

# Transport properties of diluted magnetic semiconductor ferromagnets

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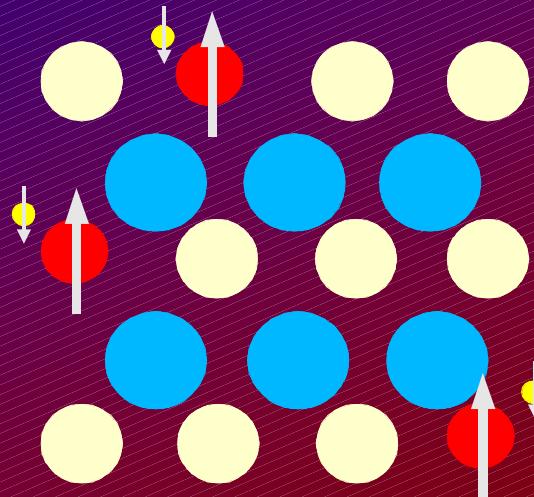


# Hole-mediated ferromagnetism

Tomasz Dietl *et al.*:  
(Phys. Rev. B '97)

- Analogy with (II,Mn)VI

diluted magnetic semiconductors

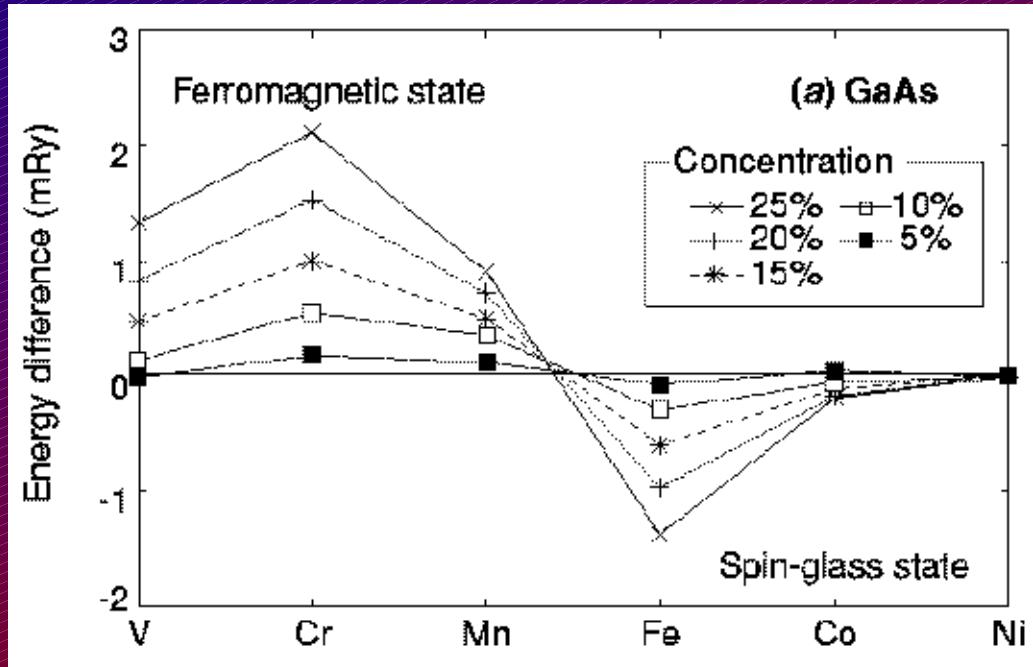


- Plus Mn is an acceptor in (III,Mn)V

MANGANESE	54.938	IF
Mn	25	7
[Ar] 3d <sup>5</sup> 4s <sup>2</sup>		
8.89	6.3	2
15.78	400	1
TECHNETIUM	98.91	R

