

# Forces and vibration modes in a chain of single gold atoms

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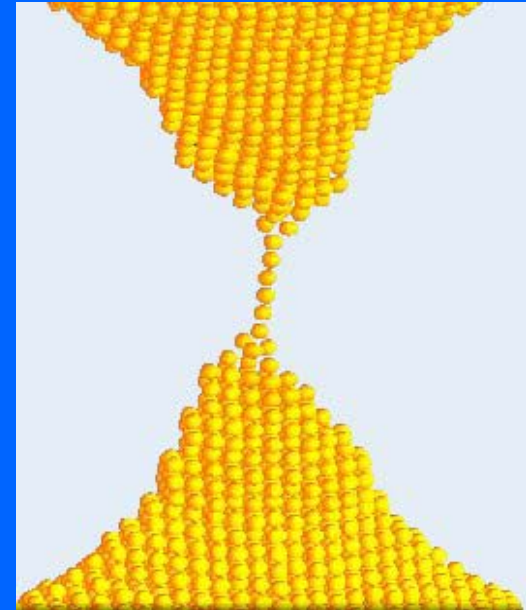
Nicolás Agraït

Carlos Untiedt

Gabino Rubio-Bollinger

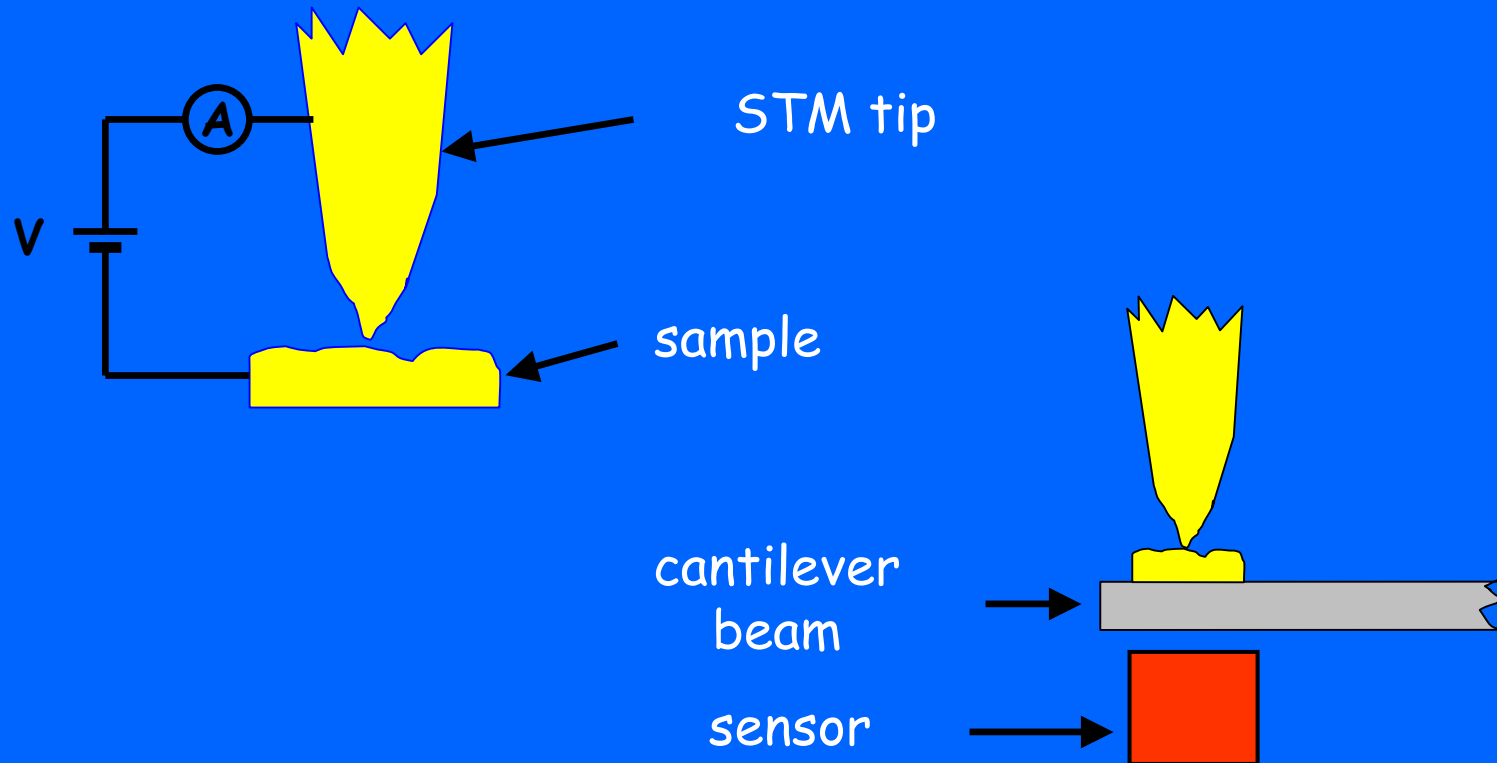
Rocio Grande

Sebastián Vieira

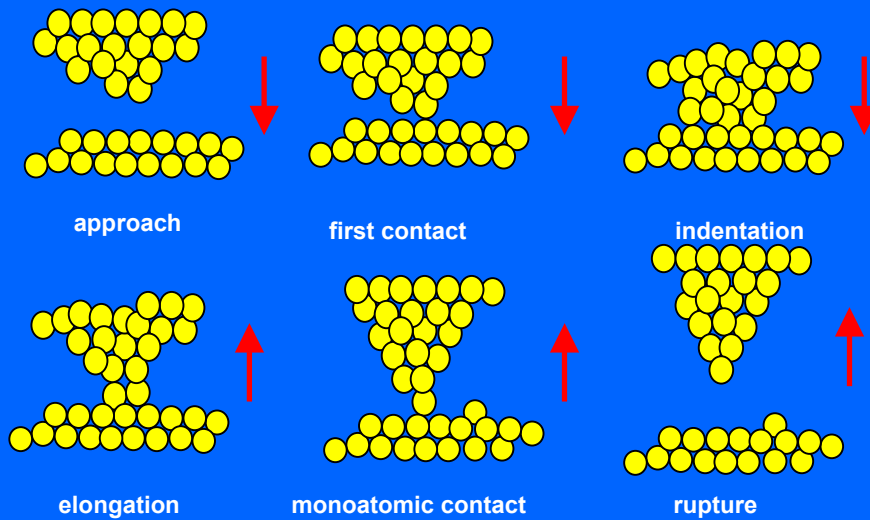


MD simulation by K. W. Jacobsen y M. R. Sørensen

# scanning tunneling microscope (STM) atomic force microscope (AFM)

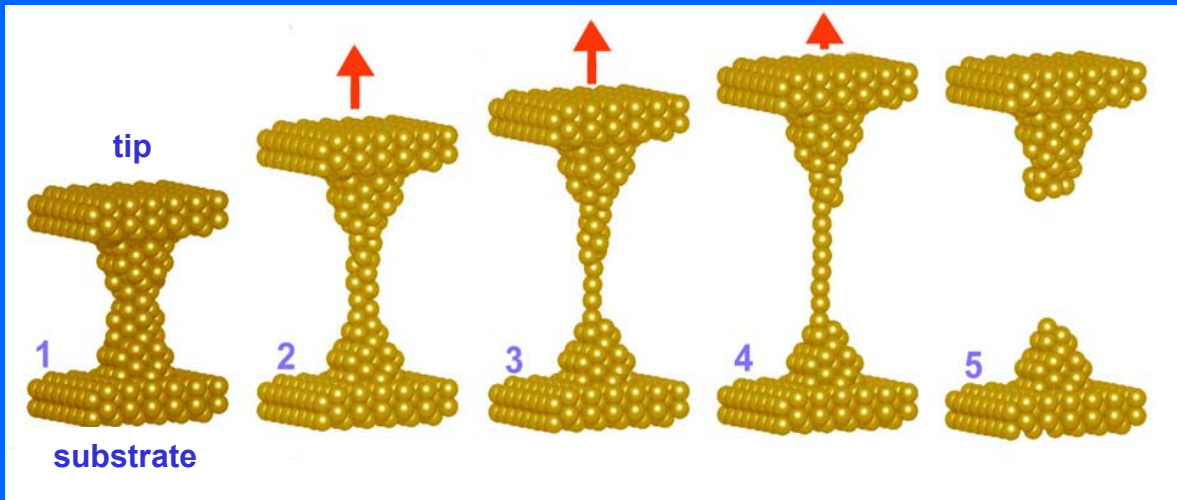


# formation of an atomic chain



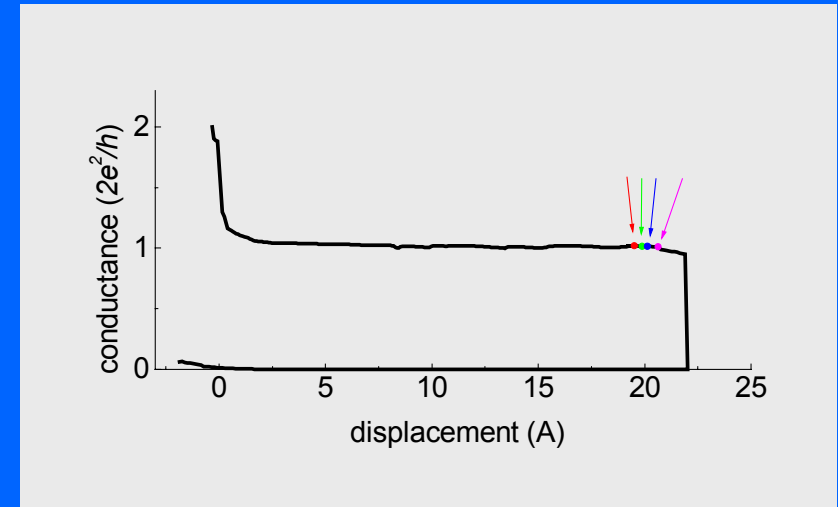
MD simulation by K. W. Jacobsen y M. R. Sørensen

