

Transport through Quantum Rings and Dots

Rolf J. Haug

U.F. Keyser, C. Fühner, M. Rogge, J. Regul, A. Nauen, F. Hohls

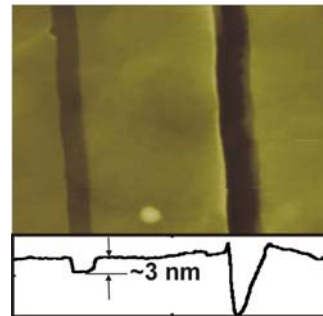
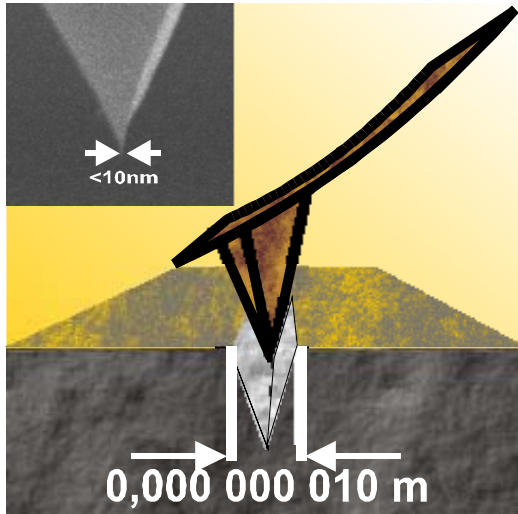
**Abteilung Nanostrukturen
Institut für Festkörperphysik
Universität Hannover
Germany**

Overview

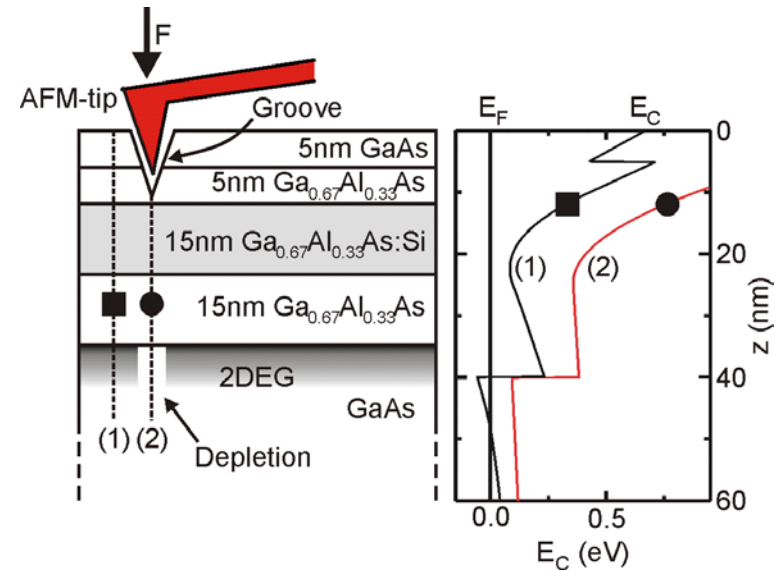
- **Direct writing with an atomic force microscope (AFM)**
- **Transport through a quantum ring: Aharonov-Bohm effect**
- **Coulomb blockade, Kondo, fractional Aharonov-Bohm effect, Fano effect**
- **more quantum-dot physics**

Surface Modification with an AFM

- nanomachining



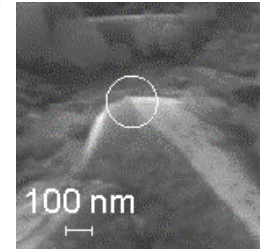
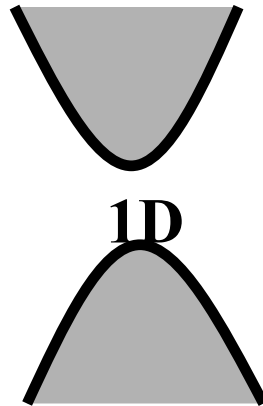
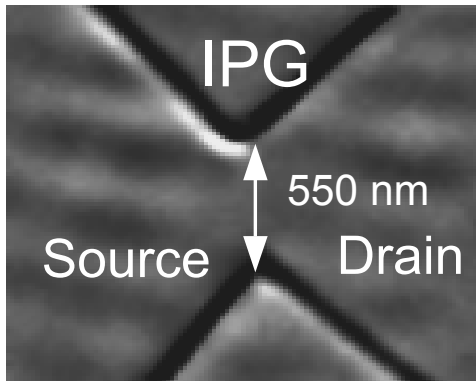
application:
GaAs/AlGaAs heterostruktur



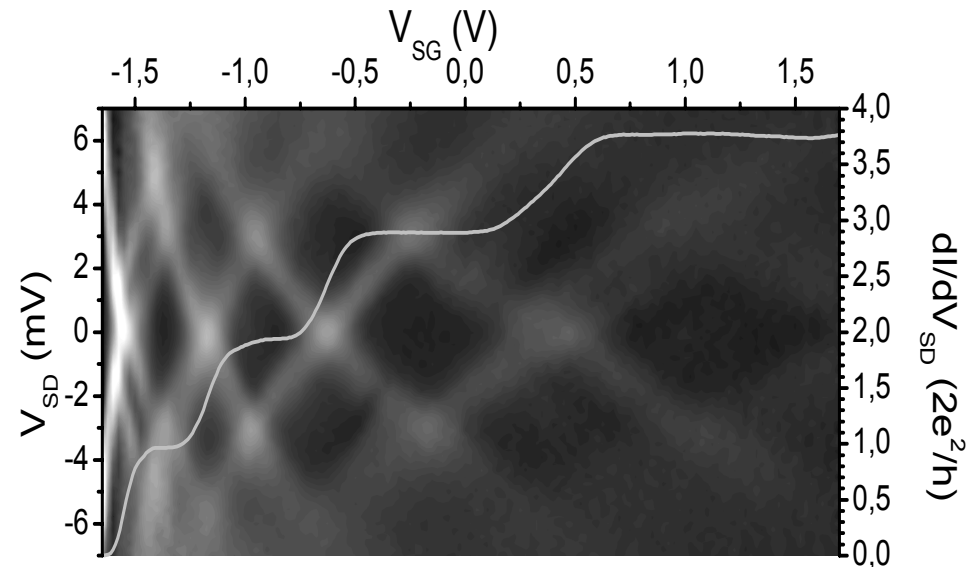
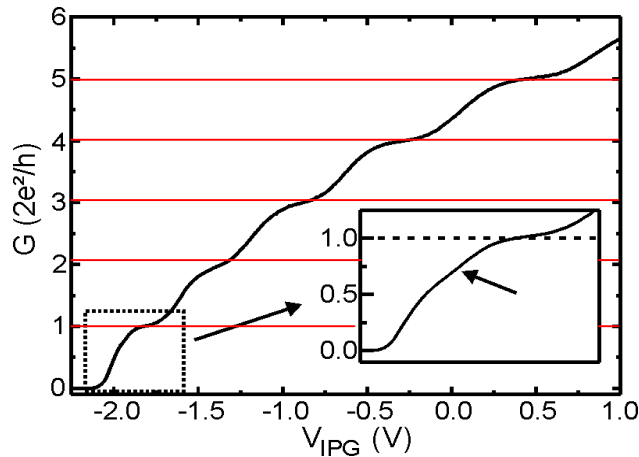
Appl. Phys. Lett.
75, 1107 (1999)

Nanomachining of a Point Contact

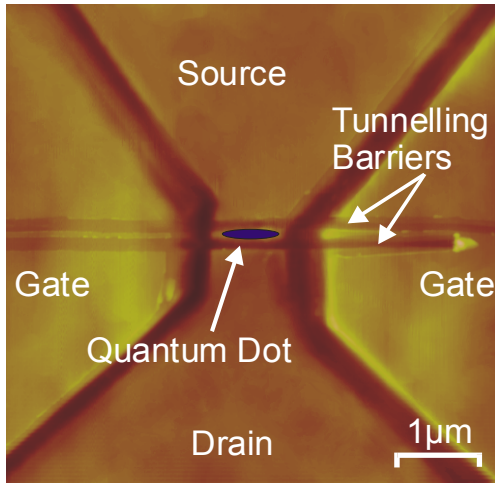
(with diamond tip!)