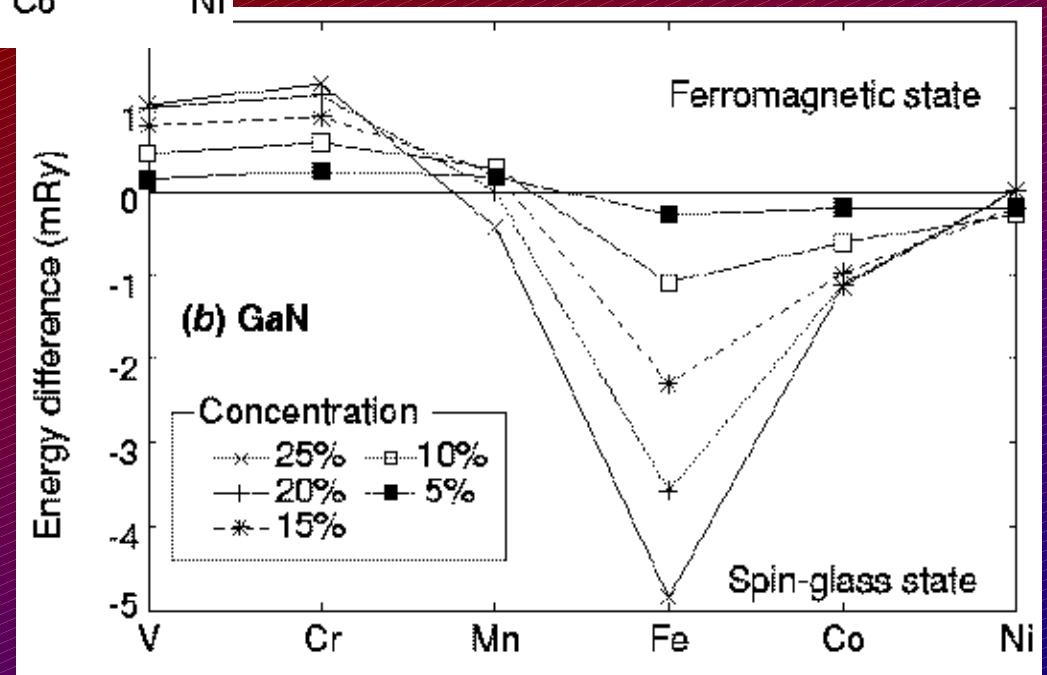
ZINC	65.38	GALLIUM	69.72	GERMANIUM	72.59	ARSENIC	74.922	SELENIUM	78.96
7.14	<b>Zn</b> 30	5.91	<b>Ga</b> 31	5.32	<b>Ge</b> 32	5.72	<b>As</b> 33	4.79	<b>Se</b> 34
	[Ar] 3d <sup>10</sup> 4s <sup>2</sup>		[Ar] 3d <sup>10</sup> 4s <sup>2</sup> 3p <sup>1</sup>		[Ar] 3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>2</sup>		[Ar] 3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>3</sup>		[Ar] 3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>4</sup>
2.66	HEX 1.856	4.51	ORC 1.695 1.001	5.66	DIA	4.13	RHL 54° 10'	4.36	HEX 1.136
693	234	303	240	1211	360	1090	285	490	150 <sup>L</sup> T
CADMUIM	112.40	INDIUM	114.82	TIN	118.69	ANTIMONY	121.75	TELLURIUM	127.60
8.65	<b>Cd</b> 48	7.31	<b>In</b> 49	7.30	<b>Sn</b> 50	6.62	<b>Sb</b> 51	6.24	<b>Te</b> 52
	[Kr] 4d <sup>10</sup> 5s <sup>2</sup>		[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>1</sup>		[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>2</sup>		[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>3</sup>		[Kr] 4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>4</sup>
2.98	HEX 1.886	4.59	TET 1.076	5.82	TET 0.546	4.51	RHL 57° 6'	4.45	HEX 1.330
594	120	429.8	129	505	170	904	200	723	139 <sup>L</sup> T