# formation of an atomic chain

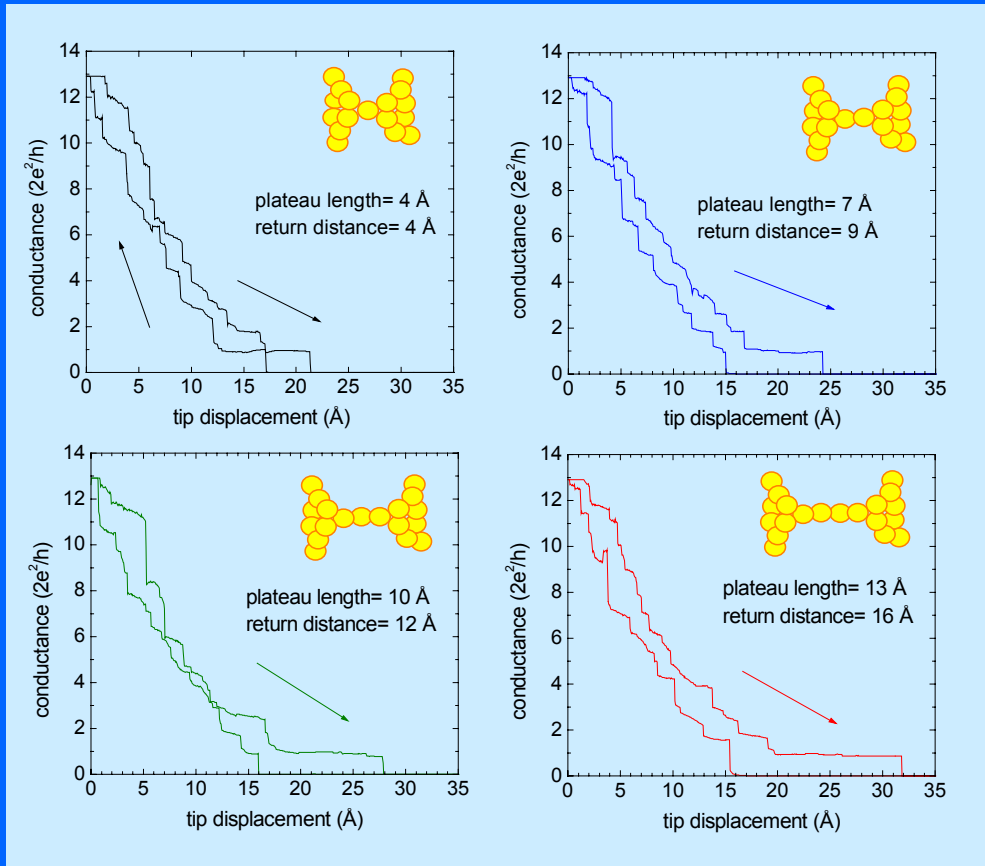


MD simulation by K. W. Jacobsen y M. R. Sørensen

- Conductance 1 quantum independent of **length** and **temperature**
- Very stable at low temperatures (hours)

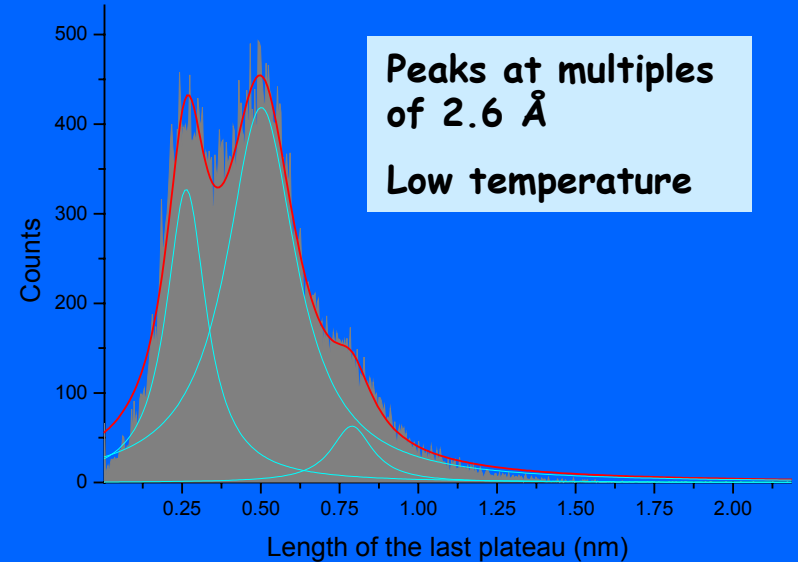


# length of an atomic chain



Conductance 1 quantum independent of length

Low probability for long chains



Yanson, Rubio Bollinger, van den Brom, Agraït, van Ruitenbeek, *Nature* **395**, 783 (1998)

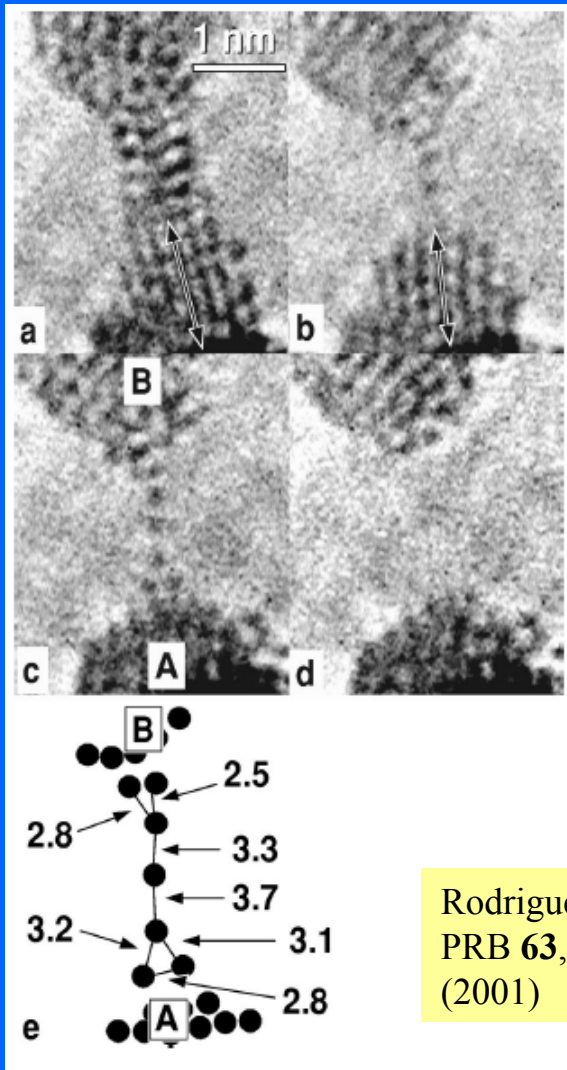
Untiedt, Yanson, Grande, Rubio-Bollinger, Agraït, Vieira, van Ruitenbeek, *PRB* 2002

