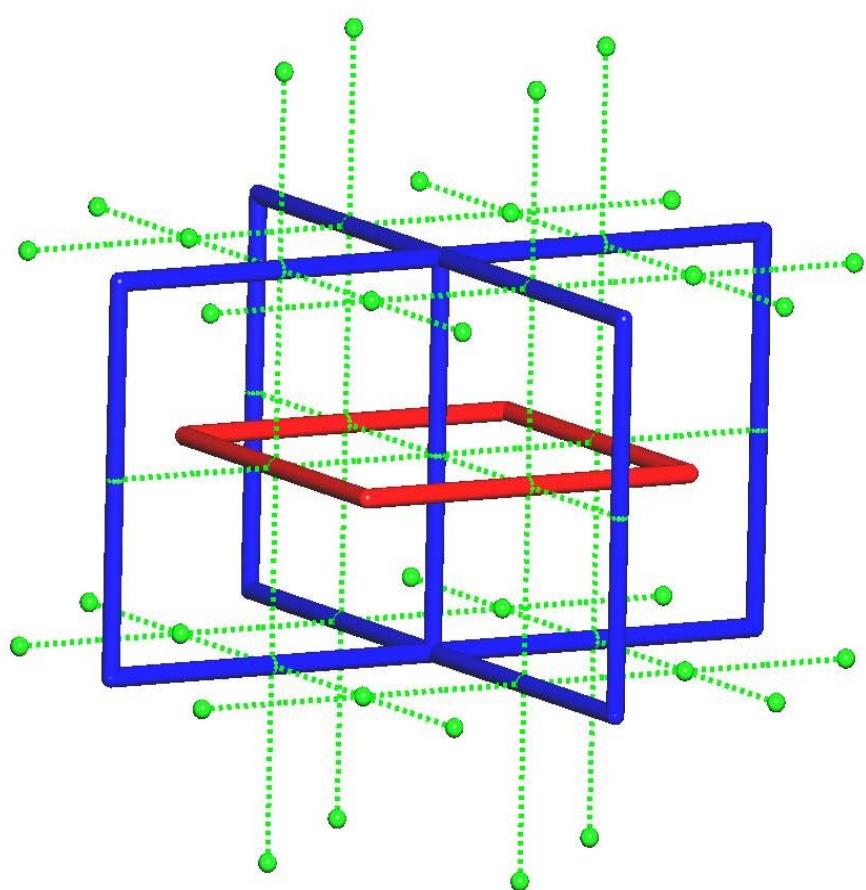
Cycle 1		Cycle 2		Chain		Cross		Link		Hopf		Mult
6a		6a		inf.		1		1		*		2
6a		6b		inf.		1		1		*		4
6b		6a		inf.		1		1		*		4
6b		6b		inf.		1		1		*		6

A topological method for the classification of entanglements in crystal networks¹

Eugen V. Alexandrov,^a Vladislav A. Blatov^{a*} and Davide M. Proserpio^{b*}



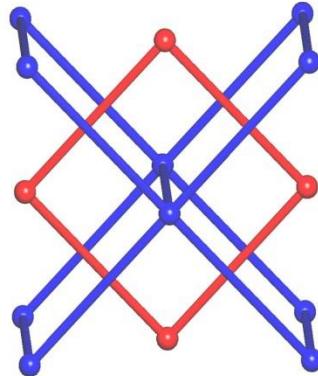
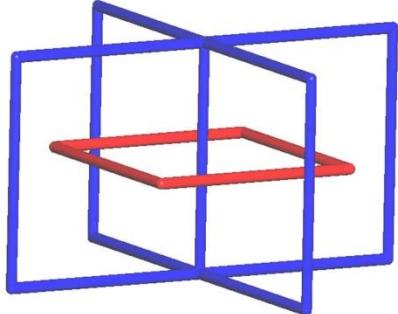
Pattern of catenation = HRN = Hopf ring net...



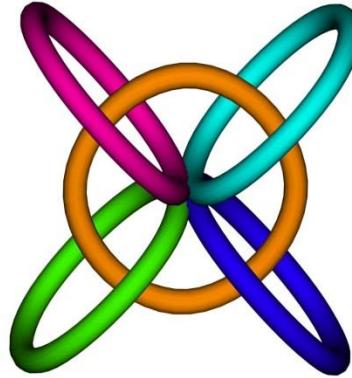
nbo

HRN

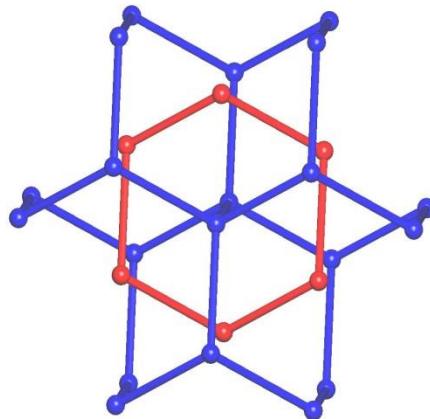
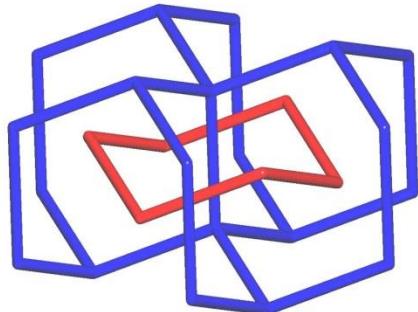
*... that is the **nbo** net.*



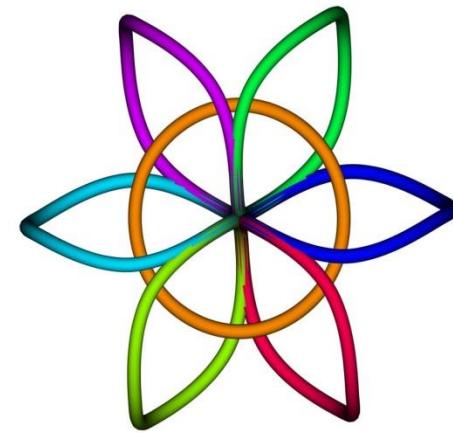
2 fold pcu = pcu-c



4-coor nbo



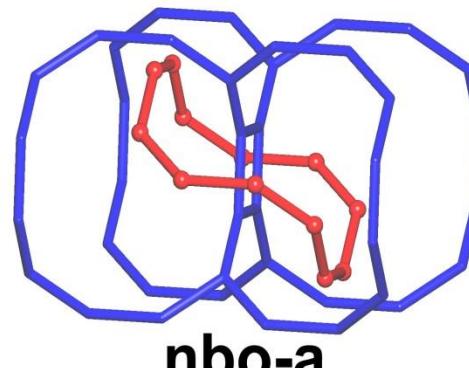
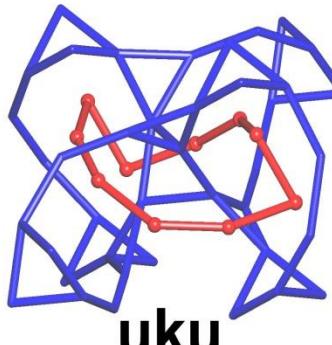
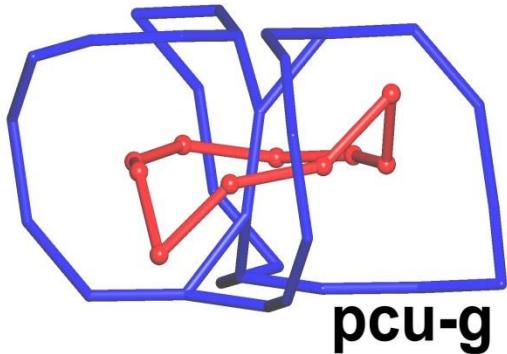
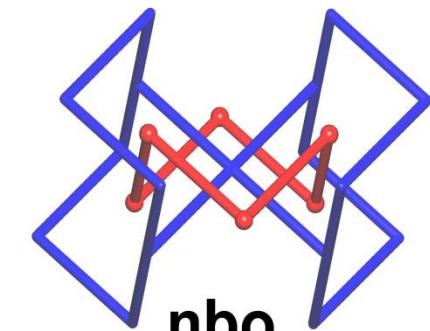
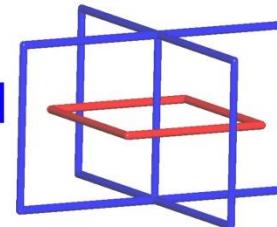
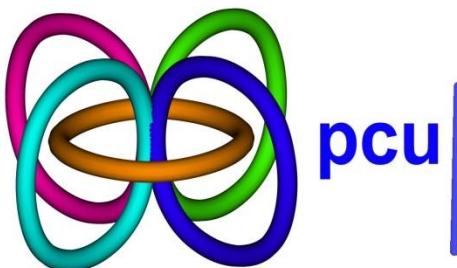
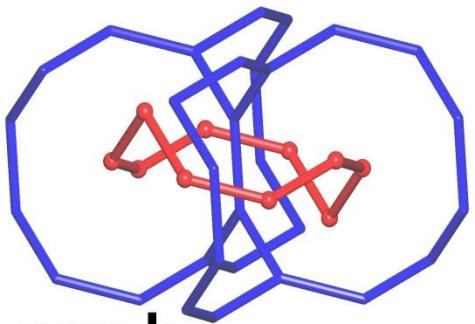
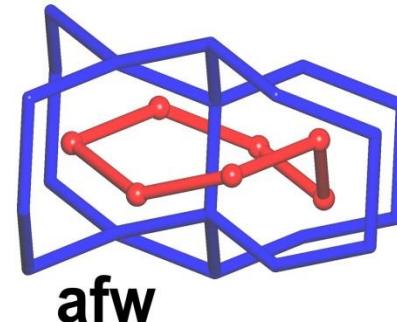
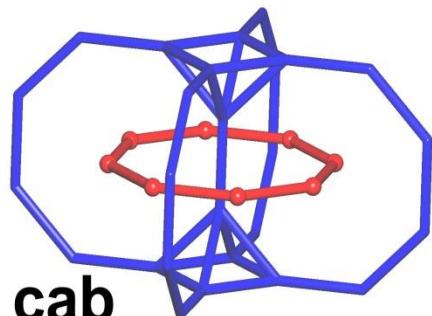
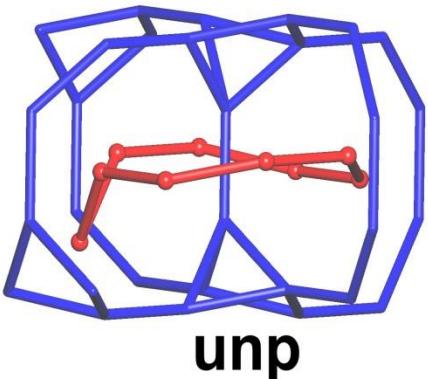
2 fold dia = dia-c