# LDA ground-state



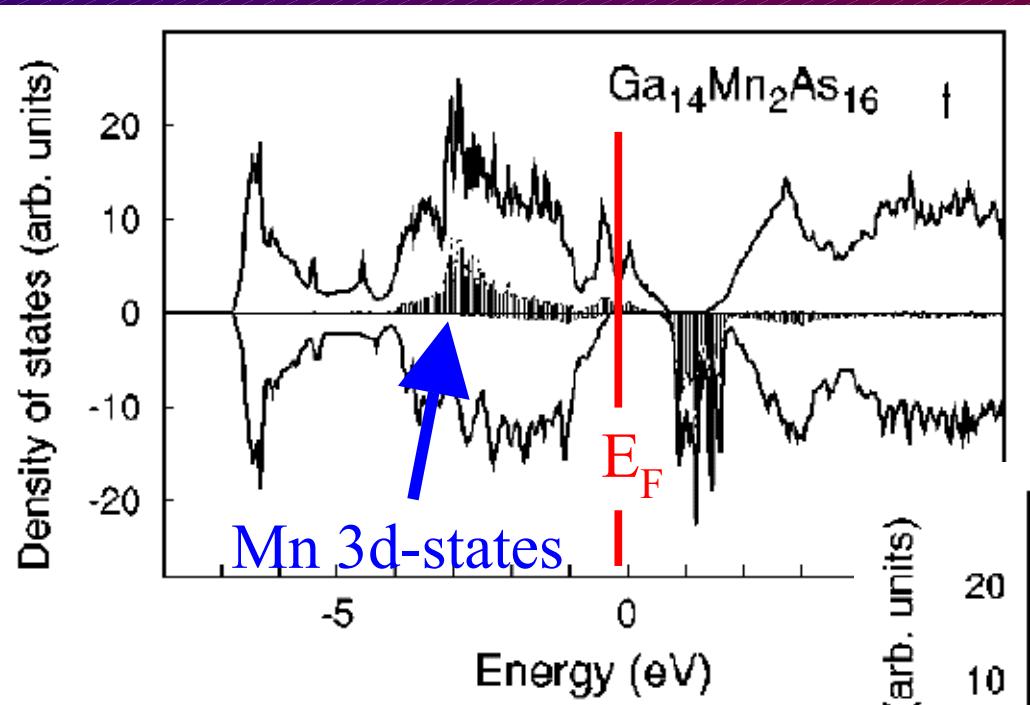
ferromagnet  
vs  
spin-glass

(K. Sato and H. Katayama-Yoshida,  
Semicond. Sci. and Technol. '02)