Appl. Phys. Lett.
81, 2023 (2002)



Nanomachining of a 0d System

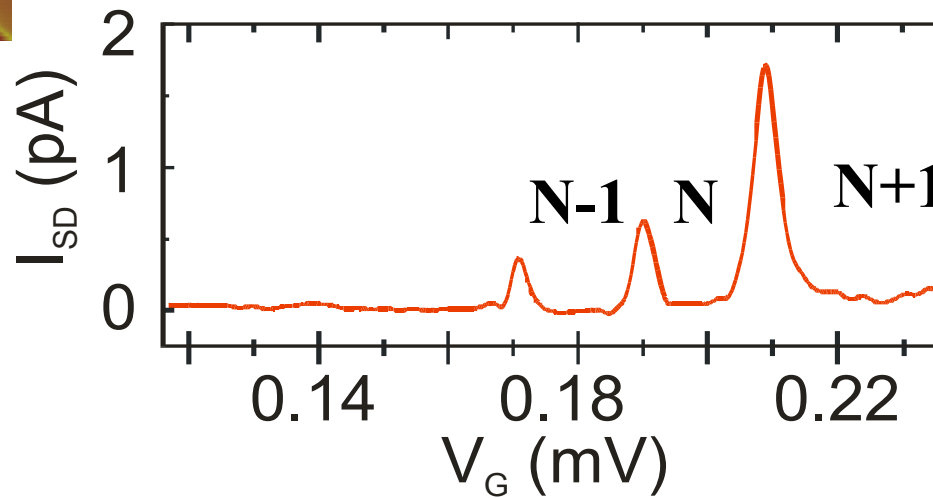
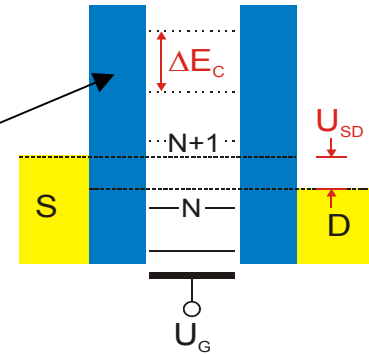


Appl. Phys. Lett. 1999

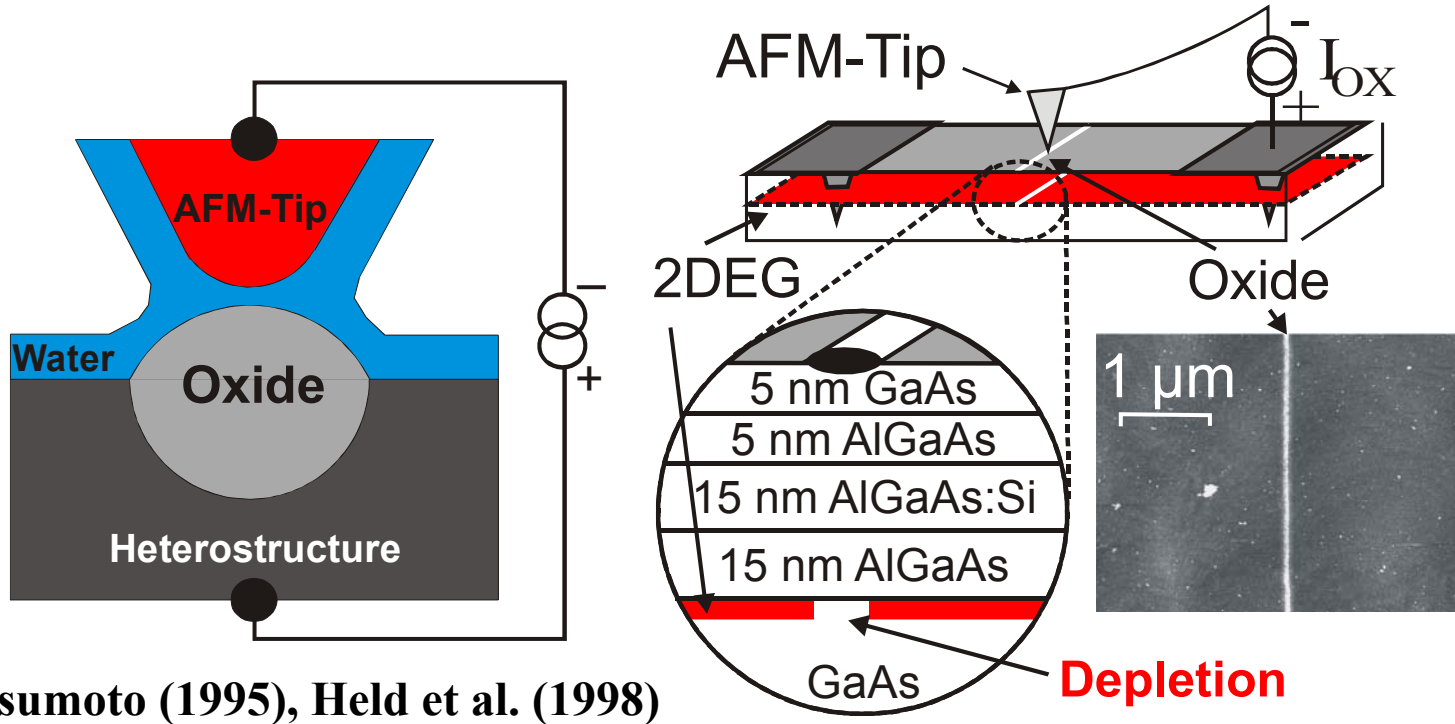
single-electron
transistor

$$\Delta E_c = \frac{e^2}{C}$$

Coulomb blockade

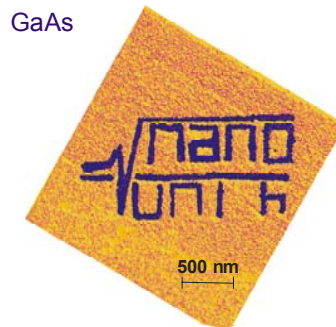
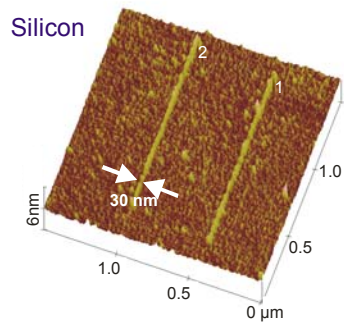


Local Oxidation

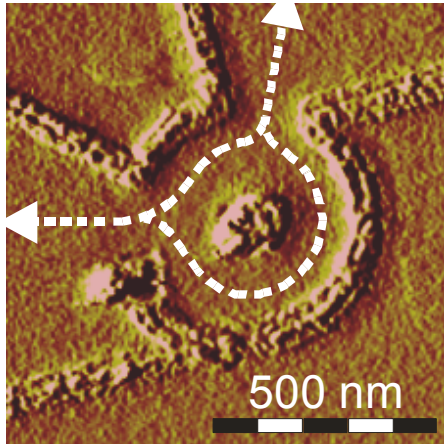


Ishii, Matsumoto (1995), Held et al. (1998)

Appl. Phys. Lett. 76,457 (2000)