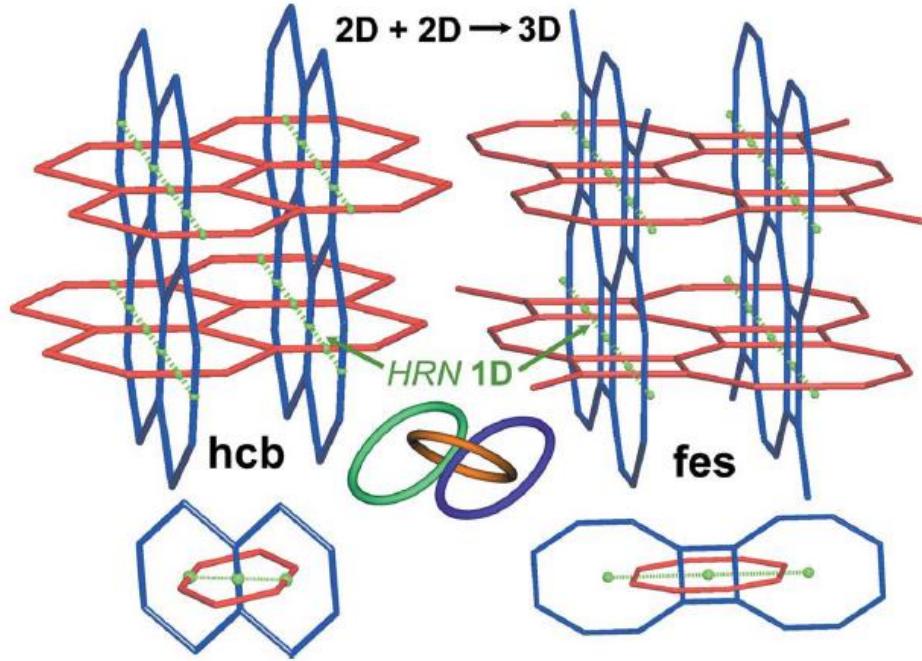
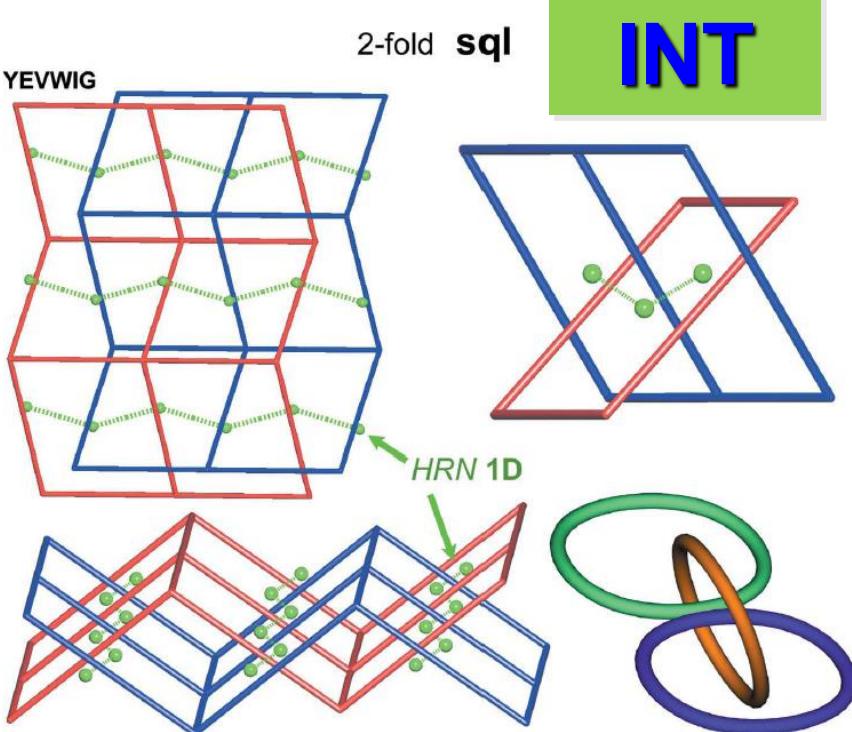
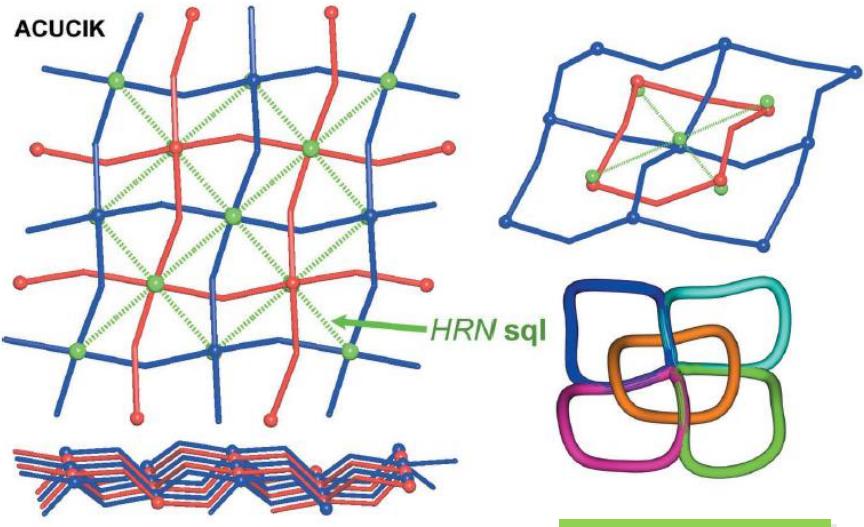