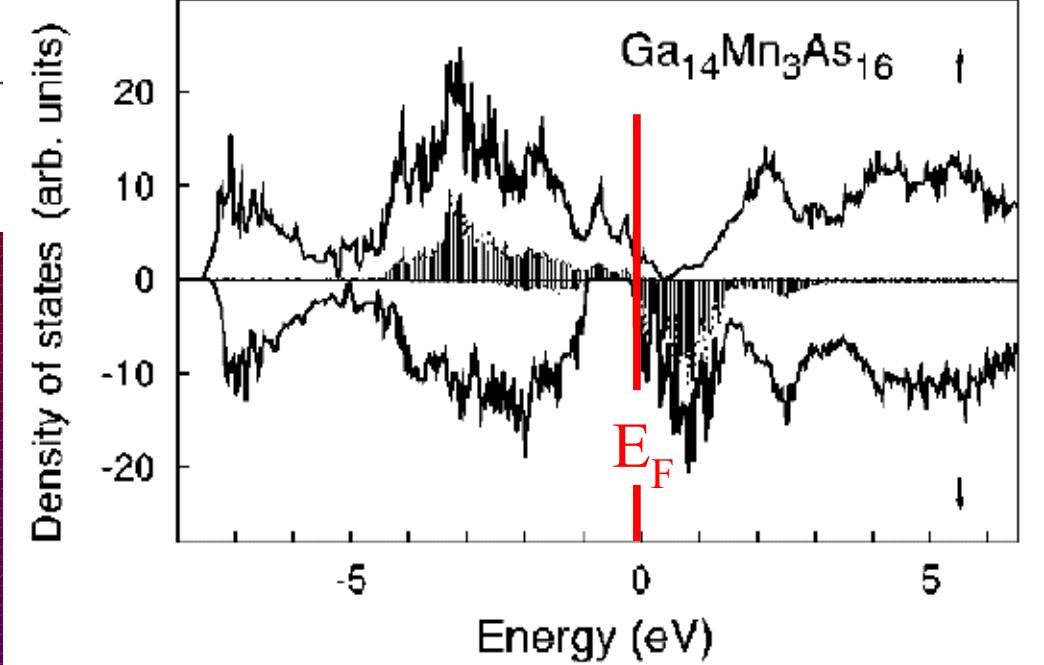


# Electronic structure

2 substitutional Mn ions

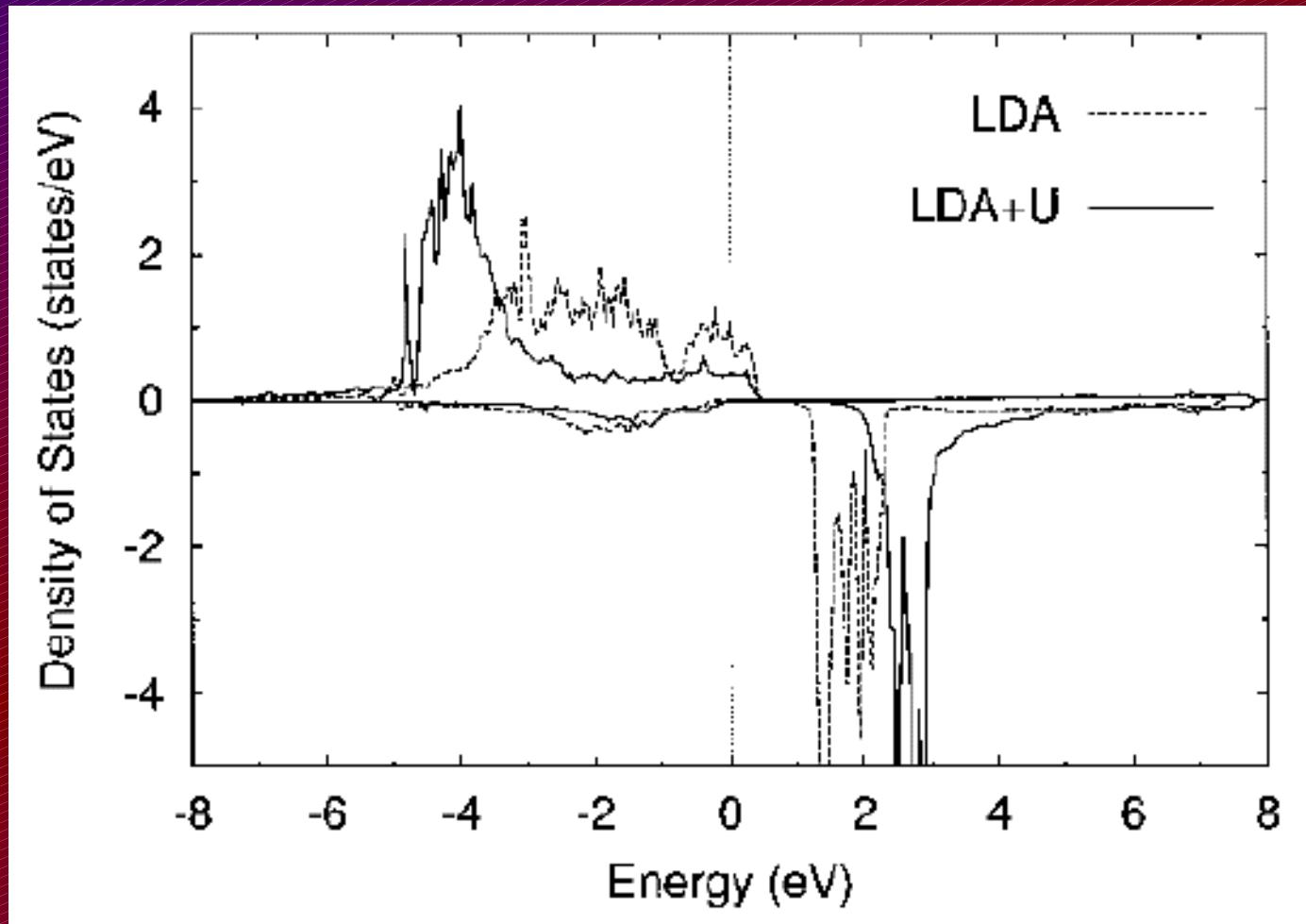


2 substitutional and  
1 interstitial Mn



(F. Máca and J. Mašek PRB '02)