# HRTEM images of Au atomic

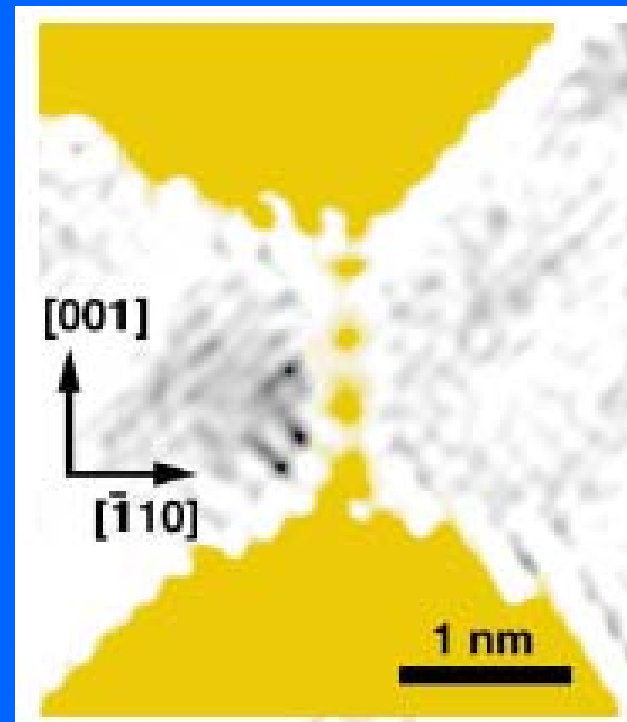
Room temperature

Stability ~ few seconds

$G \sim 1 G_0$



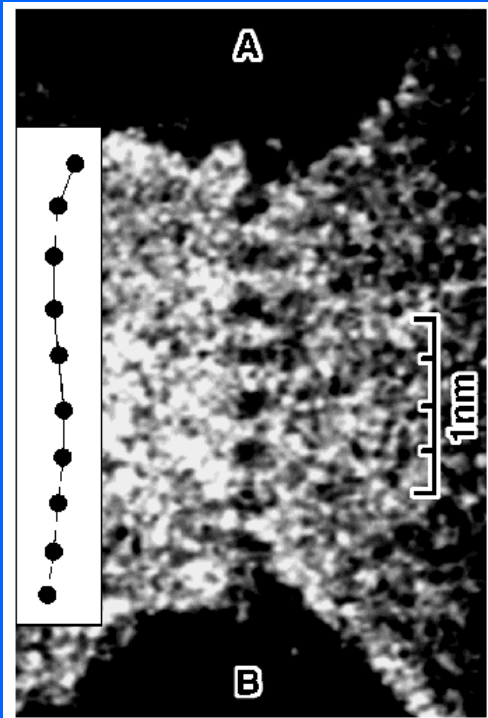
Rodrigues *et al.*,  
PRB **63**, 073405  
(2001)



Ohnishi *et al.*, Nature  
**395**, 780 (1998)

# HRTEM images of Au atomic

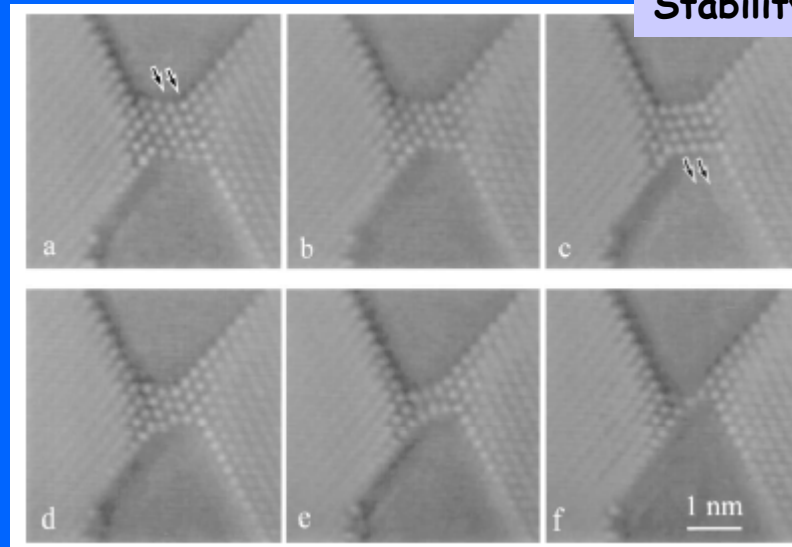
Room temperature



interatomic distance  $\sim 2.5 - 2.9 \text{ \AA}$

Stability  $\sim 20 \text{ s}$   
Non-conducting!

Kizuka *et al.*, JJAPL 40, L71 (2001)



Stability  $\sim$  few seconds

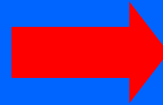
interatomic distance  
 $\sim 2.9 \text{ \AA}$

Takai *et al.*, PRL 87, 106105 (2001)

# electronic transport in atomic chains

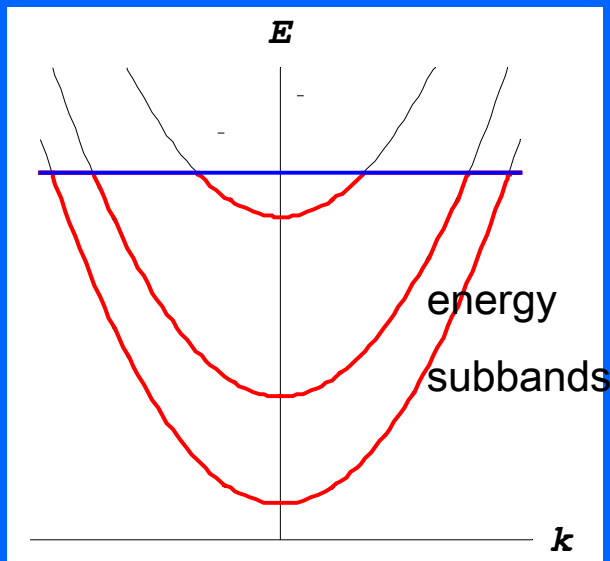
conductance  $\approx 2e^2/h$

- independent of length
- independent of temperature



one (almost) completely open quantum channel

conductance: Landauer's approach



$$G = \frac{2e^2}{h} M$$

no scattering  
 $M$  = number of modes

$$G = \frac{2e^2}{h} \sum_i T_i$$

scattering  
 $T_i$  = transmission of each subband



# mechanical properties of an atomic chain?

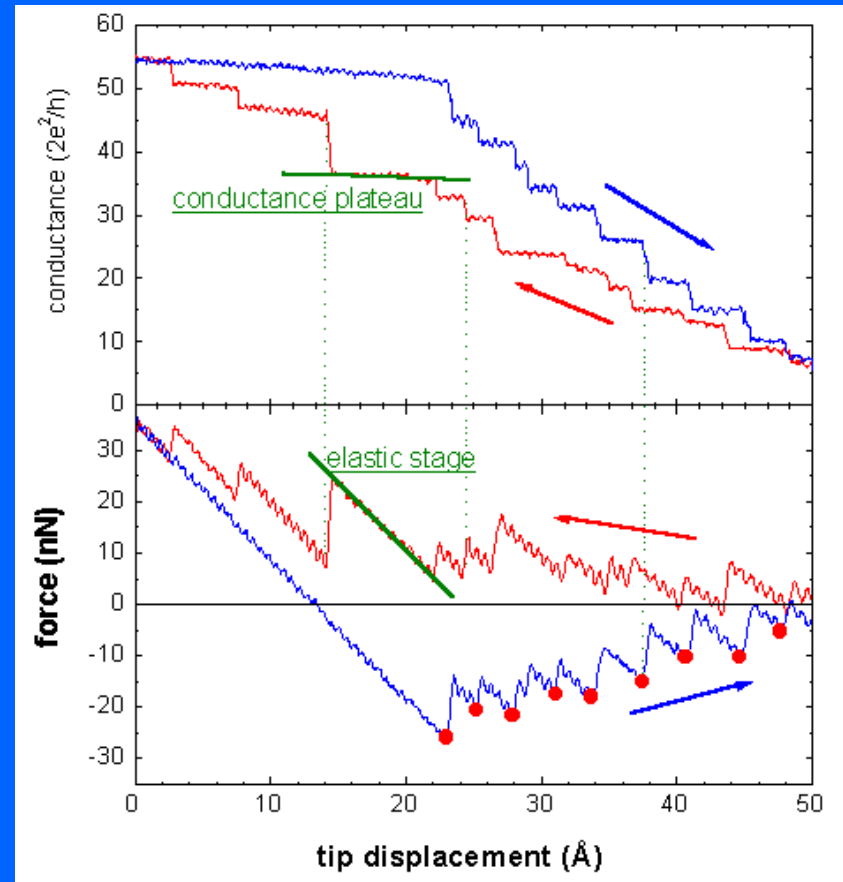
- o force to break an atomic chain
- o stiffness of the chain  
(related to bond stiffness)
- o vibration modes of an atomic  
chain