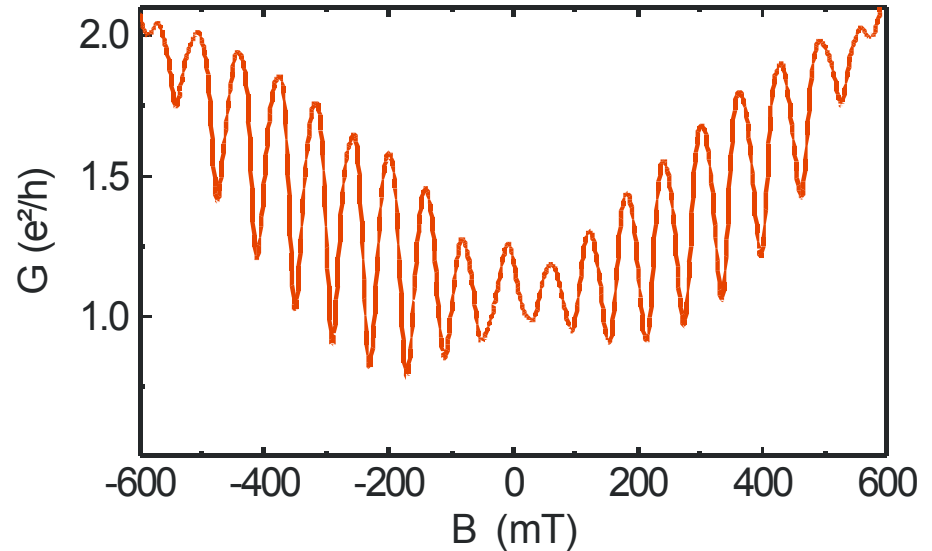


A Quantum Ring

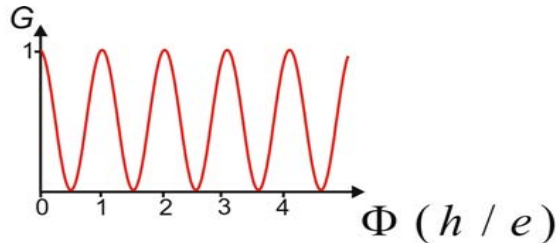
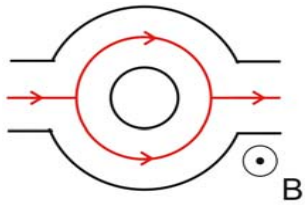


Semicond. Sci. Techn. 2002

see also Fuhrer et al. Nature 2001



Aharonov-Bohm effect



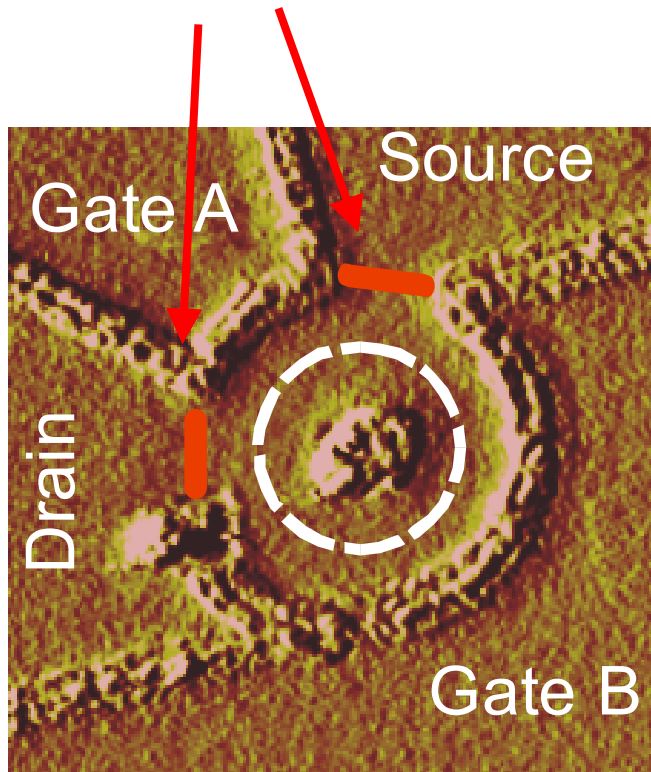
Periodicity 58mT: R=150nm

**up to 50% modulation of the
conductance**

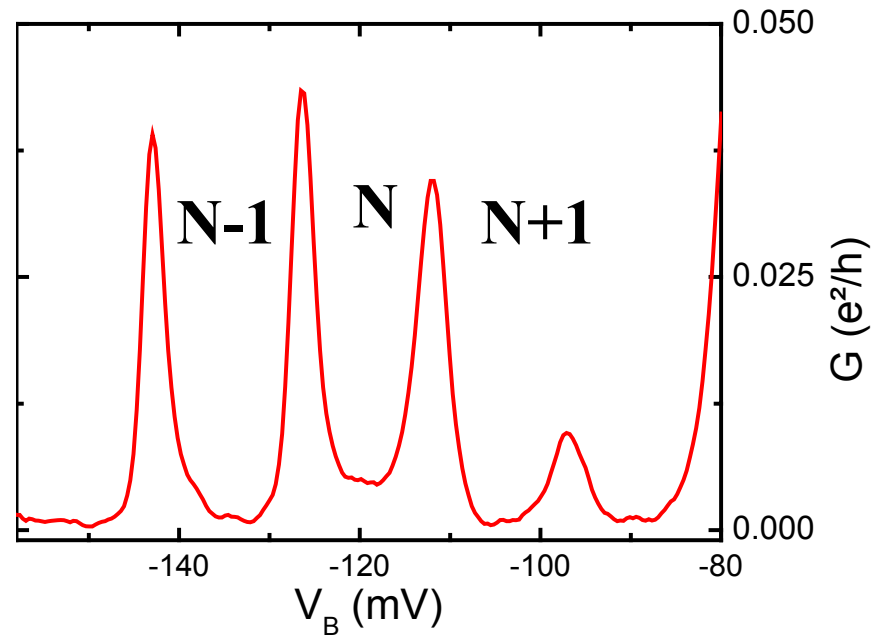
one 1d channel transmitted

Tunable Quantum Ring

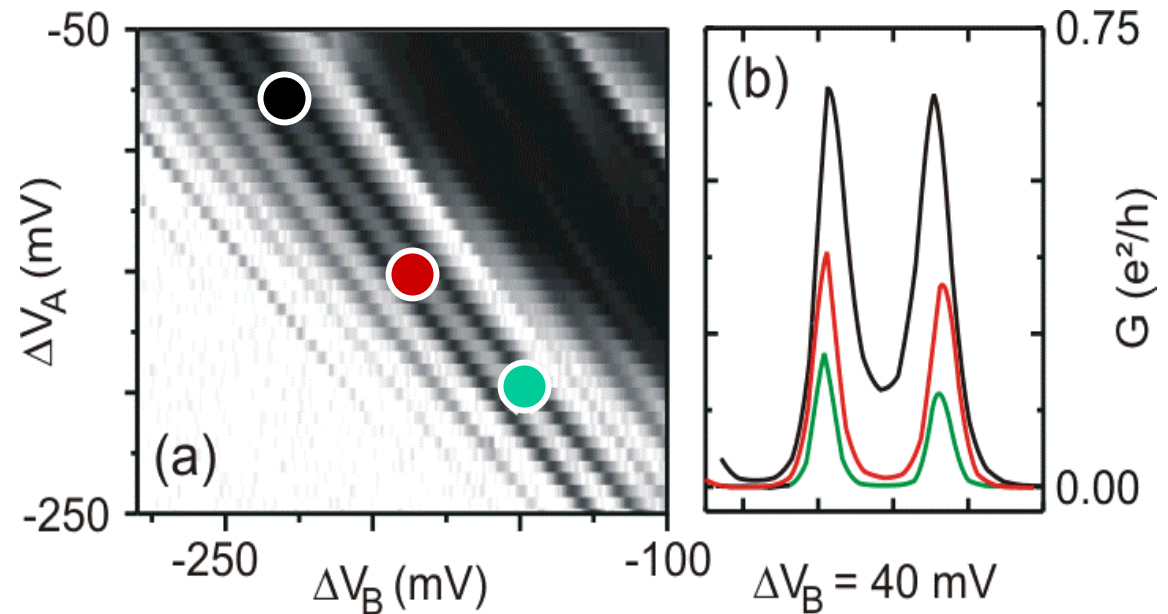
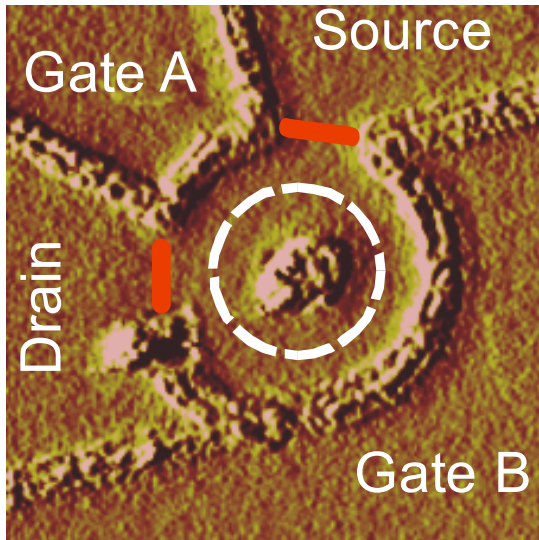
barriers