# On Mn-site correlations

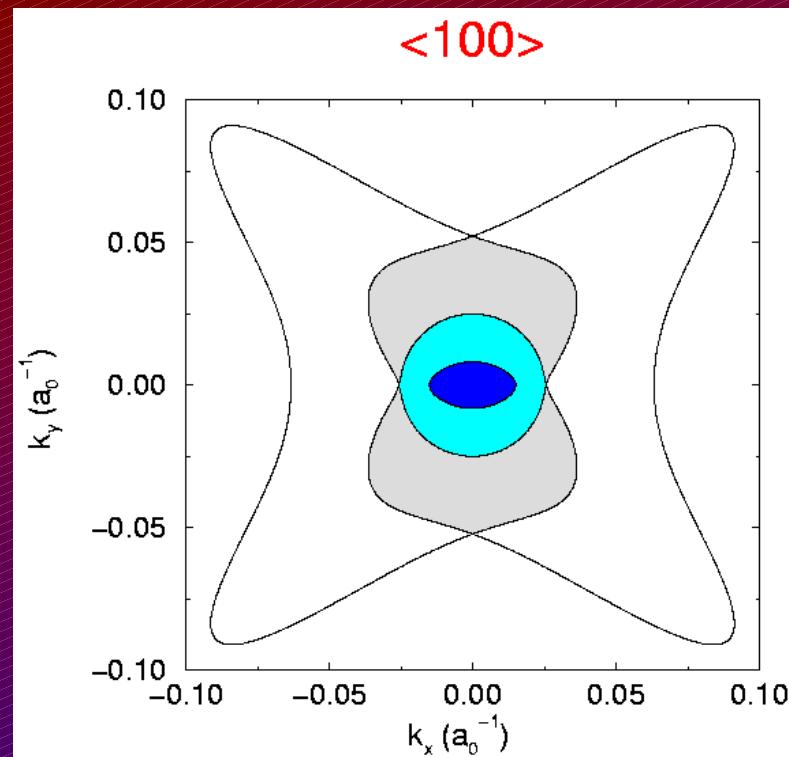


(J.H. Park, S.K. Kwon, and B.I. Min, *Physica B* '00)

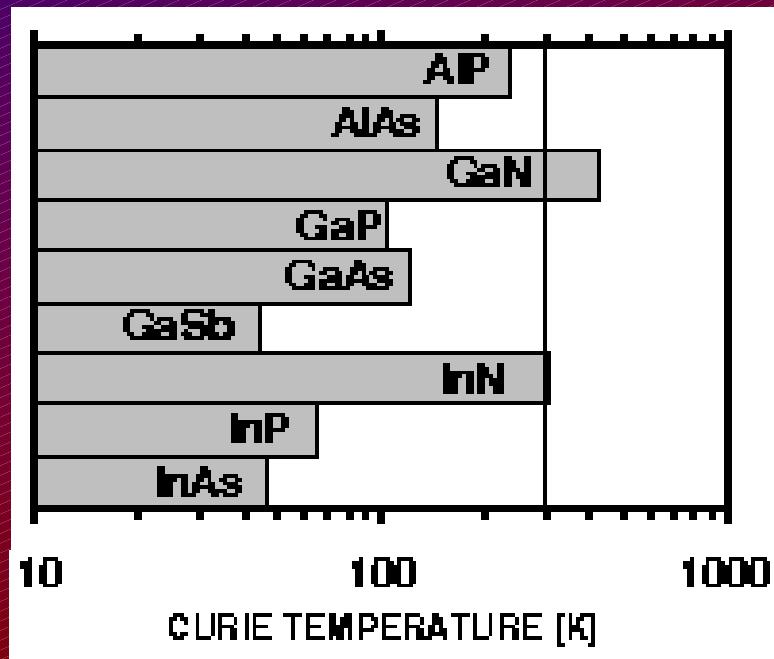
# Effective Hamiltonian theories

- Semi-phenomenological Kohn-Luttinger model for heavy, light, and spin-orbit split-off band holes
- Kondo spin Hamiltonian:  
 $\sum_i J_{pd} \mathbf{S}_i \cdot \mathbf{s}$  ; Mn:  $S=5/2$ ; valence-band hole:  $s=1/2$ ;  $J_{pd} > 0$
- Mean-field theory