# elastic and plastic deformation in nanoscopic metallic systems

- Correlation between conductance jumps and force relaxations
- Very strong: ideal strength (2-4 GPa)

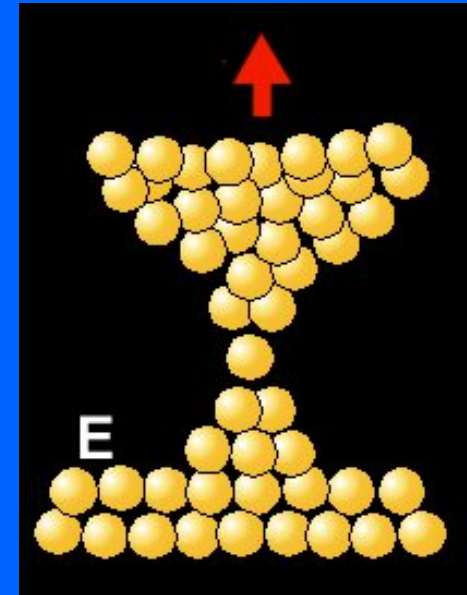
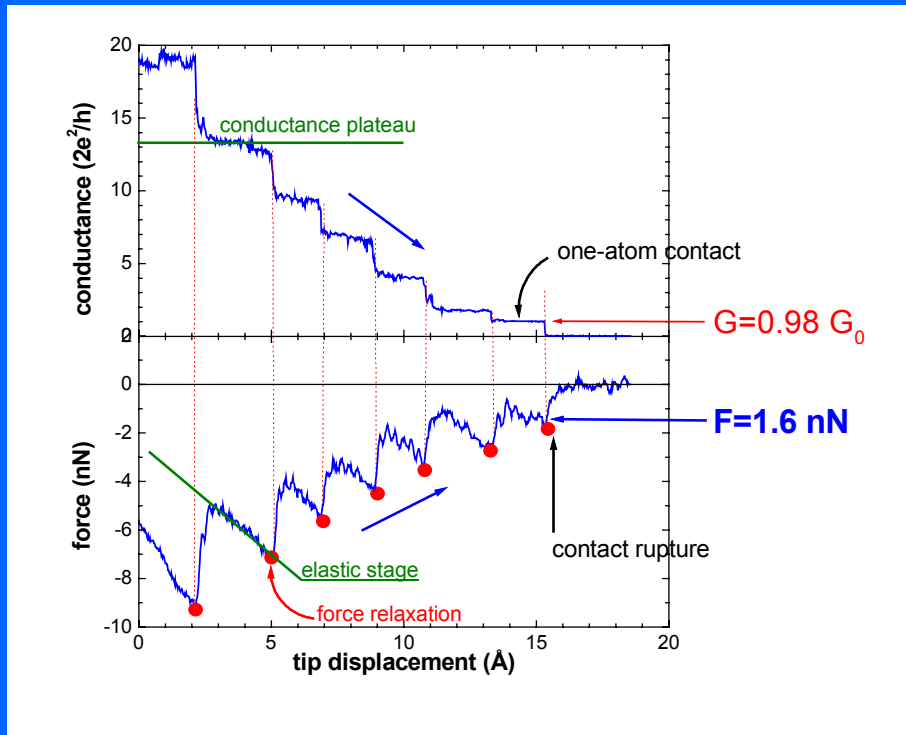
Elastic stages and sudden relaxations  
due to atomic rearrangements

Plastic deformation by slip of atomic  
planes (absence of dislocations)



N. Agraït, G. Rubio, S. Vieira.  
*Phys. Rev. Lett.* **74** (1995).

# breaking a one-atom contact

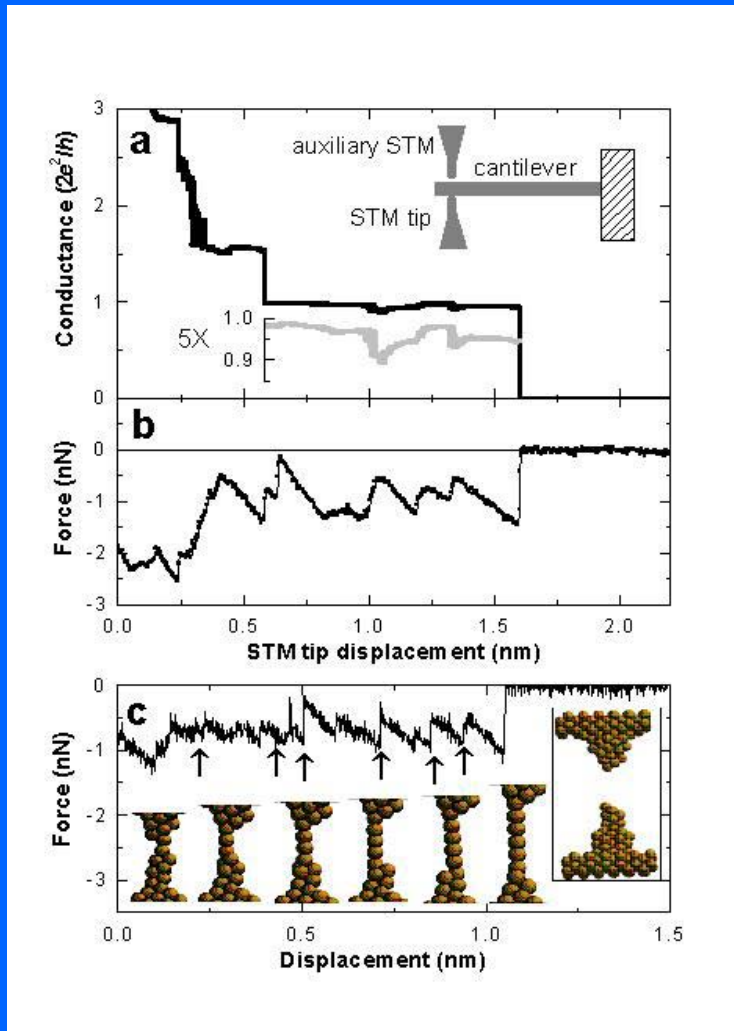


force to break the  
one-atom contact = 1.6 nN

G. Rubio, N. Agrait, S. Vieira.  
*Phys. Rev. Lett.* **76** (1996).

# mechanical properties of atomic chains

G. Rubio-Bollinger, S.R. Bahn, N. Agrait, K.W. Jacobsen, S. Vieira.  
*Phys. Rev. Lett.* **87** (2001).



elastic stages + atomic rearrangements  
during pullout of the chain

Experimental setup:

- low temperature
- very high mechanical stability  $\sim 1$  pm
- sensor's spring constant  $\sim 400$  N/m