Coulomb blockade and single-electron tunneling



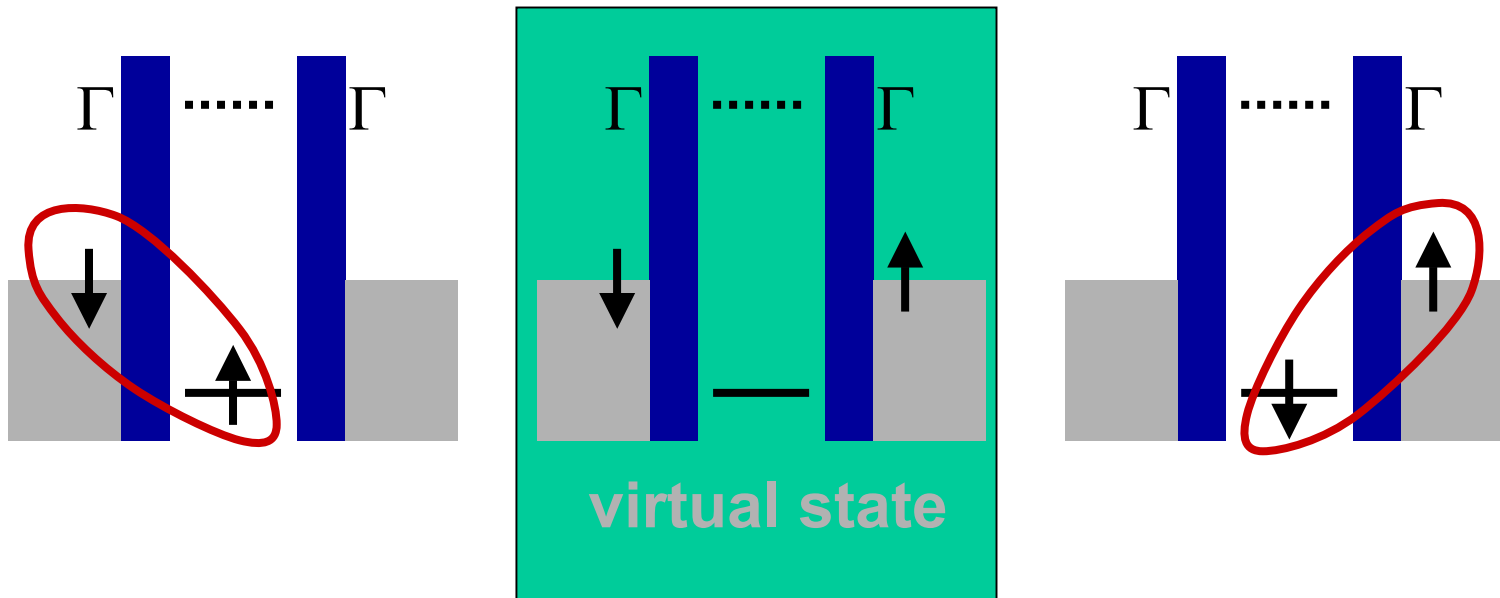
Quantum Ring as Quantum Dot: Variation of Coupling



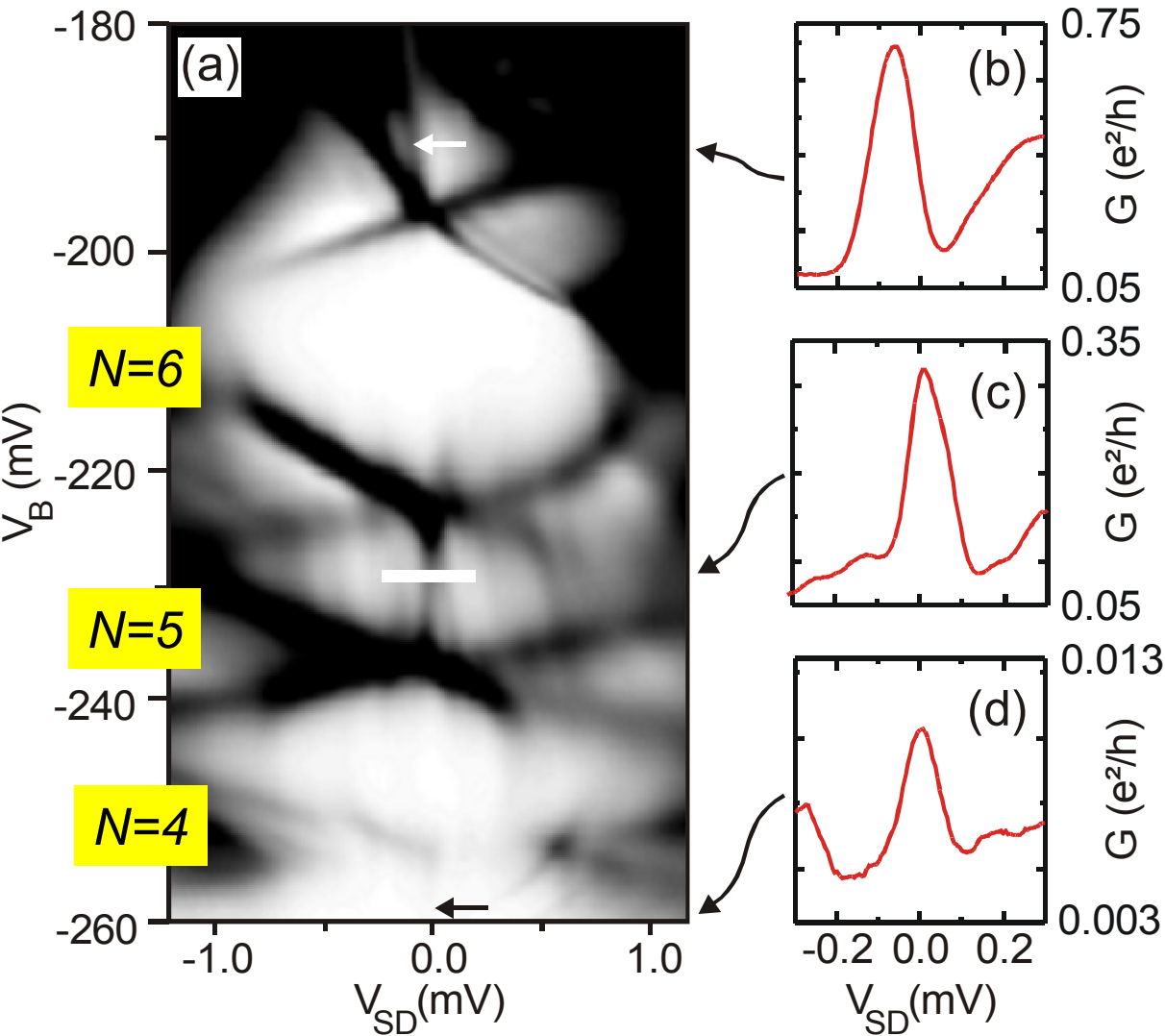
variation of conductance in the Coulomb-blockade regime

Kondo Effect

- quantum dot in a degenerate state
- formation of a spin singlet with the states in the lead
- increased conduction in the Coulomb-blockade regime