6-coor hxg

*... but are these patterns observed in other
2-fold interpenetrated nets?*

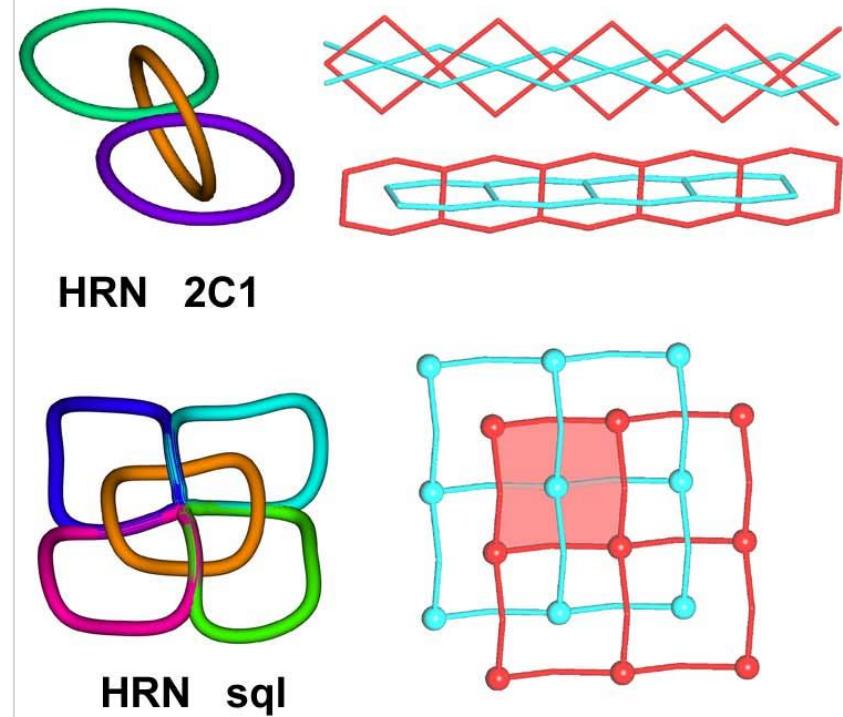
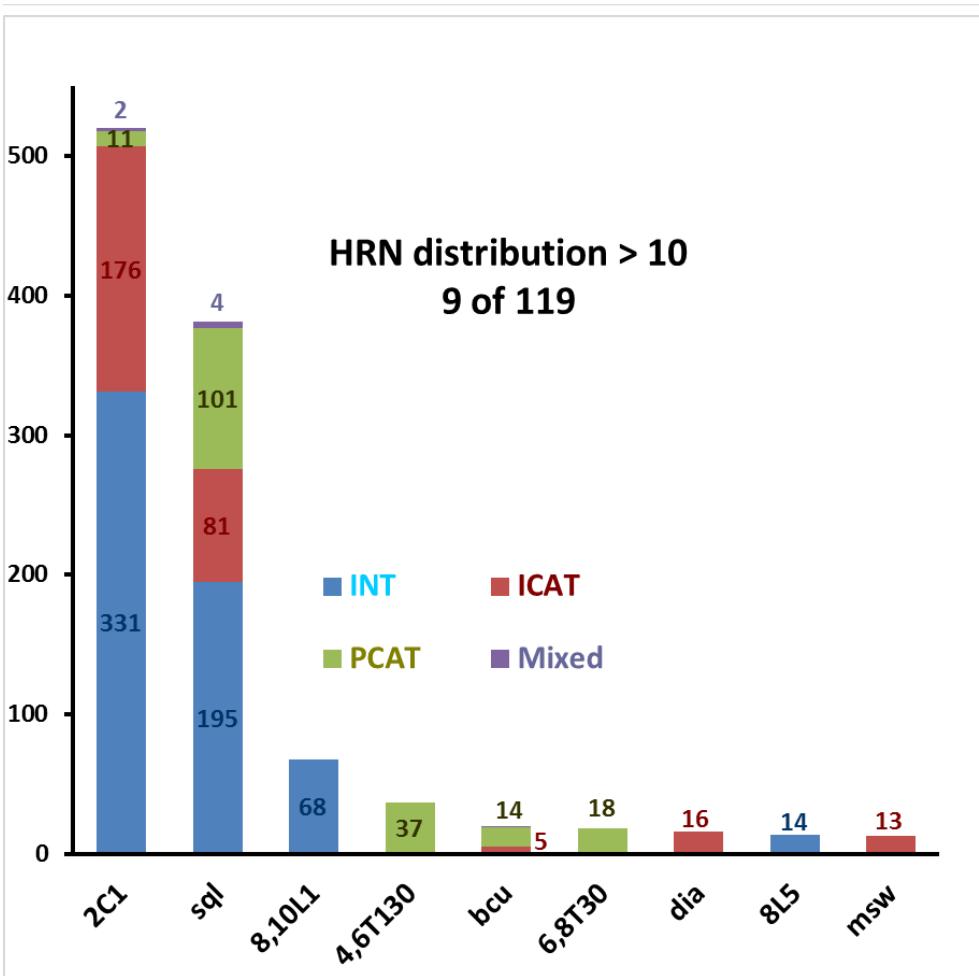
***YES, the same HRN may be found for different nets.
same “bouquet”***





Some **HRN** in 2-periodic entanglements:
sql and **simple chain (2C1)**

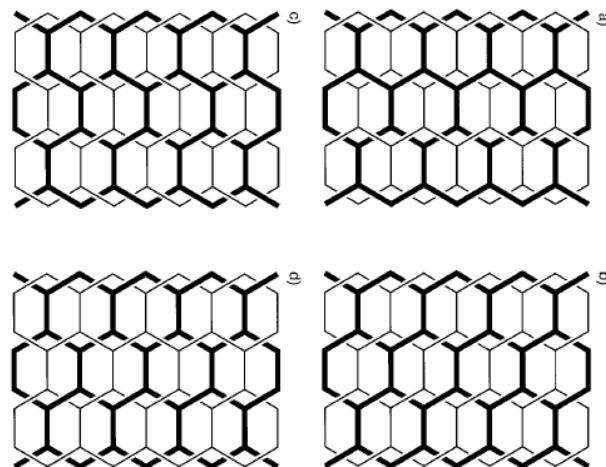
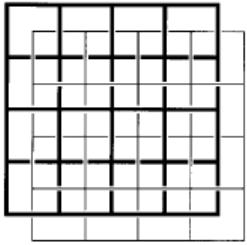
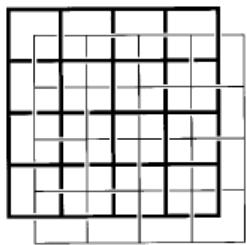
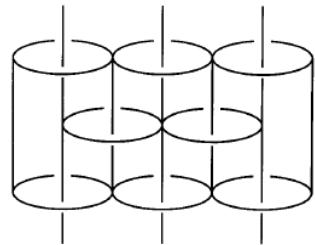
119 HRN in 2-periodic entanglements: 70% are simple chain (2C1) and sql



Interpenetrating Nets: Ordered, Periodic Entanglement

Stuart R. Batten and Richard Robson*

Angew. Chem. Int. Ed. **1998**, *37*, 1460–1494

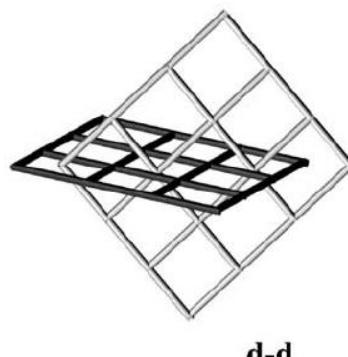
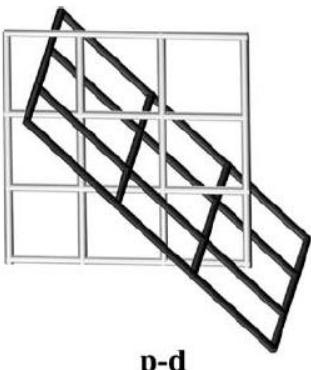
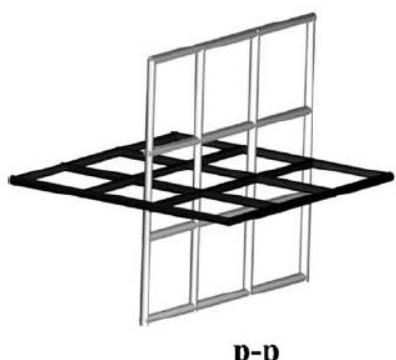


Chem. Rev. **2001**, *101*, 1629–1658

1629

From Molecules to Crystal Engineering: Supramolecular Isomerism and Polymorphism in Network Solids

Brian Moulton and Michael J. Zaworotko*



p-p

p-d

d-d

**Underlying net
topology**

sql, hcb, Kla...

Ring nets

FRN + HRN = ERN

**Pattern of
catenation**

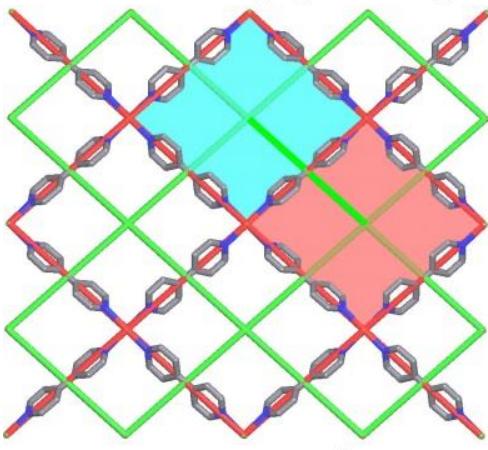
Hopf ring net HRN

Entanglement

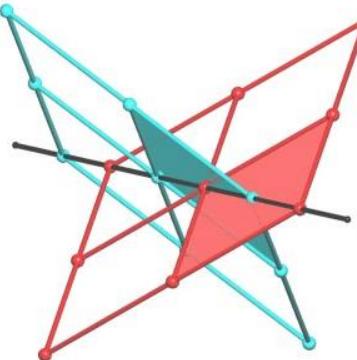
INT, ICAT, PCAT...

... and from HRN + FRN = ERN

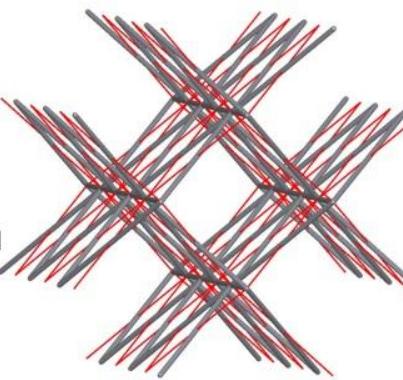
JEZRUB $[\text{Zn}(\text{H}_2\text{O})_2(4,4'\text{-bipy})_2]^{2+}$