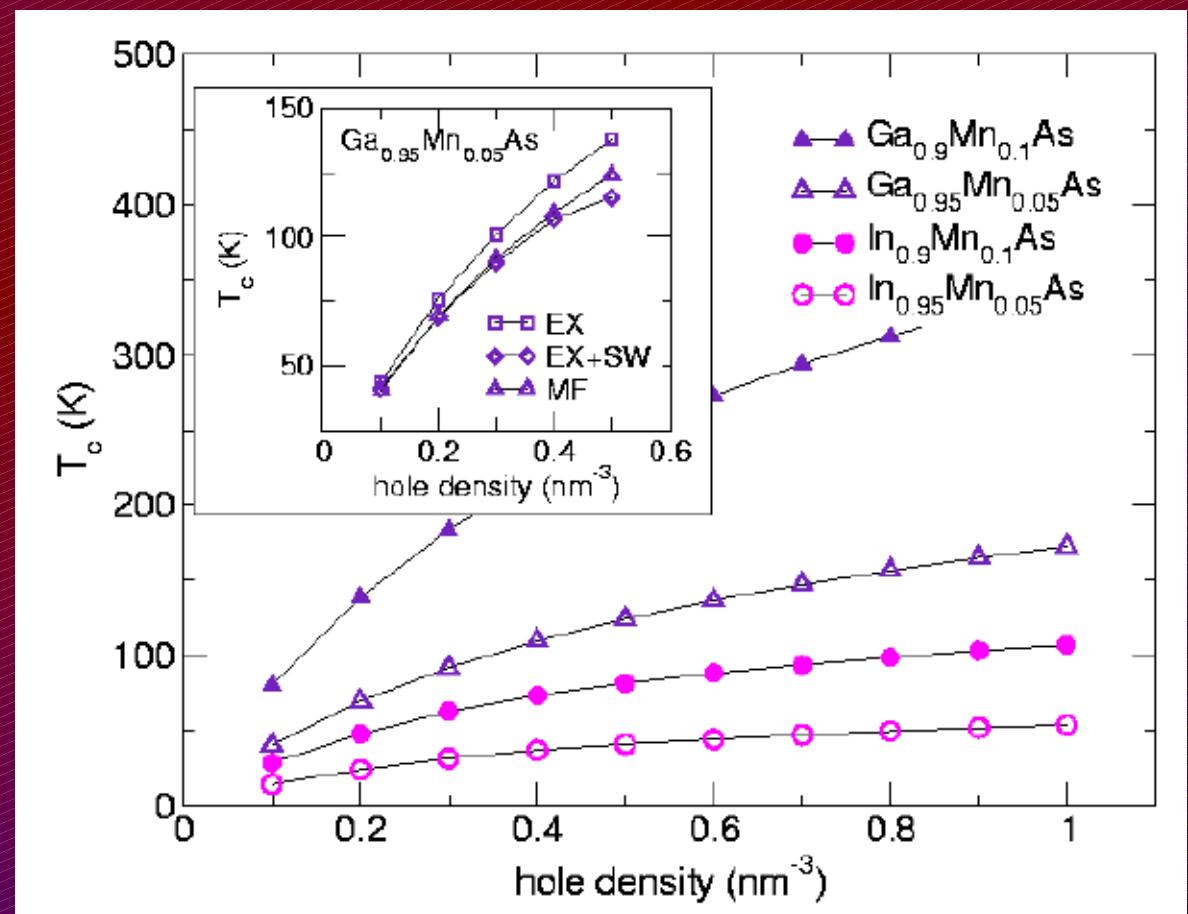
(*T. Jungwirth et al. Phys. Rev.B'99;*  
*T.Dietl et al., Science '00*)



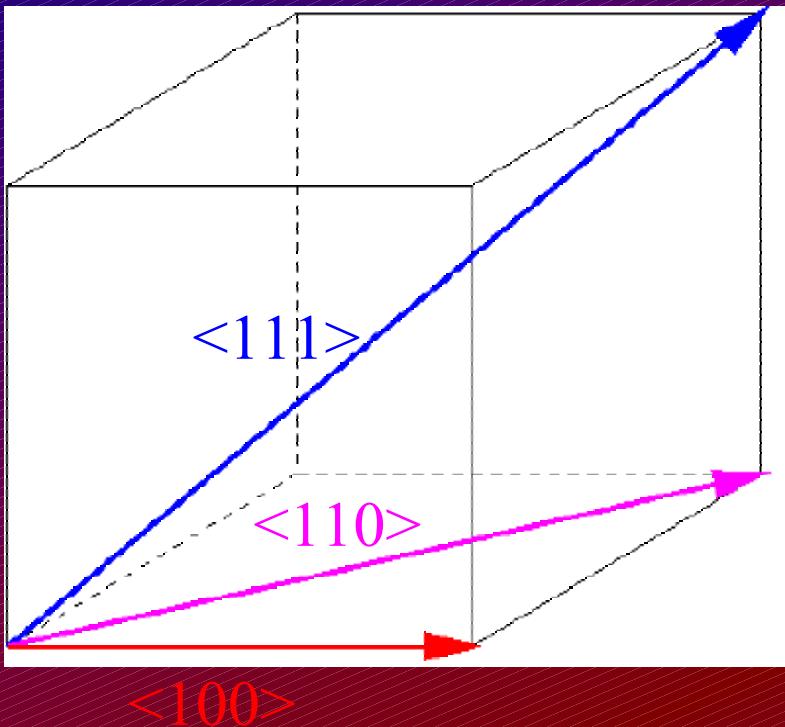
# Ferromagnetic transition temperature



(*T. Dietl, H. Ohno, T. Matsukura,  
Phys. Rev. B '01; T. Jungwirth  
et al. Phys. Rev. B '99; '02*)