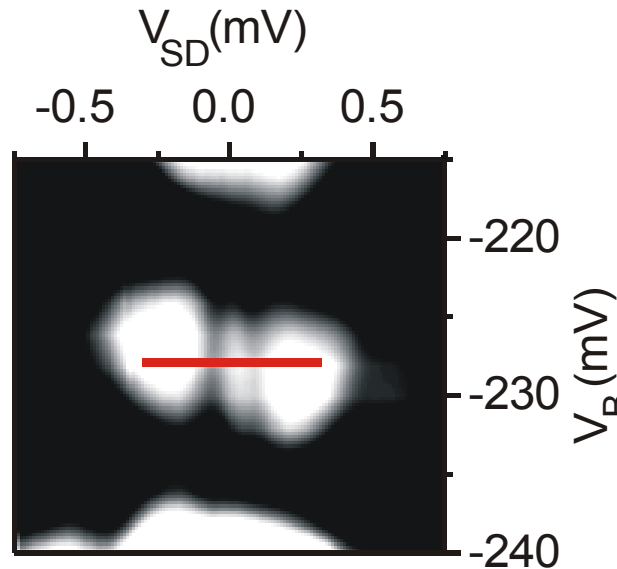
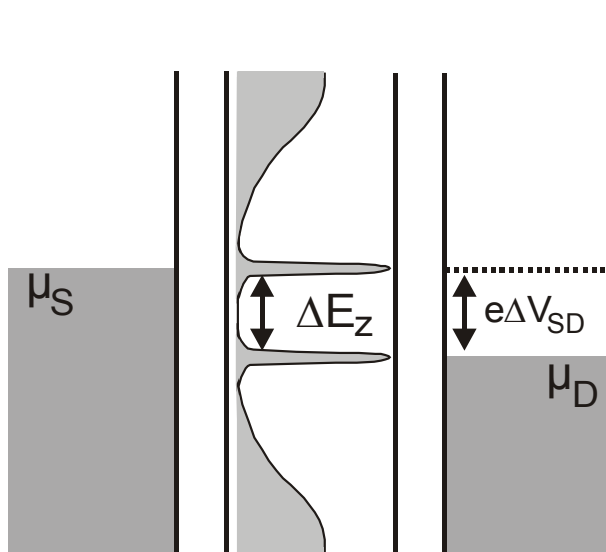
Influence of Number of Electrons



- **zero-bias anomaly**
- **spin-1/2 Kondo effect (for odd number of electrons)**

Keyser *et al.*, cond-mat/0206262

Splitting with Magnetic Field

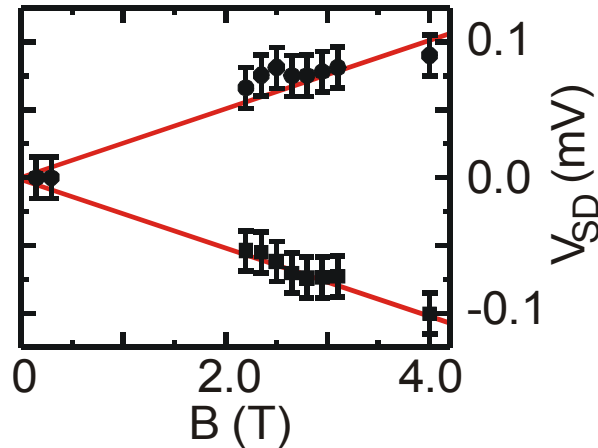
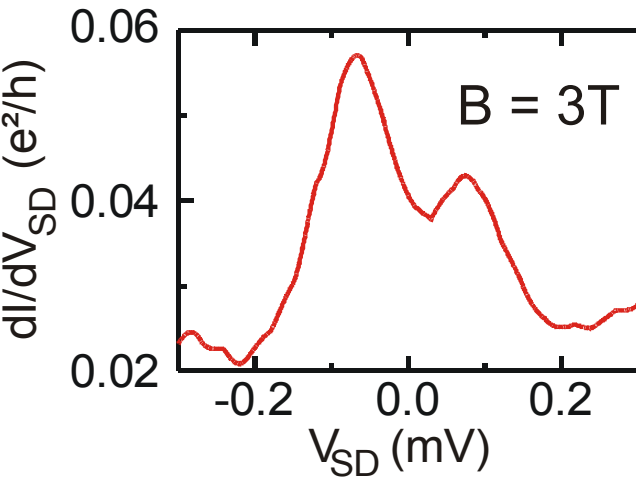


- **Kondo resonance splits with applied magnetic field B**

- **Observed splitting fits for spin 1/2**

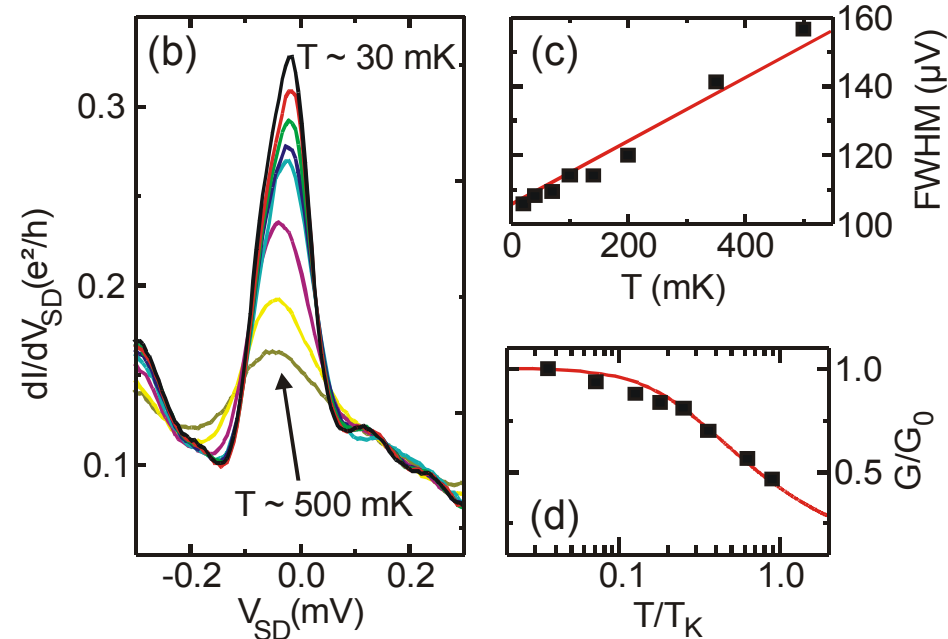
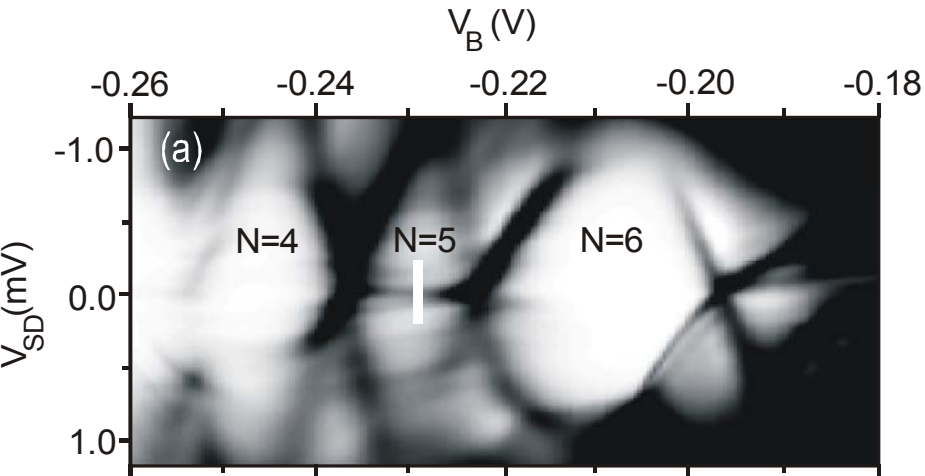
$$eV_{SD} = \pm g_{GaAs} \mu_B B$$

$$g_{GaAs} = -0.44$$



- **For $B < 2$ T no spin splitting observed**
- **Probably caused by high T_K**

Temperature Dependence



- zero-bias peak
- vanishes for increasing temperature
- splits in a magnetic field
- empirical fit