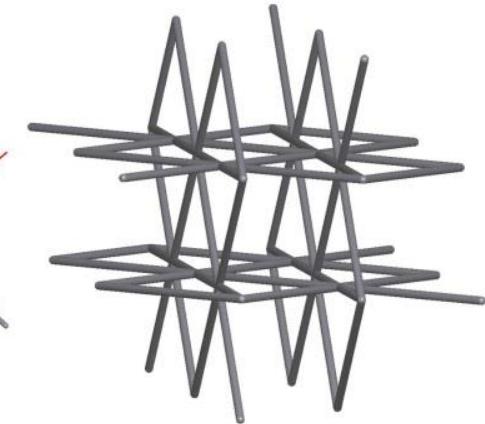
underlying net (red) **sql** +
fused ring net (green) FRN **sql**



inclined catenation of two **sql** +
Hopf ring net (HRN) 2-c linear chain

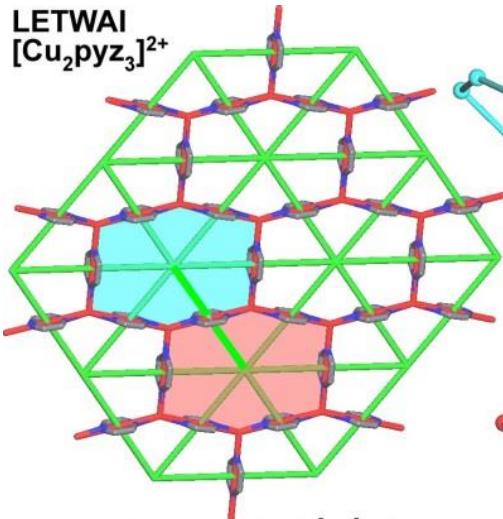


inclined catenation of **sql** (red) +
6-c extended ring net (grey) **ERN**

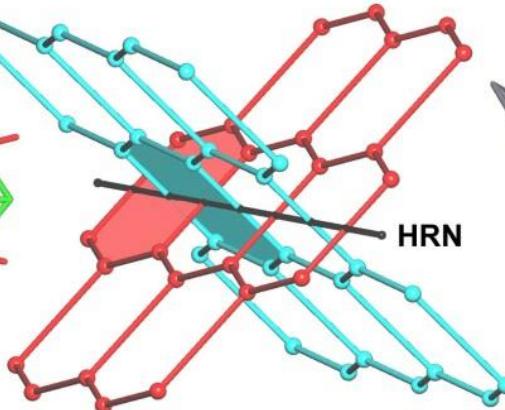


single 6-c *extended ring net*
ERN = **FRN+HRN** = $(4^9.6^6)\text{-}6\text{T13}$

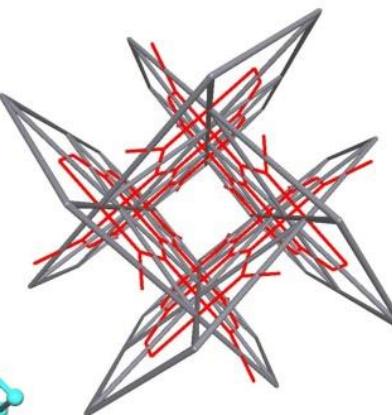
LETWAI
 $[\text{Cu}_2\text{pyz}_3]^{2+}$



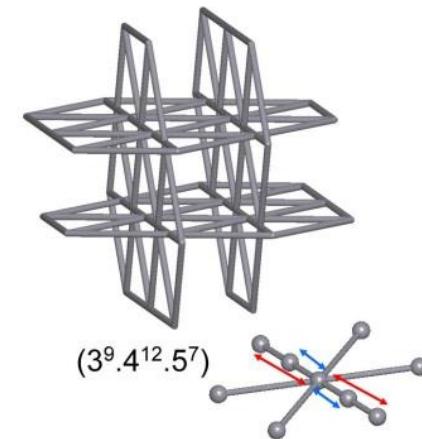
underlying net (red) **hcb** +
fused ring net (green) FRN **hxI**



inclined catenation of two **hcb** +
Hopf ring net (HRN) 2-c linear chain



inclined catenation of **hcb** (red) +
8-c extended ring net (grey) **ERN**



$(3^9.4^{12}.5^7)$
single 8-c *extended ring net*
with some coincident edges

ERN fully characterize the entanglement

Interpenetrating Nets: Ordered, Periodic Entanglement

Stuart R. Batten and Richard Robson*

Angew. Chem. Int. Ed. **1998**, *37*, 1460–1494

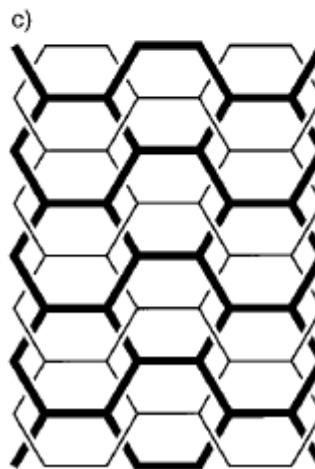
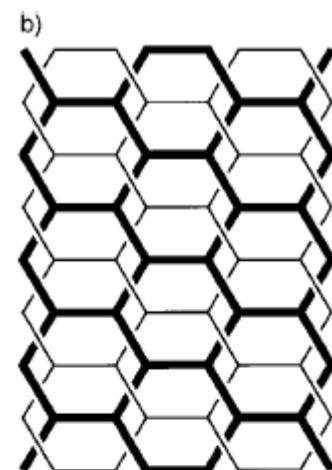
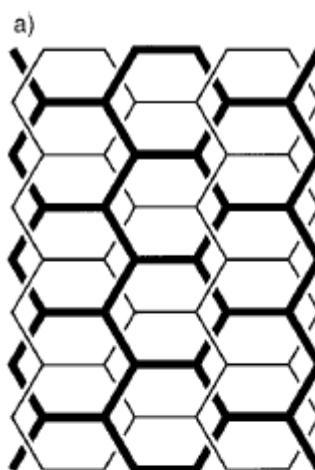
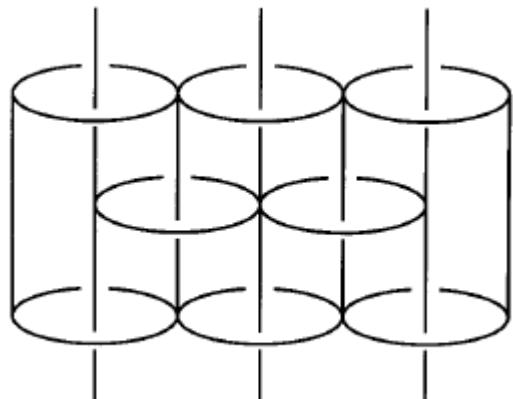
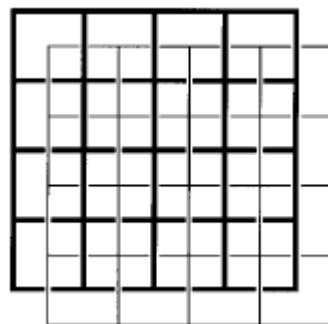
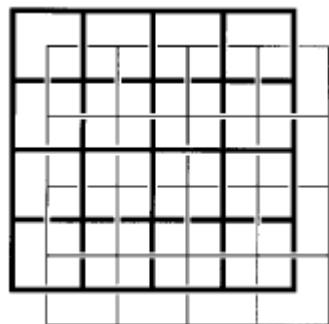
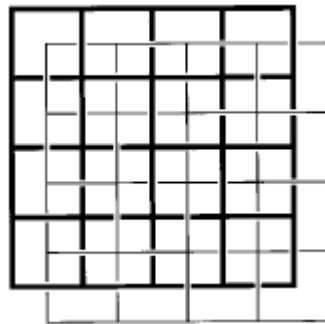
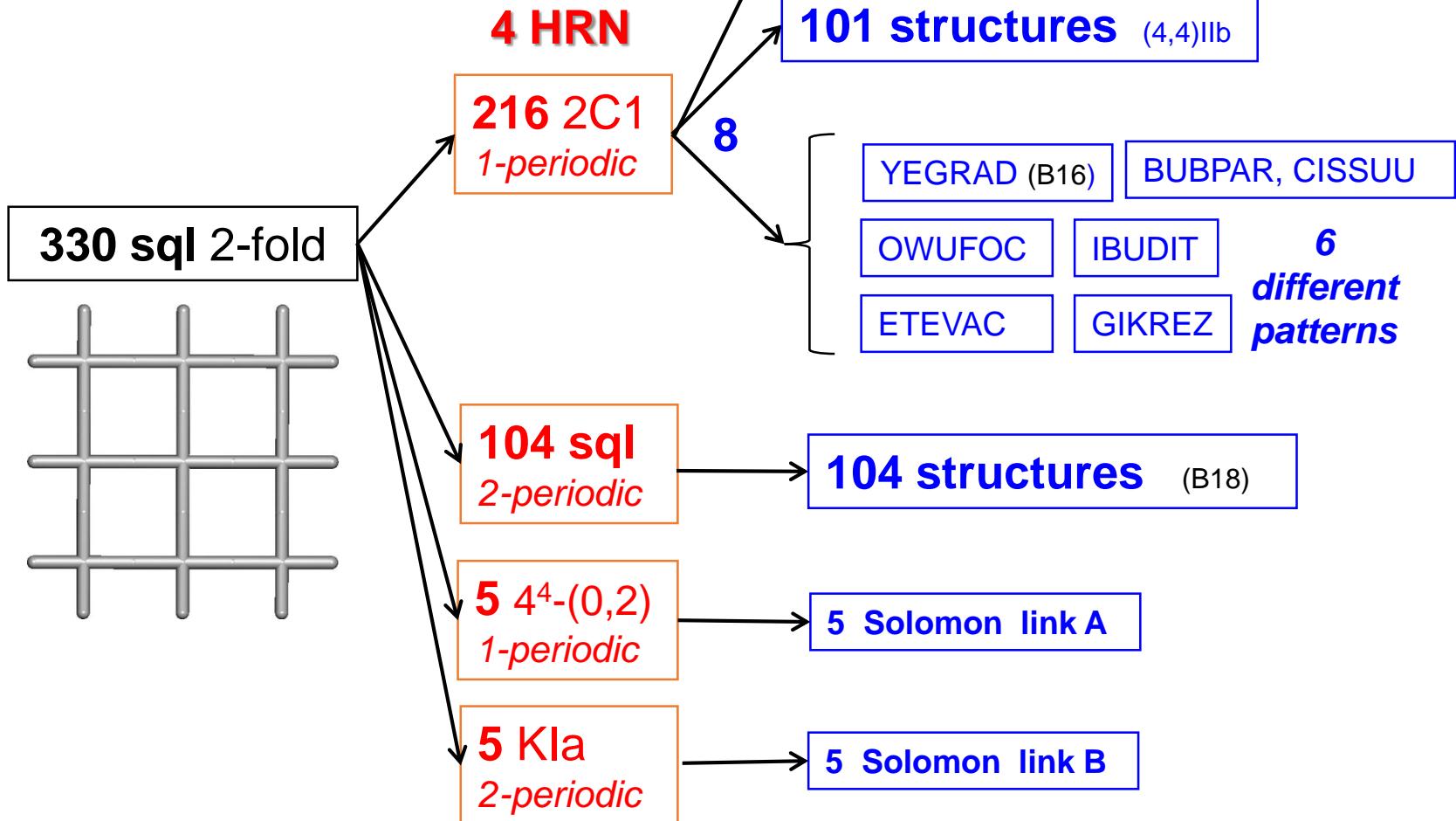