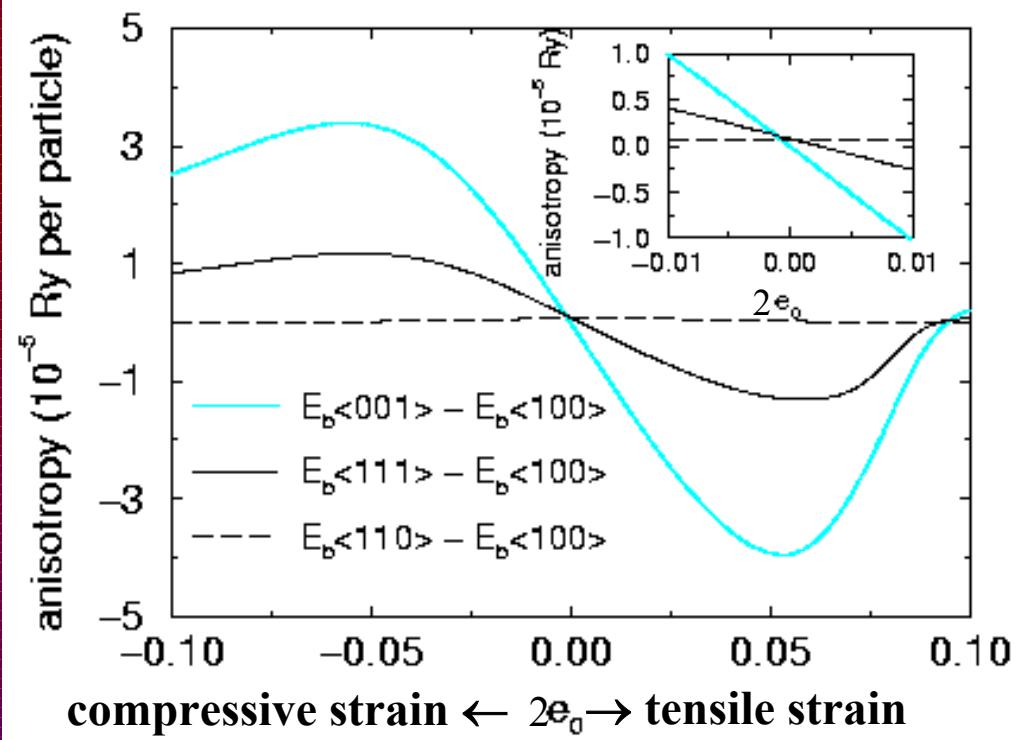
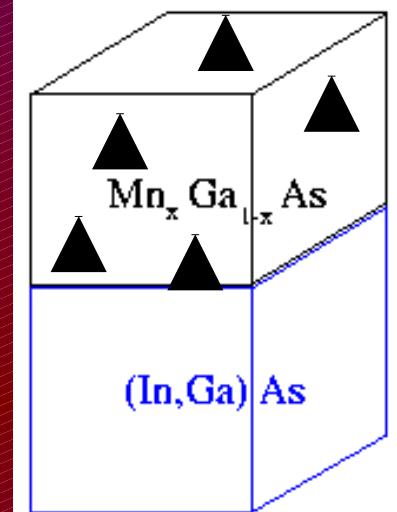
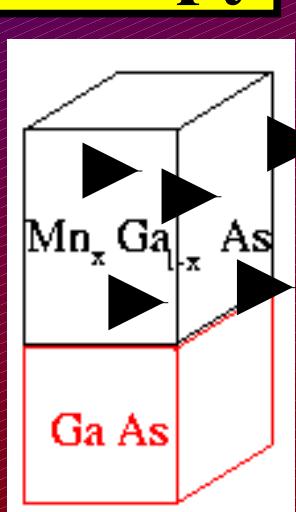