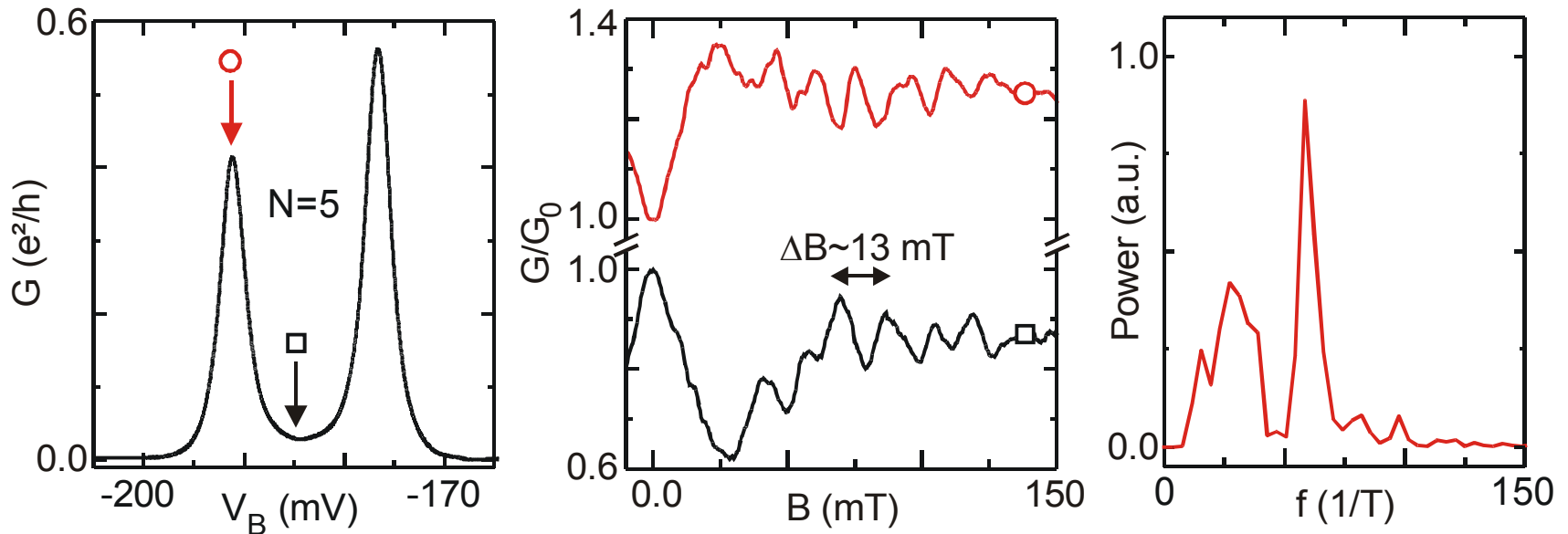
$$G(T) = G_0 \left(\frac{T_K'^2}{T^2 + T_K'^2} \right)^s$$

Goldhaber-Gordon **PRL81** (1998)

- $T_K \sim 600$ mK

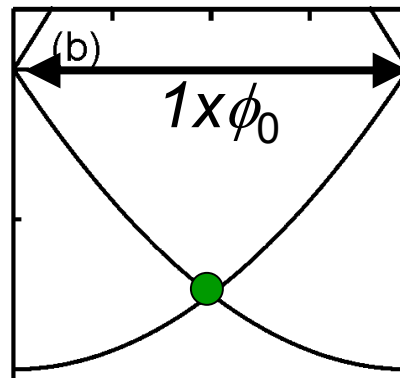
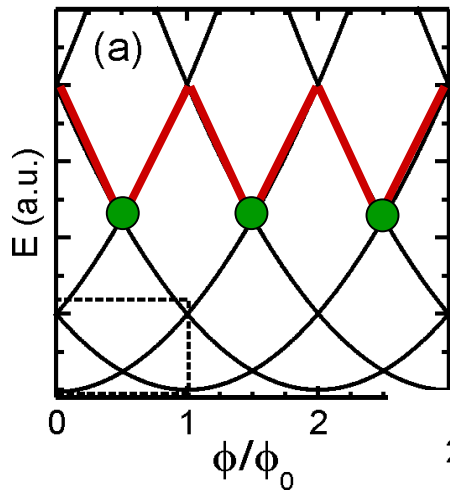
cond-mat/0206262

Influence of a Weak Magnetic Field



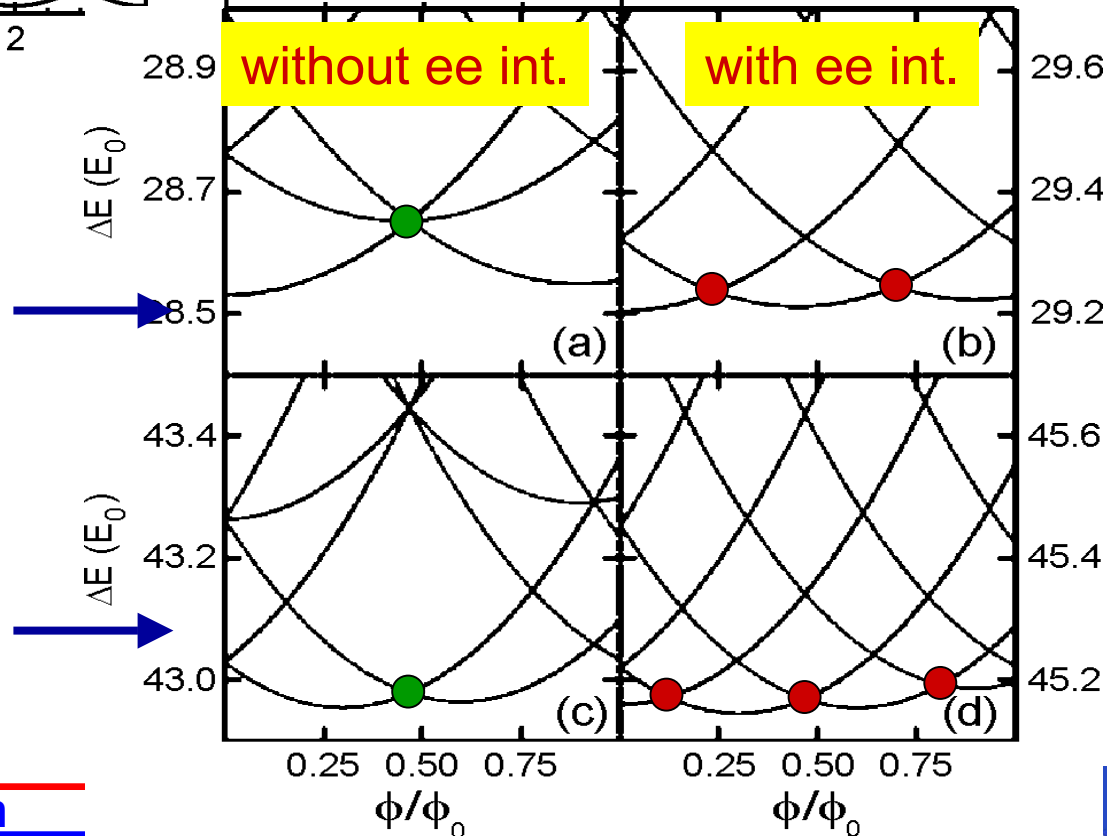
- oscillations with $\Delta B \sim 13$ mT
- Aharonov-Bohm periodicity: $\Delta B = 58$ mT