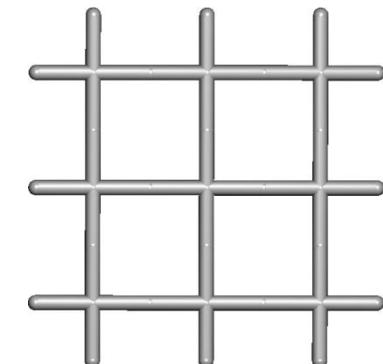
Figure 11. a)–d) Four topologically different modes of parallel interpenetration of (6,3) nets.

2-fold Interpenetration sql

11 Extended ring nets ERN



2-fold Interpenetration sql



4 HRN

216 2C1
1-periodic

104 sql
2-periodic

5 4⁴-(0,2)
1-periodic

5 Kla
2-periodic

11 Extended ring nets ERN

108 structures (4,4)IIa (B17) **32.7%**

101 structures (4,4)IIb **30.5%**

YEGRAD (B16)

BUBPAR, CISSUU

OWUFOC

IBUDIT

ETEVAC

GIKREZ

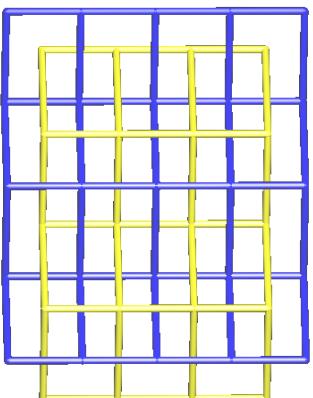
6 different patterns

104 structures (B18) **31.5%**

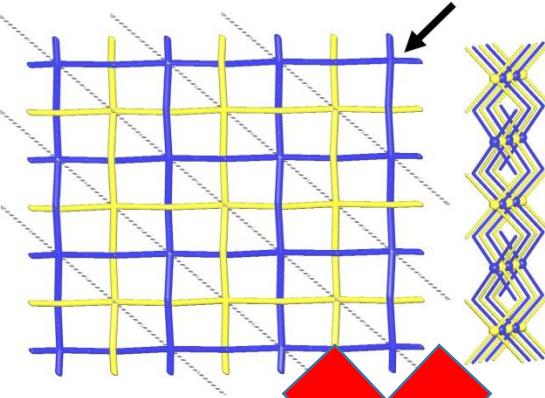
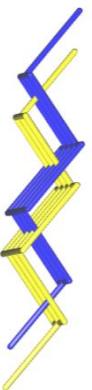
5 Solomon link A

5 Solomon link B

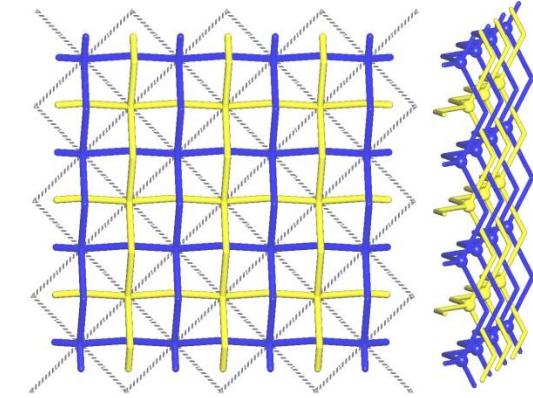
8



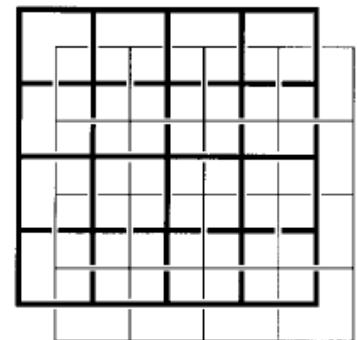
108 = 32.7%



101 = 30.6%



104 = 31.5%



Interpenetrating Nets: Ordered, Periodic Entanglement

Stuart R. Batten and Richard Robson*

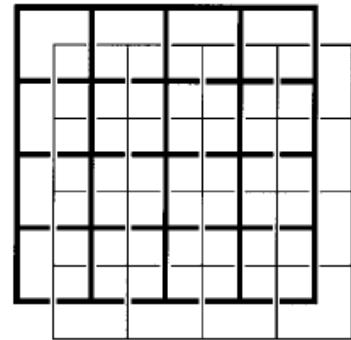
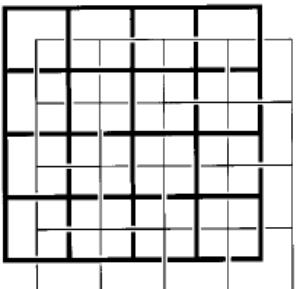
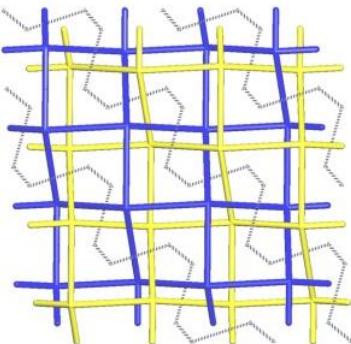


Figure 17. a) Two parallel interpenetrating (4,4) nets in the structure of $[\text{Cu}(\text{tcm})(\text{bipy})]$. The large circles represent Cu atoms, and the small circles C and N atoms. b) Schematic representation of the mode of interpenetration.

Figure 18. Schematic representation of the two parallel interpenetrating hydrogen-bonded (4,4) nets in the structure of $[\text{Re}_4(\text{CO})_{12}(\text{OH})_4] \cdot 2\text{bipy} \cdot 2\text{MeOH}$. The four-connected nodes shown represent the centers of the Re_4 clusters.



YEGRAD



YEGRAD

YEGRAD (B16)

BUBPAR CISSUU

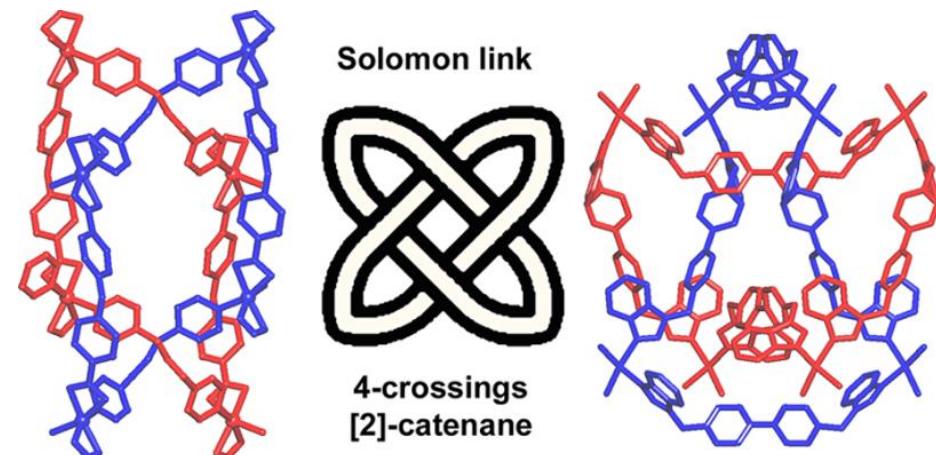
OWUFUC

IBUDIT

ETEVAC

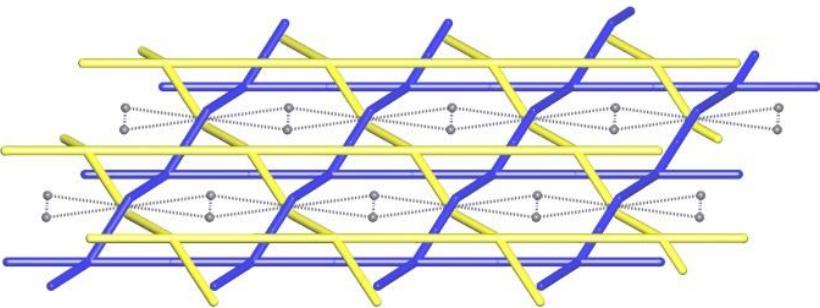
GIKREZ

Figure 16. a) Parallel interpenetrating (4,4) nets in the structure of $[Cd(4\text{-pic})_2\text{Ag}(\text{CN})_2]_2(4\text{-pic})$ (4-pic = 4-methylpyridine). The pendant 4-pic