MD simulation  
using EMT

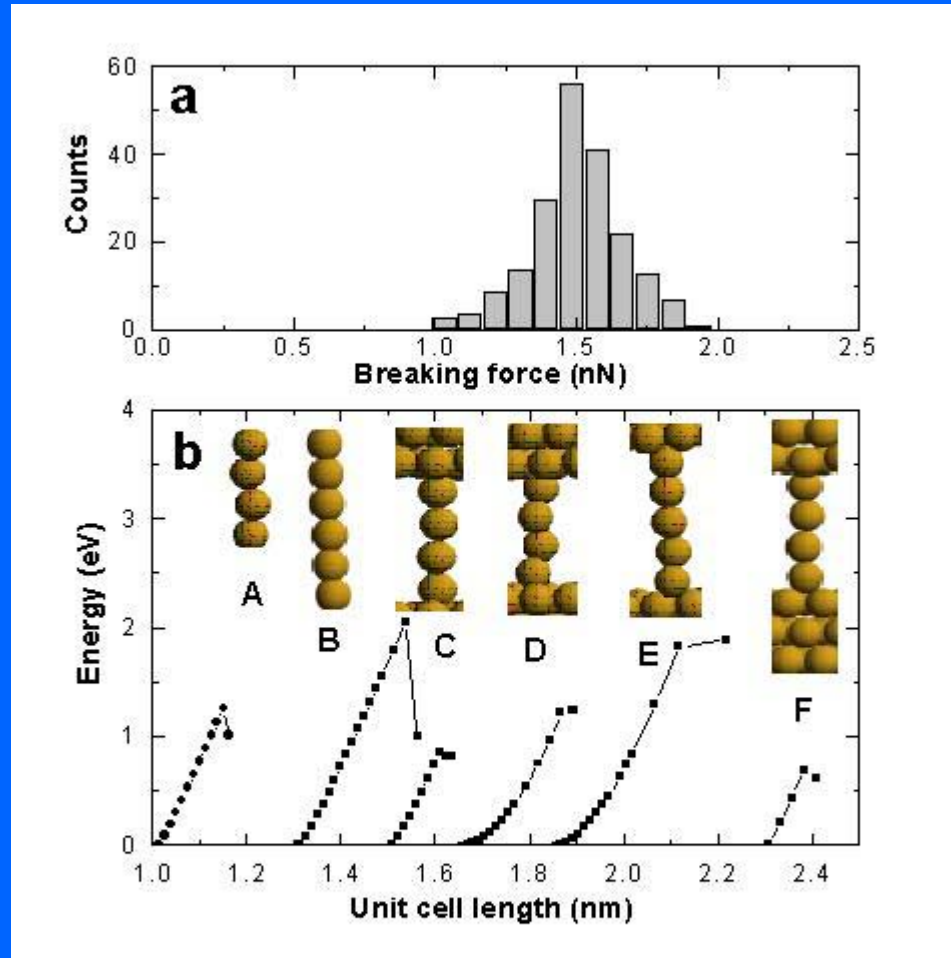
# breaking an atomic chain

## EXPERIMENT

- breaking force = 1.5 nN
- larger than during pullout
- independent of length

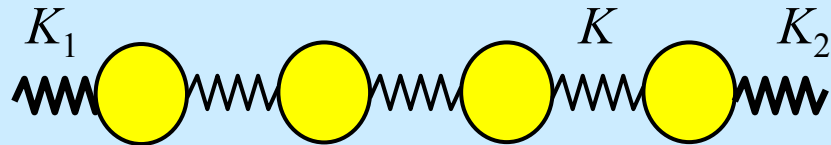
## THEORY

- breaking force = 1.4 - 1.6 nN (depends on approximation for exchange-correlation)
- independent of connection to substrate
- bonds in the chain are stronger (x2) than in bulk due to low coordination environment



# stiffness of an atomic chain

$N$ -atom chain

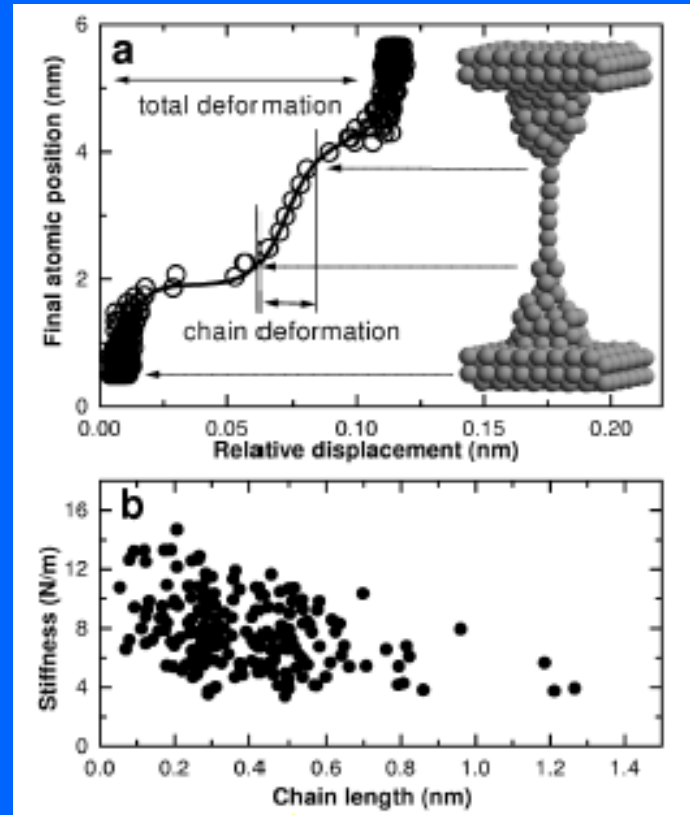


$$K_{\text{tot}} = \left( \frac{1}{K_1} + \frac{N}{K} + \frac{1}{K_2} \right)^{-1}$$

Chain can be much stiffer than electrodes:

- connections to electrodes can take most of the deformation

EMT MD simulation



EXPERIMENT

# vibration modes of an atomic chain

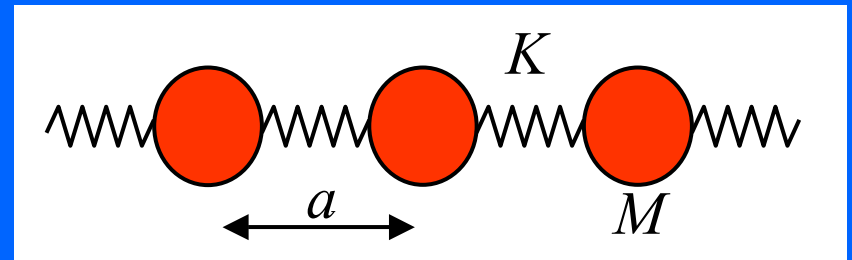
$N$  = number of atoms



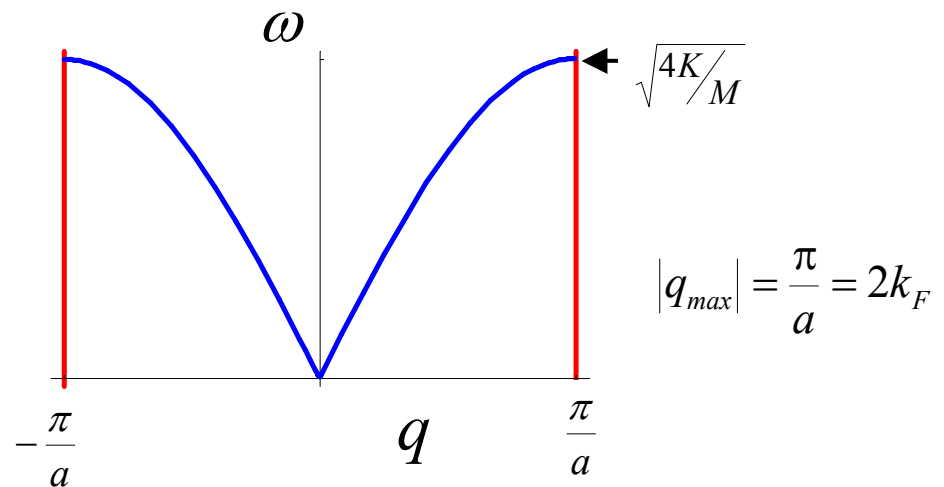
$N$  longitudinal modes



$2N$  transverse modes



## Longitudinal modes

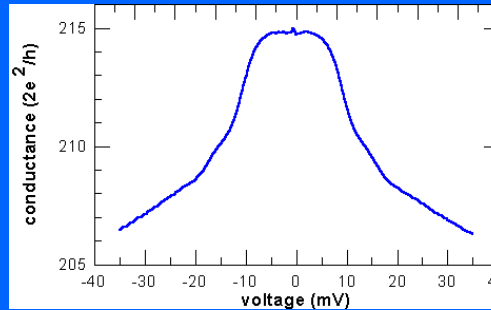
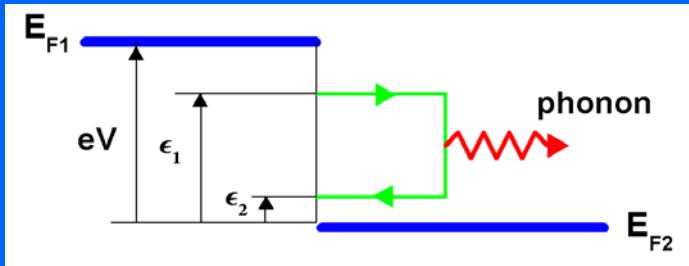