Ground States of a Quantum Ring



← single-particle levels:
 $E \sim (l + m)^2$

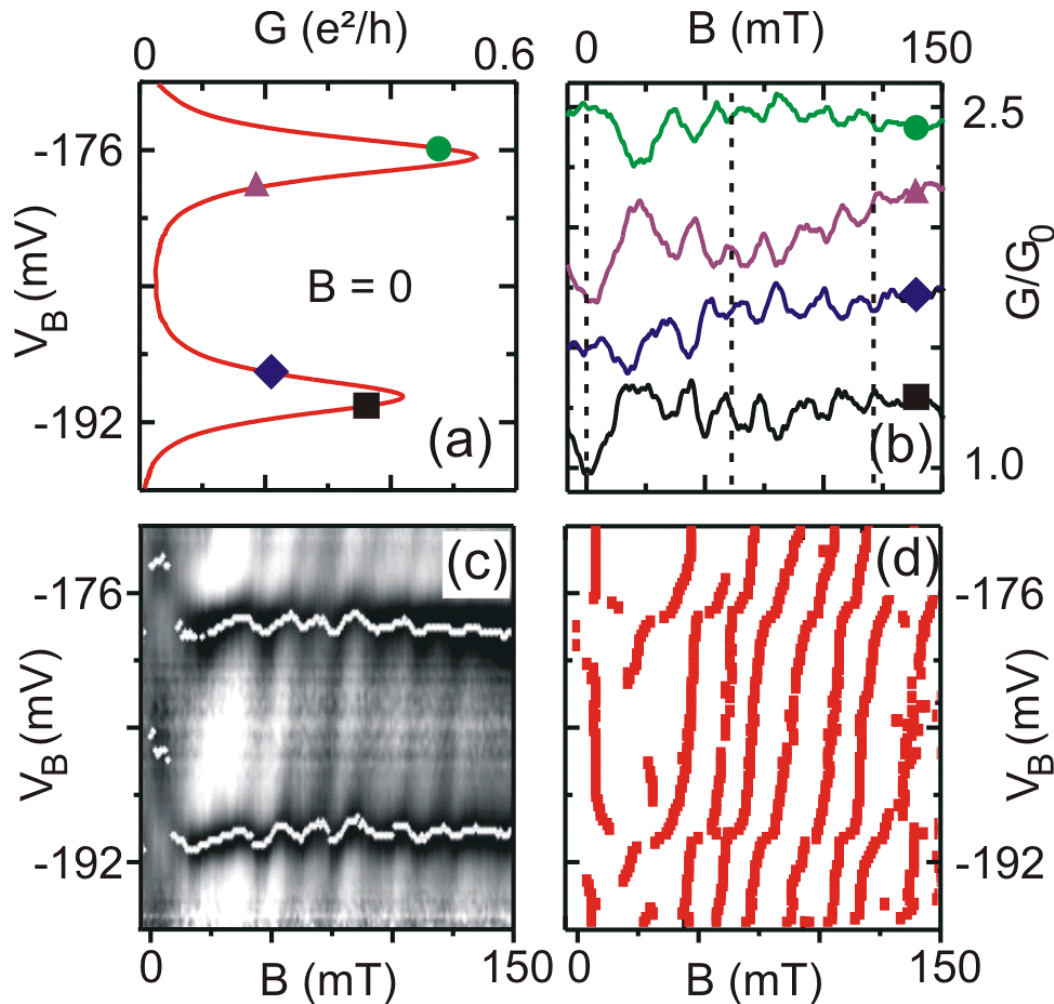
$N=2$ electrons



$\Delta B \sim 1/N$

Niemelä *et al.*,
 EPL36 (1996)

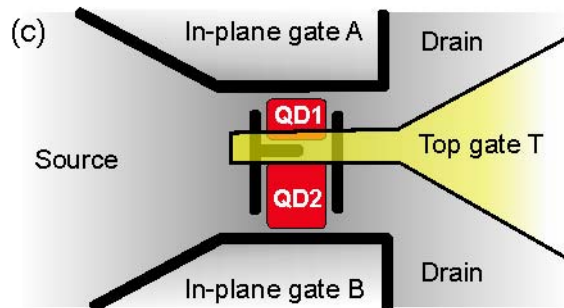
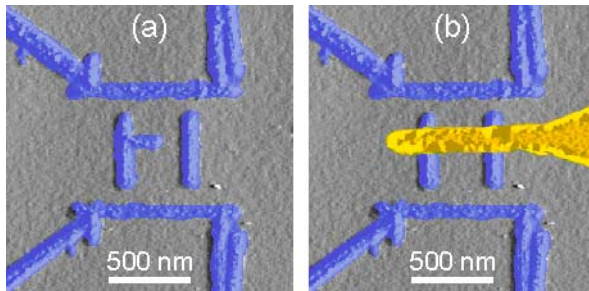
Fractional Aharonov-Bohm Effect



- **Kondo effect: oscillations visible in the Coulomb-blockade regime**
- **phase jumps at the resonances**

Combination of AFM and E-Beam

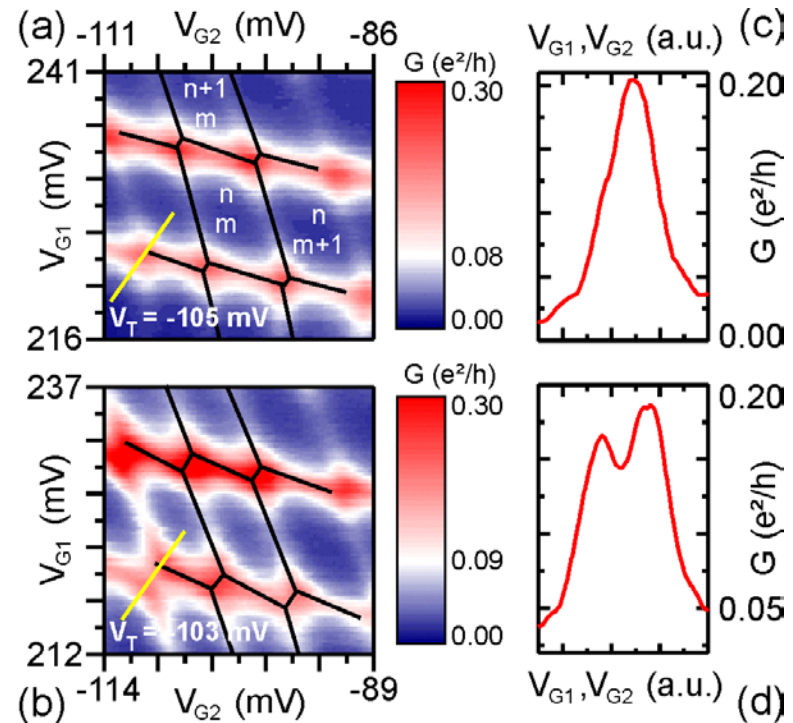
coupled quantum dots



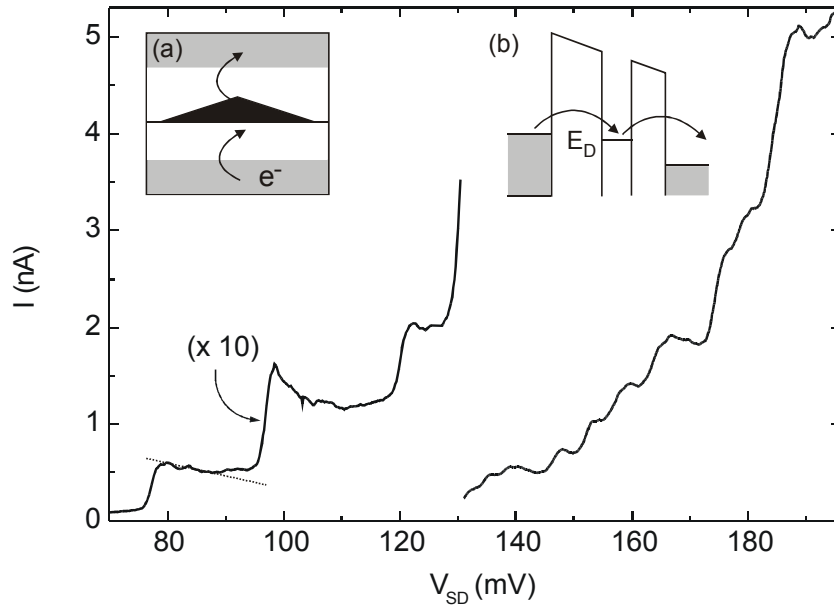
tunability

Phys. Rev. Lett. 80,
4032 (1998)