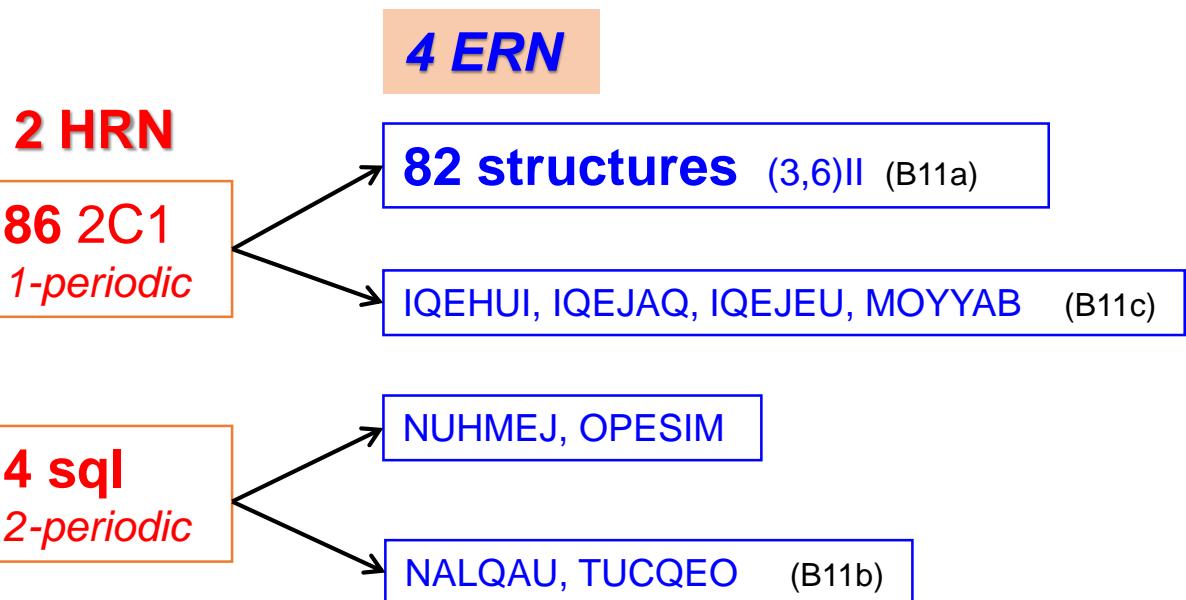
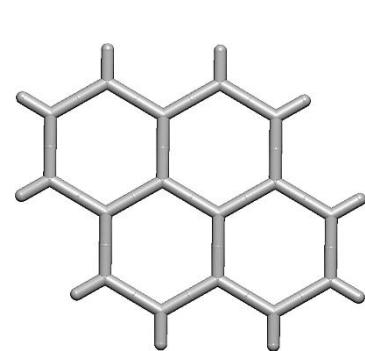


2-fold interpenetration sql

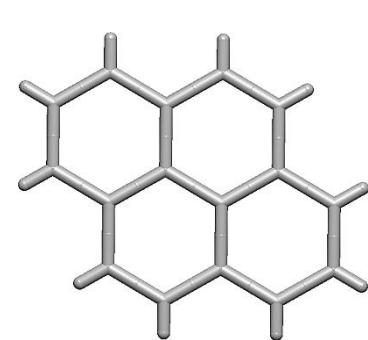
5 Solomon link A



2-fold Interpenetration hcb



2-fold Interpenetration **hcb**



90 hcb 2-fold

2 HRN

86 2C1
1-periodic

4 ERN

82 structures

(B11a)

91%

IQEHUI, IQEJAQ, IQEJEU, MOYYAB (B11c)

4 sqI
2-periodic

NUHMEJ, OPESIM

NALQAU, TUCQEO (B11b)

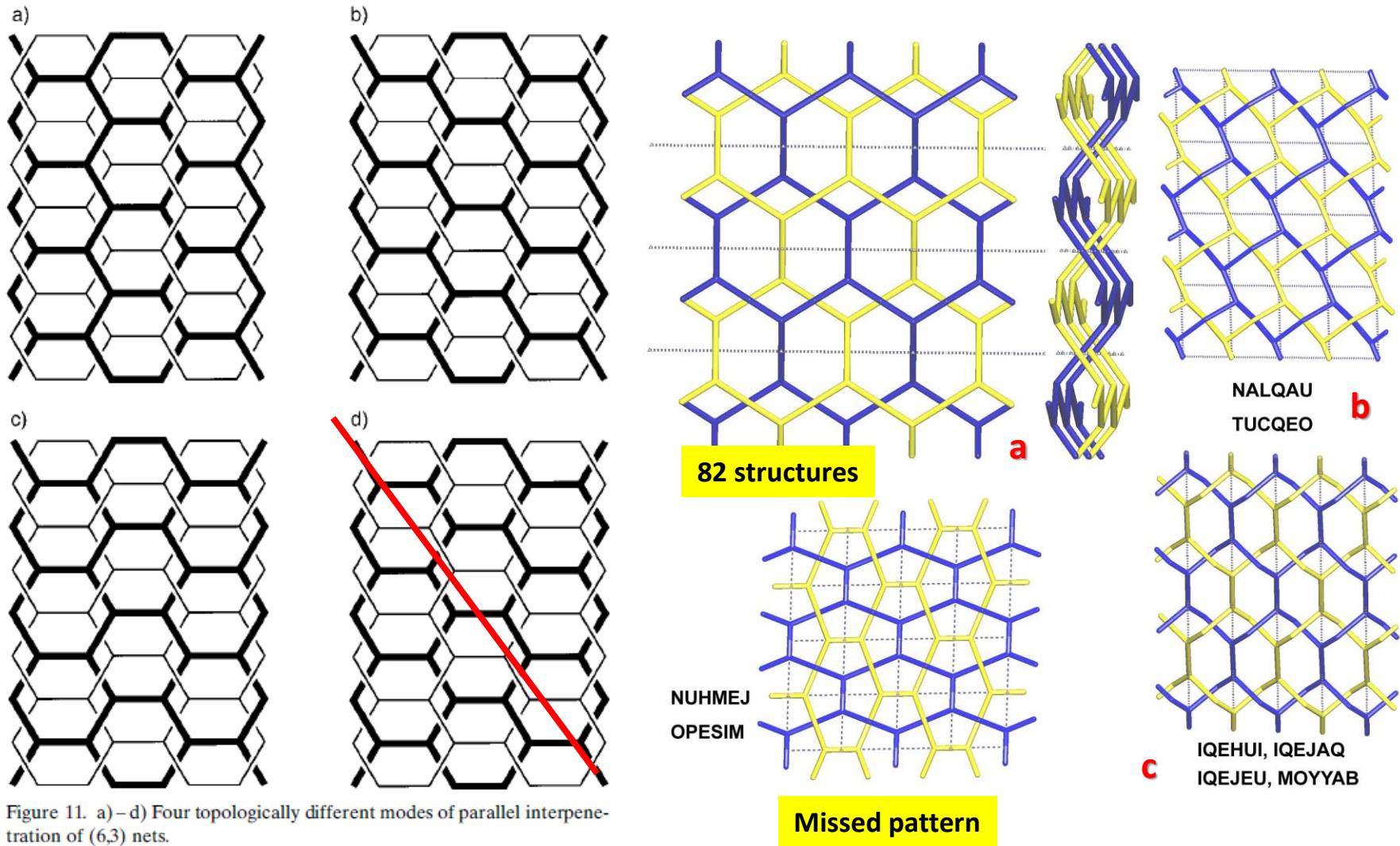
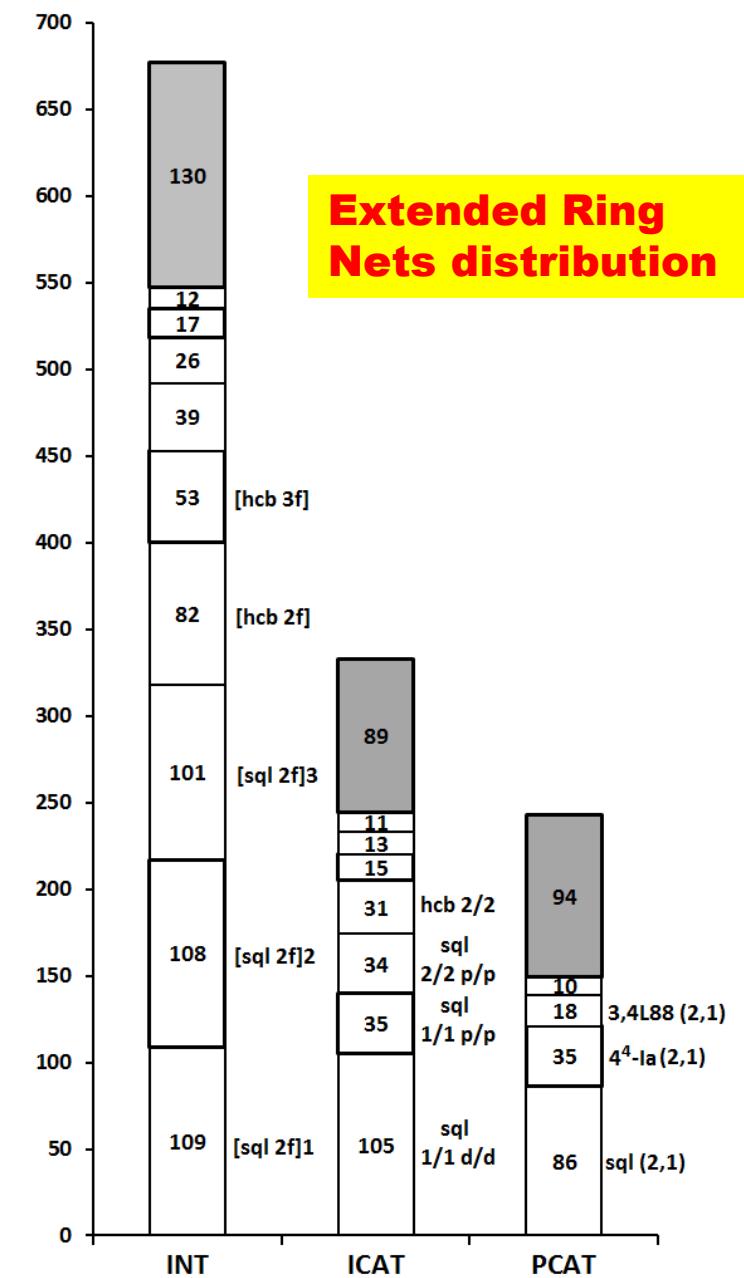


Figure 11. a)–d) Four topologically different modes of parallel interpenetration of (6,3) nets.