$$\omega^2 = 4 \frac{K}{M} \sin^2 \frac{qa}{2}$$

For a half filled band

$$k_F = \pi/2a$$

# Point-Contact Spectroscopy (PCS)

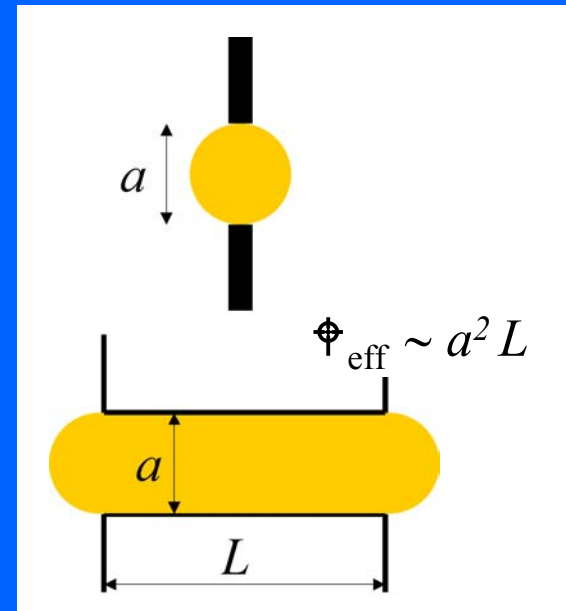
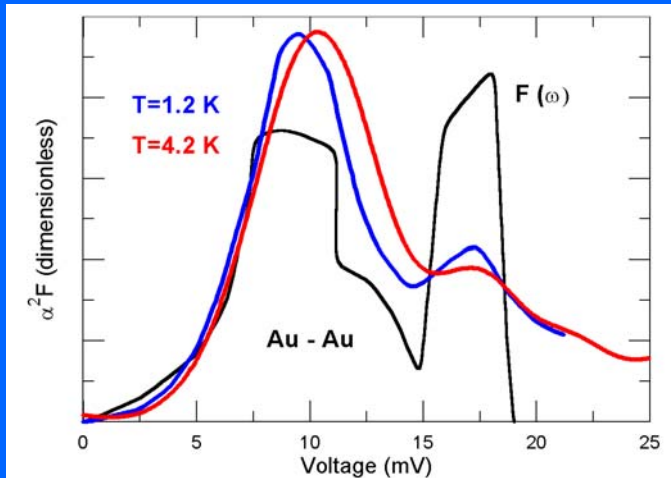


PCS probes local phonon DOS

$$\frac{d^2 I}{dV^2} \propto \Omega_{\text{eff}} N(0) \alpha^2 F_{\text{ph}}(eV)$$

$$\Delta G \propto G^{3/2}$$

$$\Delta G / G \propto a$$



Effective volume for inelastic scattering

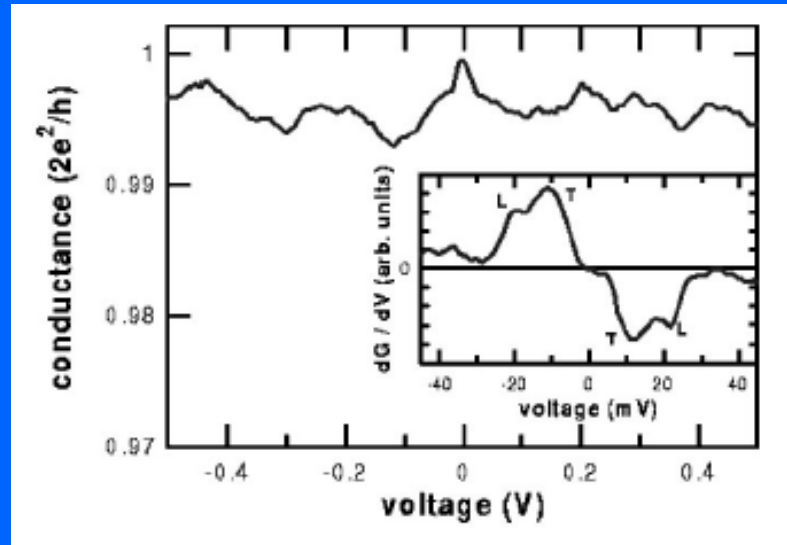
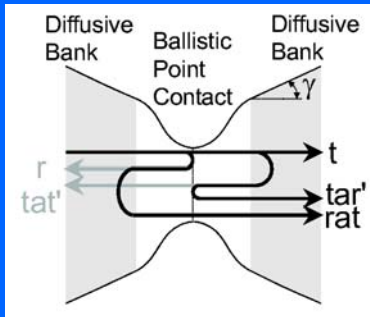


# Point-Contact Spectroscopy (PCS) in one-atom contacts

PCS of a one-atom contact

Conductance fluctuations  
due to elastic scattering  
near the contact

Ludolph *et al.*, PRL **82**, 1530 (1999)

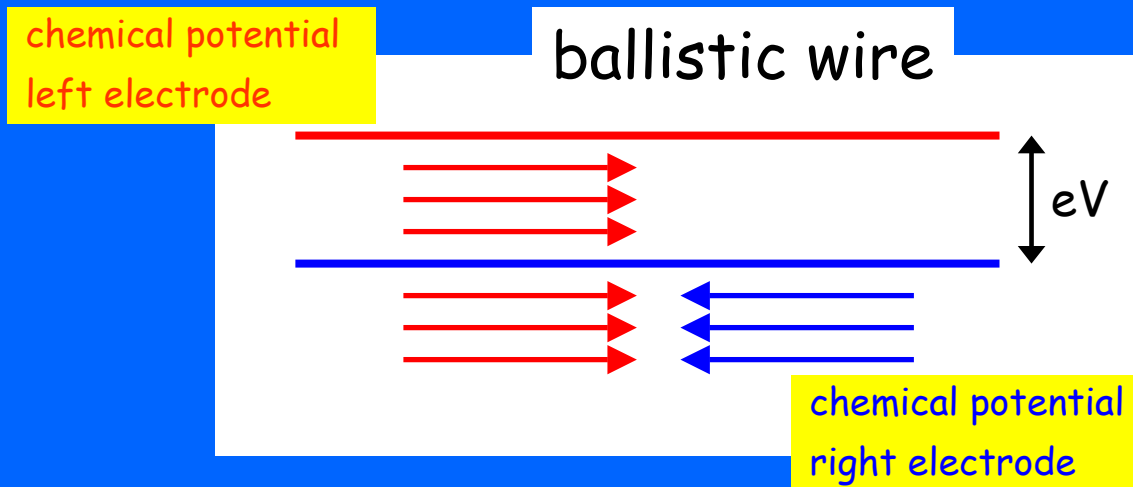
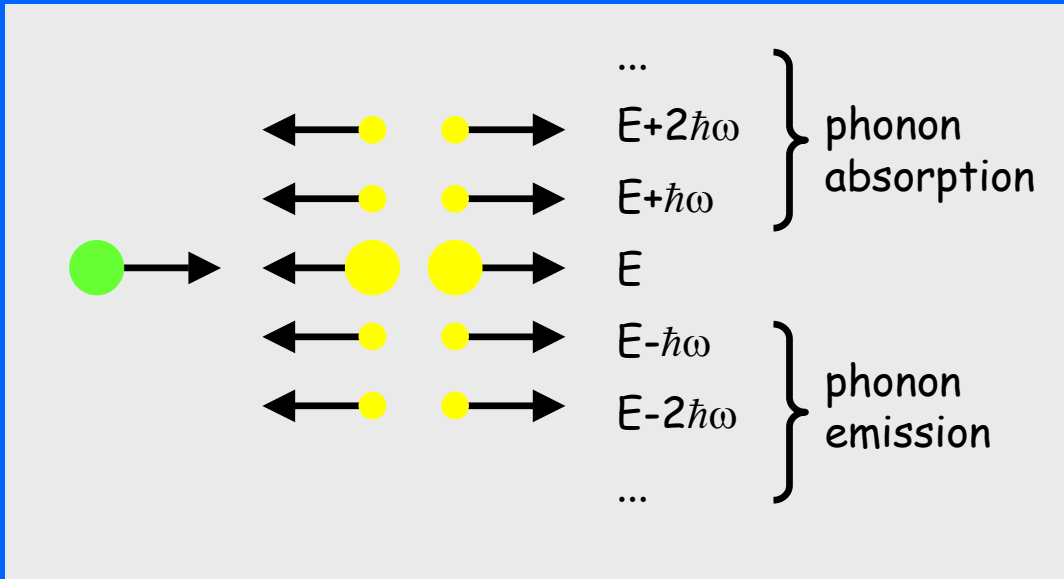


For one channel  
 $\Delta G \sim T(1-T)^{1/2}$

Untiedt *et al.*, PRB  
**62**, 9962 (2000)

Conductance drop  
due to phonons:  
 $\Delta G \propto G^{3/2}$   
 $\Delta G / G \approx 0.15 \%$

# e-ph interaction in 1d (infinite atomic chain)



only longitudinal modes interact

at low T:

- phonon absorption is always possible
- phonon emission for  $eV > \hbar\omega$

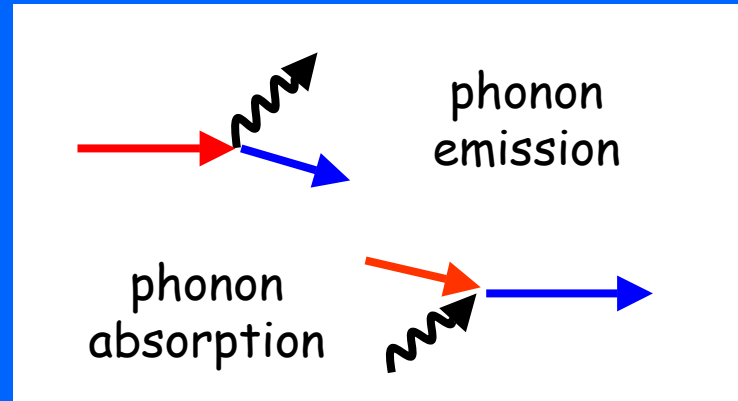
# e-ph interaction in 1d (infinite atomic chain)

## energy conservation

$$E_{el} \sim 1 \text{ eV}$$

$$E_{ph} \sim 1 \text{ meV}$$

$$E'_{el} \approx E_{el} \Rightarrow |\mathbf{k}'| \approx |\mathbf{k}| \approx k_F$$



## momentum conservation

$$\text{emission: } \mathbf{k} = \mathbf{k}' + \mathbf{q} \Rightarrow q = 0 \text{ or } q = 2k_F$$

$$\text{absorption: } \mathbf{k} + \mathbf{q} = \mathbf{k}' \Rightarrow q = 0 \text{ or } q = -2k_F$$

$$1 \text{ electron/atom} \Rightarrow k_F = q = \pi / 2a$$
$$q = \pm \pi / a$$

Brillouin zone mode

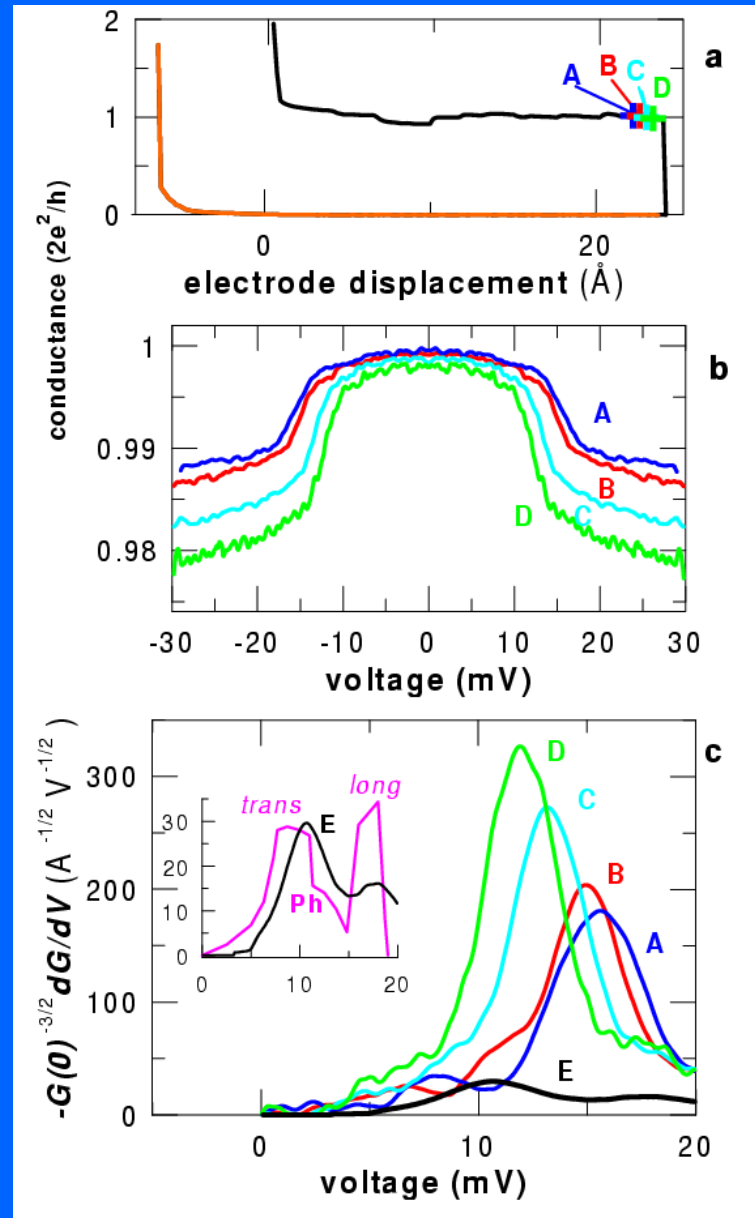


- electrons only interact with Brillouin-zone phonons
- electrons are always backscattered

# electron-phonon interaction in an atomic chain

threshold for e-ph interaction:  
no inelastic scattering below threshold

- dependence on strain



# Conductance of a finite wire of length $L$

- Probability per that an electron in state  $k$  will emit a phonon in the chain

$$P_k^{em} = \frac{L}{\ell} (n_{q_{\max}} + 1)$$

$$\text{for } \varepsilon_k - \varepsilon_F > \hbar\omega_{q_{\max}}$$

- Probability per that an electron in state  $k$  will absorb a phonon in the chain

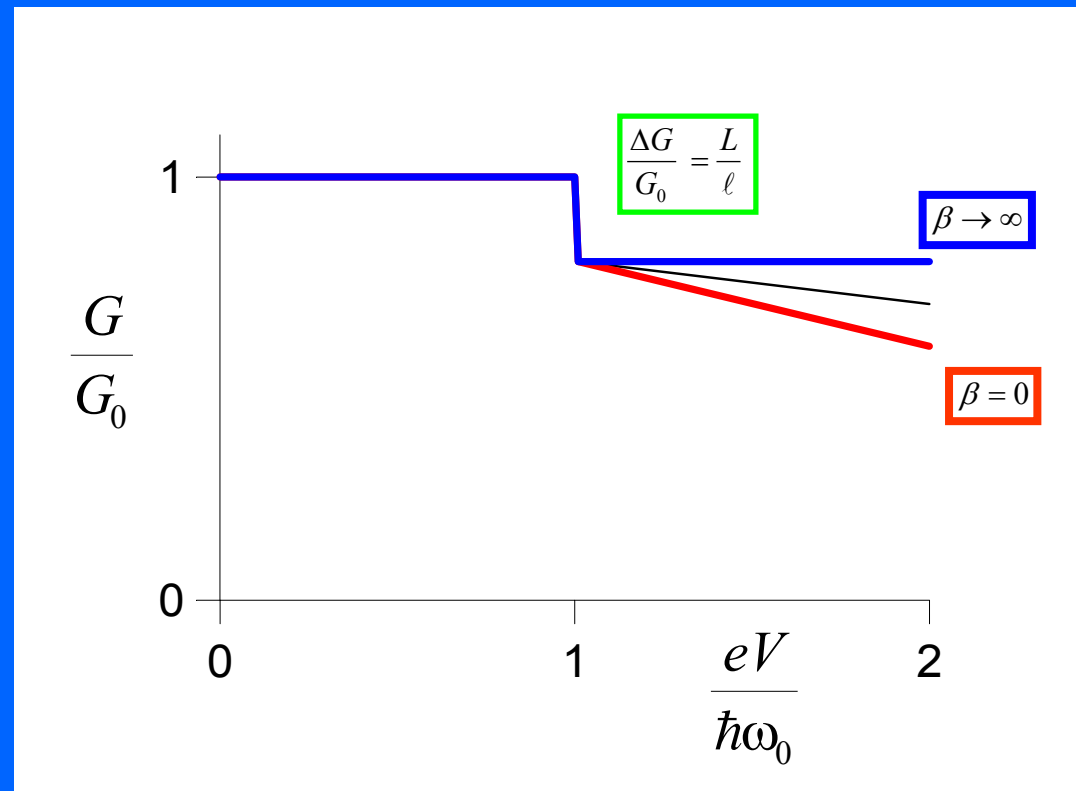
$$P_k^{ab} = \frac{L}{\ell} n_{q_{\max}}$$

$$\text{for } \varepsilon_k - \varepsilon_F > 0$$

At  $T = 0$ , the phonon population  $n_q$  is zero and only emission is possible

The conductance of the chain is

$$\frac{G}{G_0} = 1 - (P_k^{em} + P_k^{ab})$$



# e-ph interaction in atomic chains of different lengths

increasing length:

- peak height increases (linearly)
- frequency is unaffected

stretch:

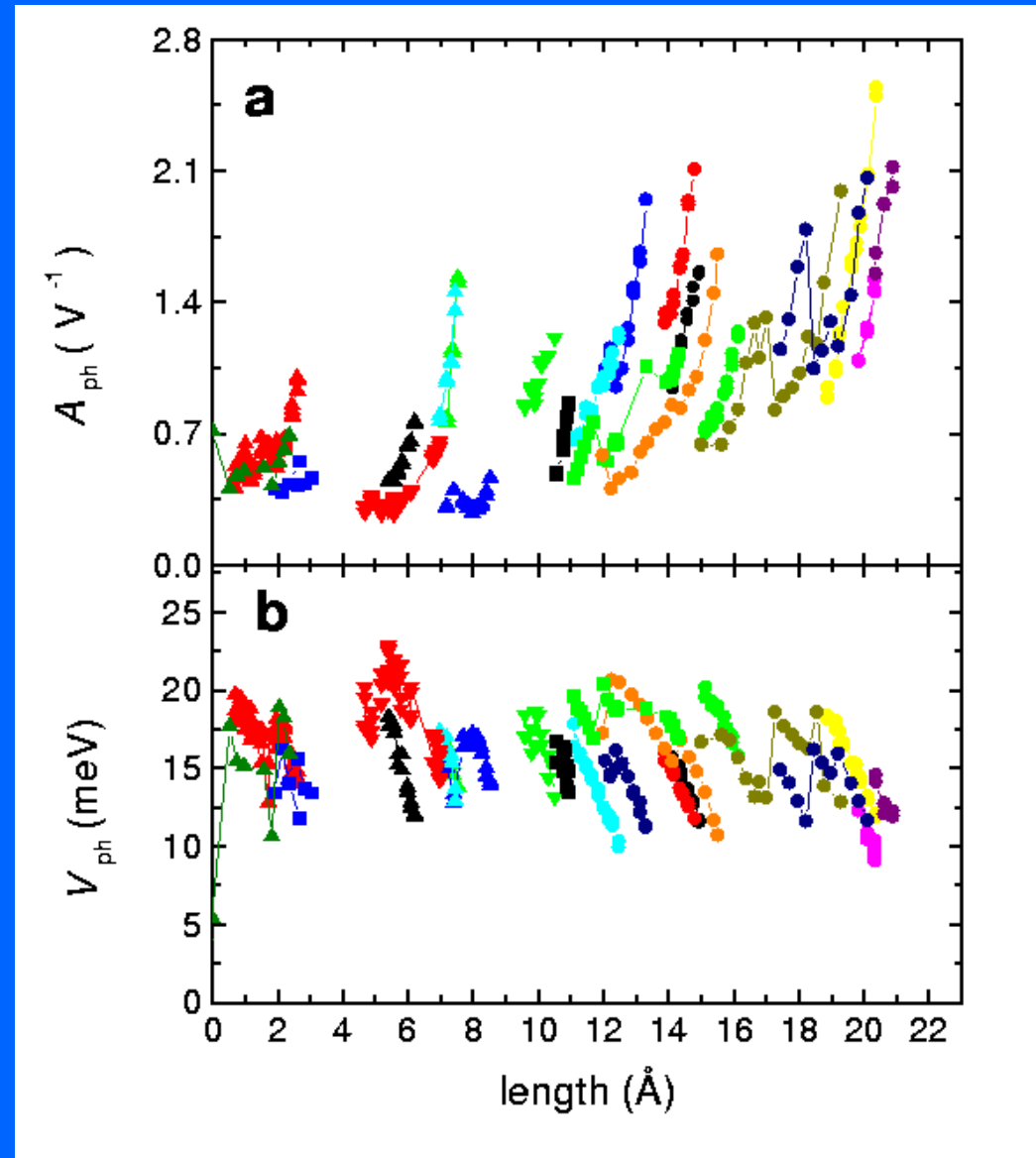
- peak height increases
- frequency decreases

## Observed frequencies

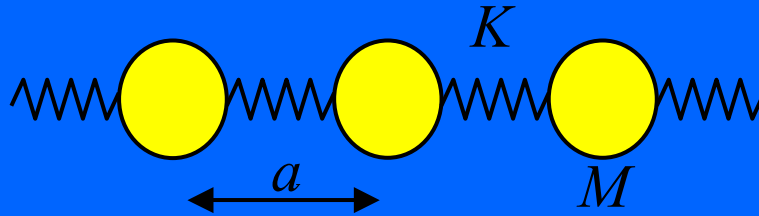
10 - 22 meV (2.3 - 5.3 THz, 80 - 180  $\text{cm}^{-1}$ )

## Interatomic bond elastic constant

$4K = m\omega^2 = 90 - 18 \text{ N/m}$



# dependence on length and frequency



$2k_F$  - mode

$$u_j = A \cos j\pi \cos \omega t$$

$$E_{kin} = \frac{1}{2} M \omega^2 A^2 N$$

quantization

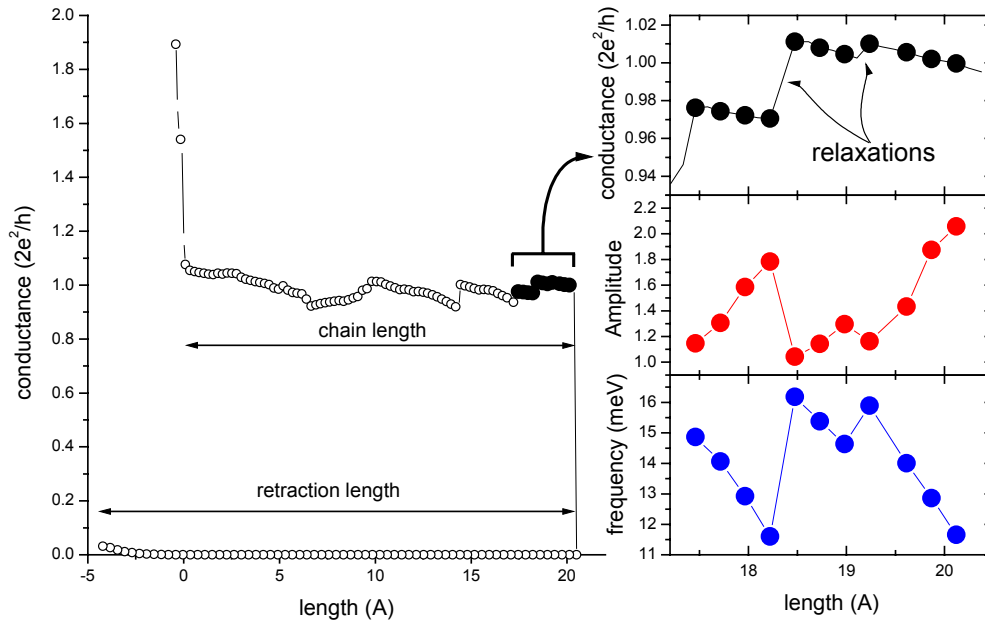
$$E_{kin} = \hbar \omega$$

$$A = \sqrt{\frac{2\hbar}{M\omega N}}$$

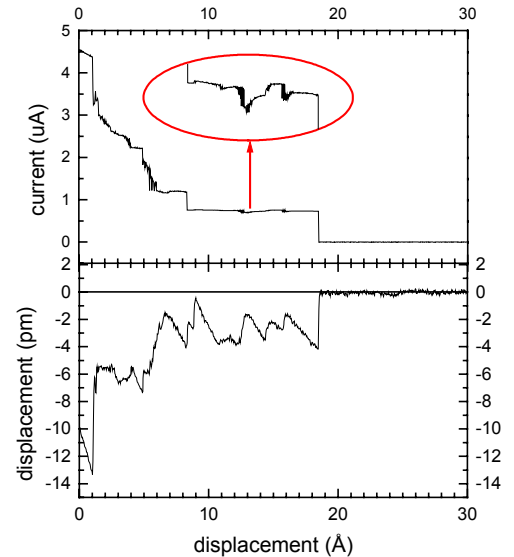
scattered wave  $\sim AL$

$$\text{scattered current} \sim A^2 L^2 = \frac{2\hbar a}{M} \frac{L}{\omega}$$

# mechanical relaxations and phonons



elastic stages (linear)  
+ atomic rearrangements  
(relaxation)



force relaxation  $\Rightarrow$  amplitude and frequency  
relaxations



## Au atomic chains

- Very stable at low temperature
- One quantum channel (Au)
- Enormous current densities
- Strength interatomic bonds: stronger than bulk
- Stiffness of interatomic bonds
- Vibrational modes
- Electron-phonon interaction

# Future work

- Formation mechanisms
- Equilibrium structure
- Dissipation and heat conduction at the nanoscale
- Coupling of mechanical and electrical properties
- Influence of adsorbates on transport
- Stability against Peierls distortions
- Hybrid chains