Phys. Rev. Lett. 81,
689 (1998)

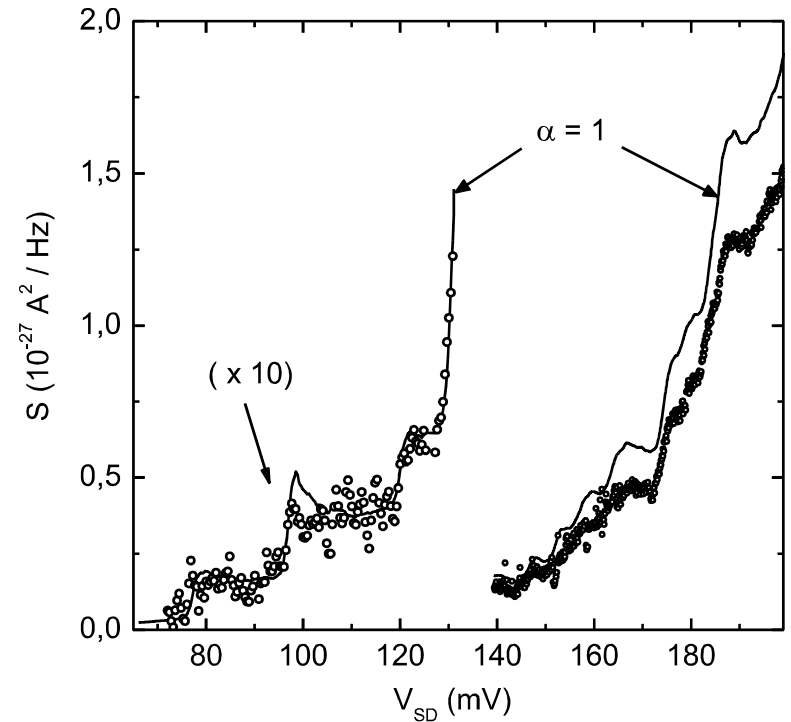


Noise measurements on InAs quantum dots



Phys. Rev. B 66, 161303R (2002)

shot noise:



Poster F. Hohls

Quantum Dot as Spectrometer

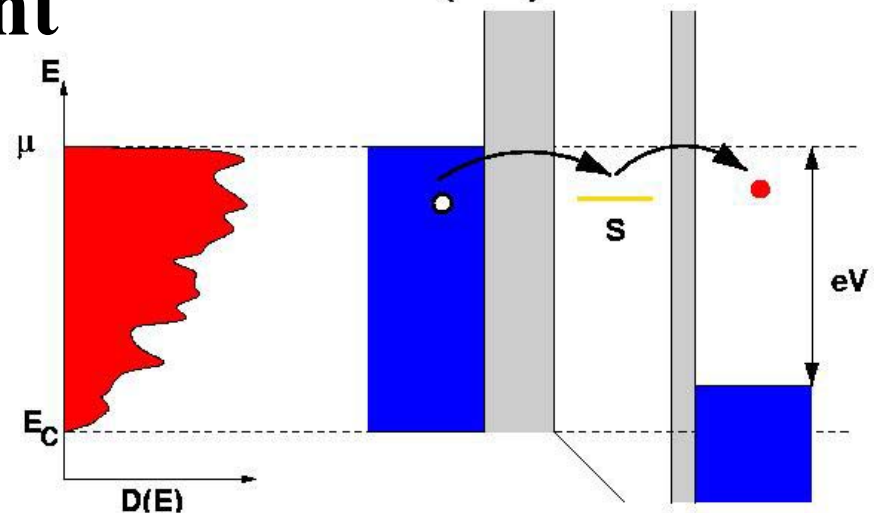
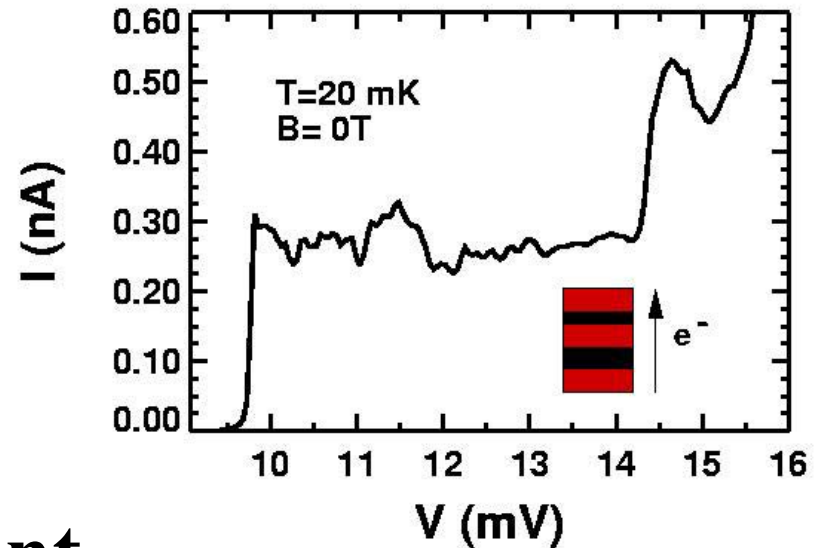
quantum dot:
extension of
lowest state: 10nm

→ local spectrometer
of emitter states

fluctuations in the current

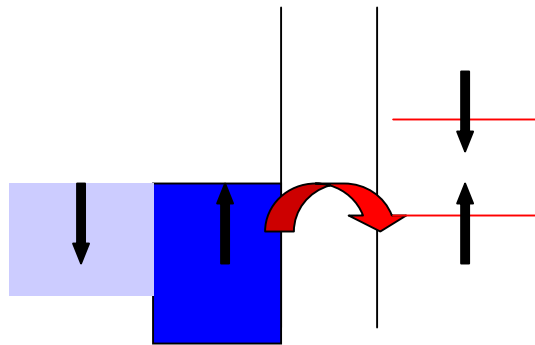
→ fluctuations of
local density of states

Europhys. Lett. 36, 61 (1996)
Phys. Rev. Lett. 78, 1540 (1997)
Phys. Rev. Lett. 86, 276 (2001)
Europhys. Lett. 54, 495 (2001)
Phys. Rev. B 2002



Spin-Resolved Tunneling through Quantum Dots

spin-resolved spectroscopy
of the local density of states



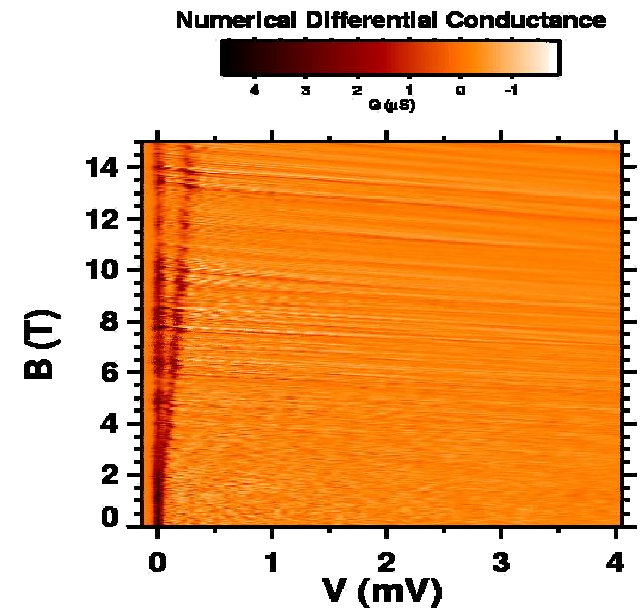
$$g = 0.14$$

Europhys. Lett. 54, 495 (2001)

 spin-polarized current

Zeeman energy

$$\Delta = g\mu_B B$$



Summary

- **nanotechnology with AFM**
- **quantum rings:**
Aharonov-Bohm effect,
Kondo effect,
Fano effect,
fractional Aharonov-Bohm effect
- **quantum dots**