Layer	Entang type	DOC, IS, Z	HRN	ERN	hits
sql	INT	Z 2	2C1	6-c 4 ⁴ -IIb	101
sql	INT	Z 2	2C1	6-c 4 ⁴ -Ila	109
sql	INT	Z 2	sql	8-c 4 ⁴ -IV	108
sql	INT	Z 3	sql	8-c ¹	17
sql	INT	Z 3	8L5	12-c ¹	12
hcb	INT	Z 2	2C1	8-c 3 ⁶ -II	82
hcb	INT	Z 3	sql	10-c ¹	53
hcb	INT	Z 2, 2-loop	8,10L1	16,35-c	26
sql	INT	Z 2, 2-loop	8,10L1	16,27,27-c	39
sql	ICAT	DOC 1/1 d/d	2C1	6T13	105
sql	ICAT	DOC 1/1 p/p	2C1	6-c sqc23	35
sql	ICAT	DOC 2/2 p/p	sql	8-c ²	34
sql	ICAT	DOC 2/2 d/d	sql	8T4	15
hcb	ICAT	DOC 1/1	2C1	8-c ³	13
hcb	ICAT	DOC 2/2	sql	10-c ²	31
hcb	ICAT	DOC 3/3	msw	12-c ²	11
sql	PCAT	DOC 2, IS 1	sql	8-c hex	86
4 ⁴ -la	PCAT	DOC 2, IS 1	4,6T130	12,16-c	35
3,4L88	PCAT	DOC 2, IS 1	6,8T30	21,24-c	18
hcb	PCAT	DOC 2, IS 1	sql	10-c bct	10



The 20 most frequent patterns of entanglement (of 224)- ERN

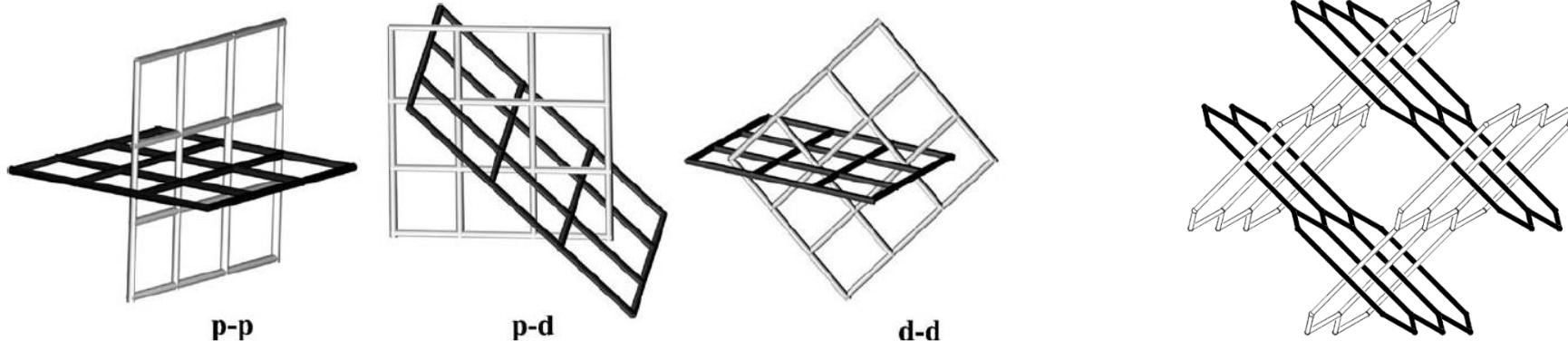
Layer	Entang. .type	DOC, IS, Z	HRN	ERN	hits
sql	ICAT	DOC 1/1 d/d	2C1	6T13	105
sql	ICAT	DOC 1/1 p/p	2C1	6-c sqc23	35
sql	ICAT	DOC 2/2 p/p	sql	8-c ²	34
sql	ICAT	DOC 2/2 d/d	sql	8T4	15
hcb	ICAT	DOC 1/1	2C1	8-c ³	13
hcb	ICAT	DOC 2/2	sql	10-c ²	31
hcb	ICAT	DOC 3/3	msw	12-c ²	11

Chem. Rev. 2001, 101, 1629–1658

1629

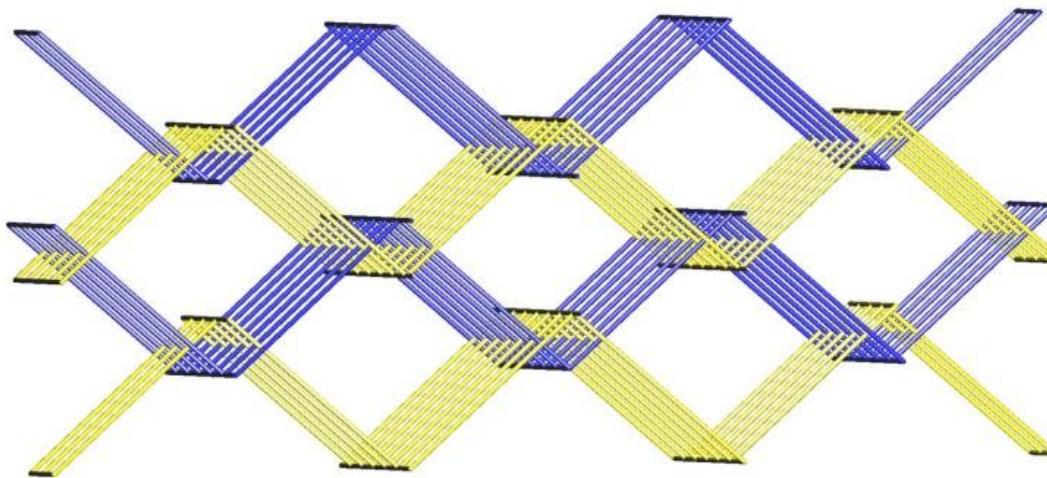
From Molecules to Crystal Engineering: Supramolecular Isomerism and Polymorphism in Network Solids

Brian Moulton and Michael J. Zaworotko*

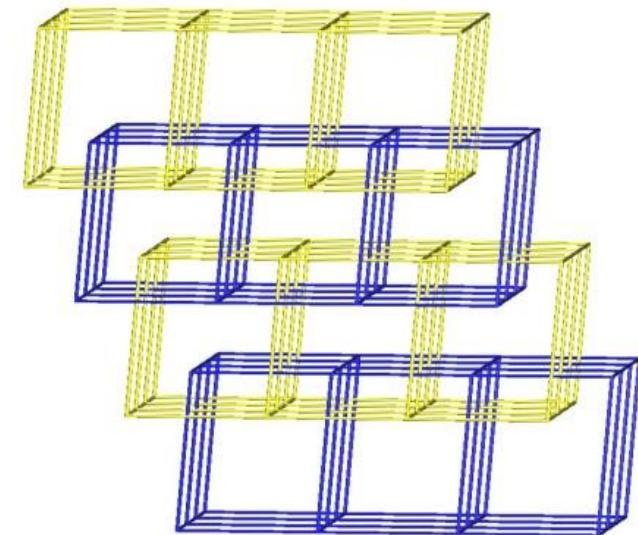


PCAT

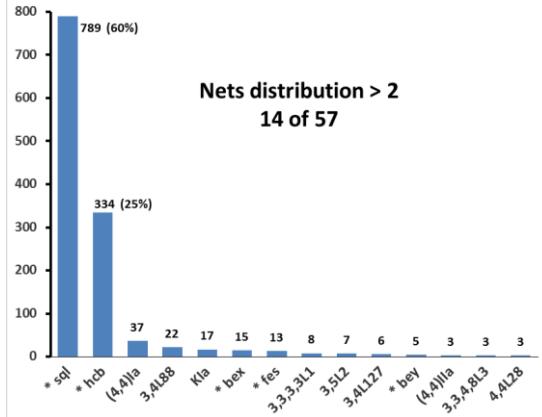
Layer	Entang type	DOC, IS, Z	HRN	ERN	hits
sql	PCAT	DOC 2, IS 1	sql	8-c hex	86
4 ⁴ -la	PCAT	DOC 2, IS 1	4,6T130	12,16-c	35
3,4L88	PCAT	DOC 2, IS 1	6,8T30	21,24-c	18
hcb	PCAT	DOC 2, IS 1	sql	10-c bct	10



86 PCAT of undulated sql

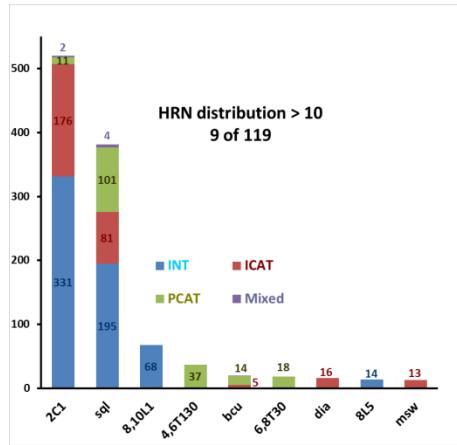


24 PCAT of double sql 4⁴-la

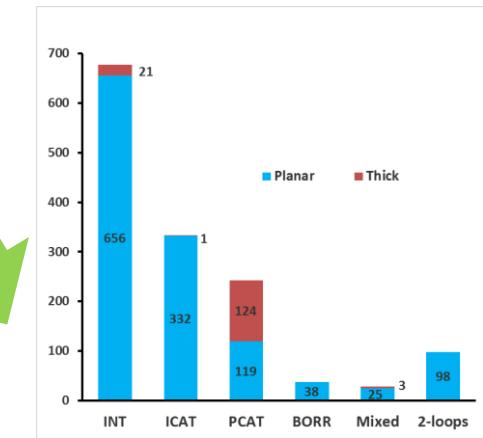
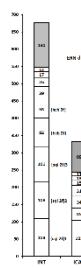


57 Underlying net topology
sql, hcb 85%

1319 structures



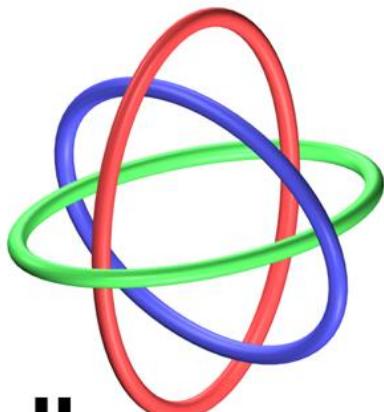
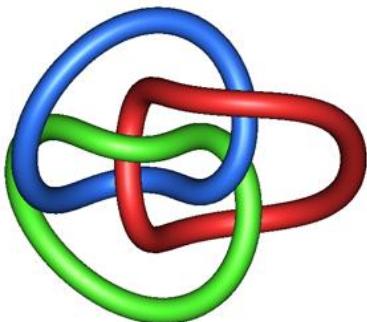
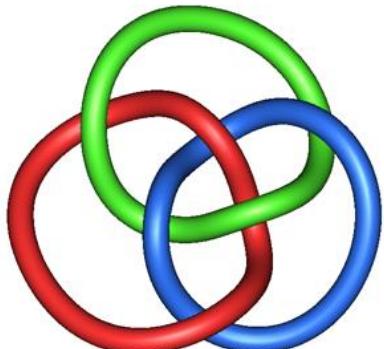
224 ERN
20 for 73%



119 Pattern of catenation HRN
sql, 2C1 70%

Entanglement
INT, ICAT, PCAT,
BORR

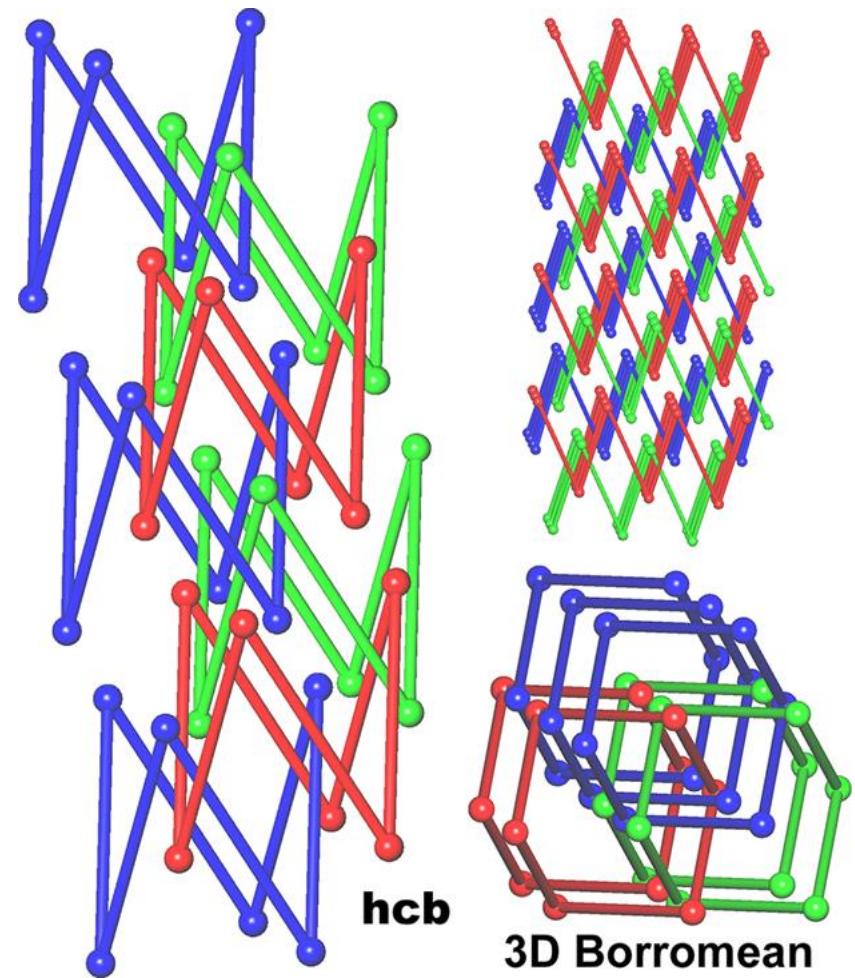
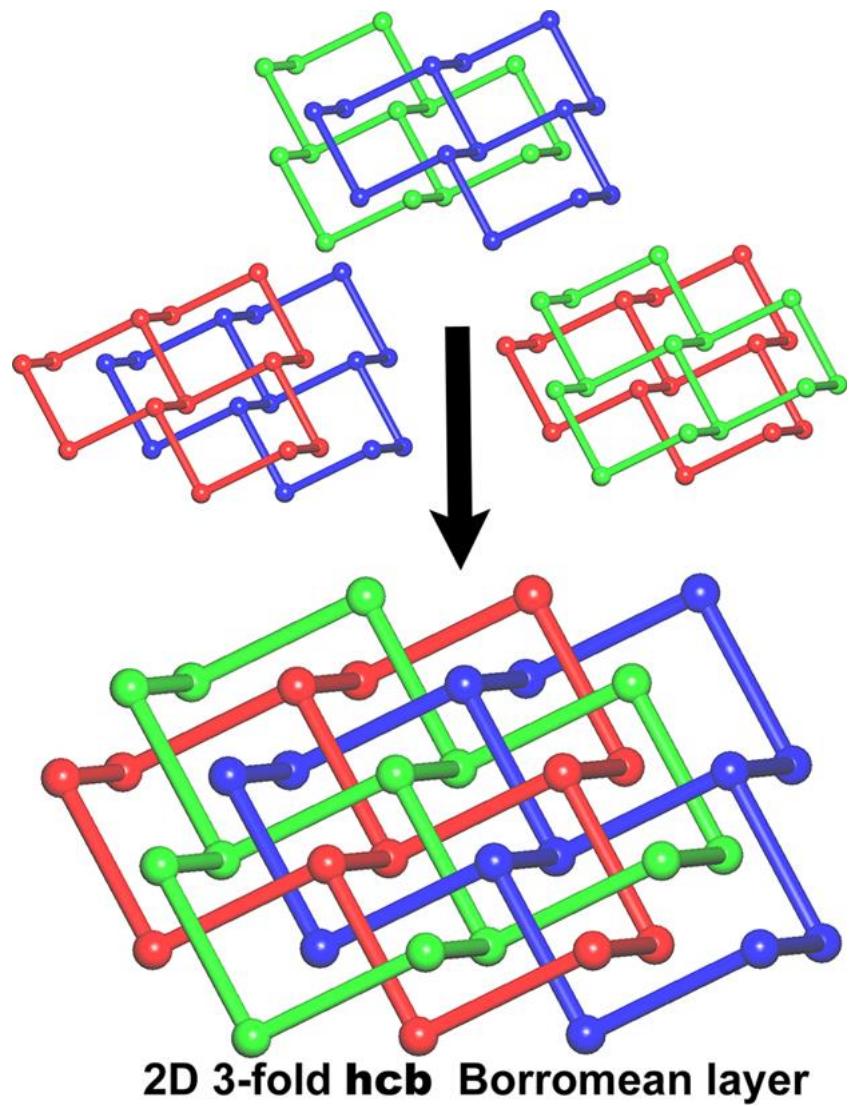
Borromean links



II

III





Applied Topological Analysis of Crystal Structures with the Program Package **ToposPro**

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program package for multipurpose
crystallochemical analysis

ToposPro

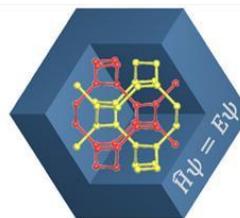
Version 5.0

PRACTICAL MANUAL 1.1.1

V.A. Blatov & D.M. Proserpio

Revision summer 2014

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