# Magnetic anisotropy



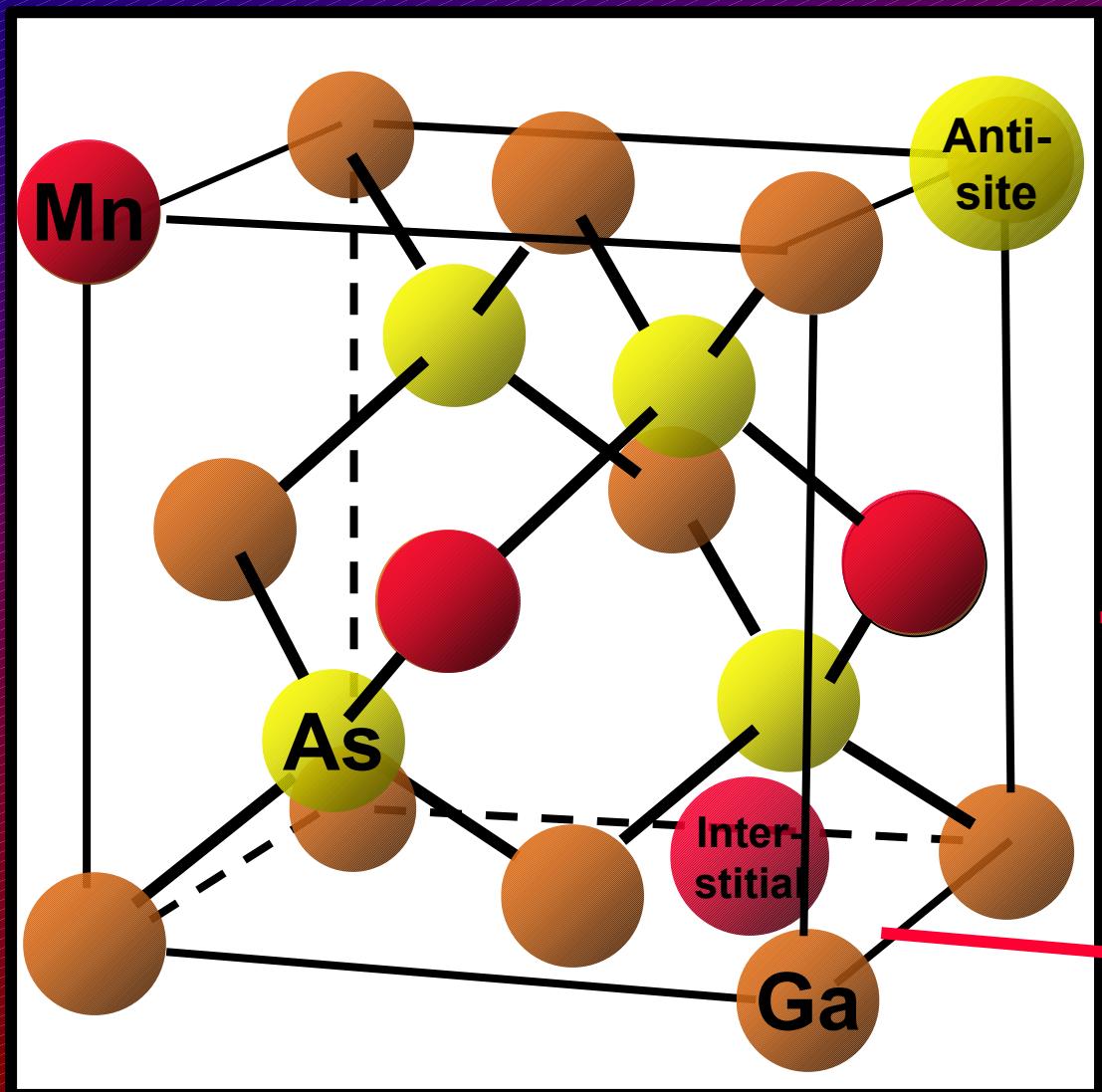
Condensation energy depends  
on magnetization orientation

(*T. Dietl, H. Ohno, F. Matsukura, PRB '01;  
M. Abolfath, T. Jungwirth, J. Brum, A.H. MacDonald,  
Phys. Rev. B '01*)



# Low Temperature MBE

## Disorder



As anti-site defect:  
 $Q=+2e$   
Coulomb potential

Substitutional Mn:  
 $Q=+e$  and local  $5/2$  moment  
Coulomb and exchange  
potentials

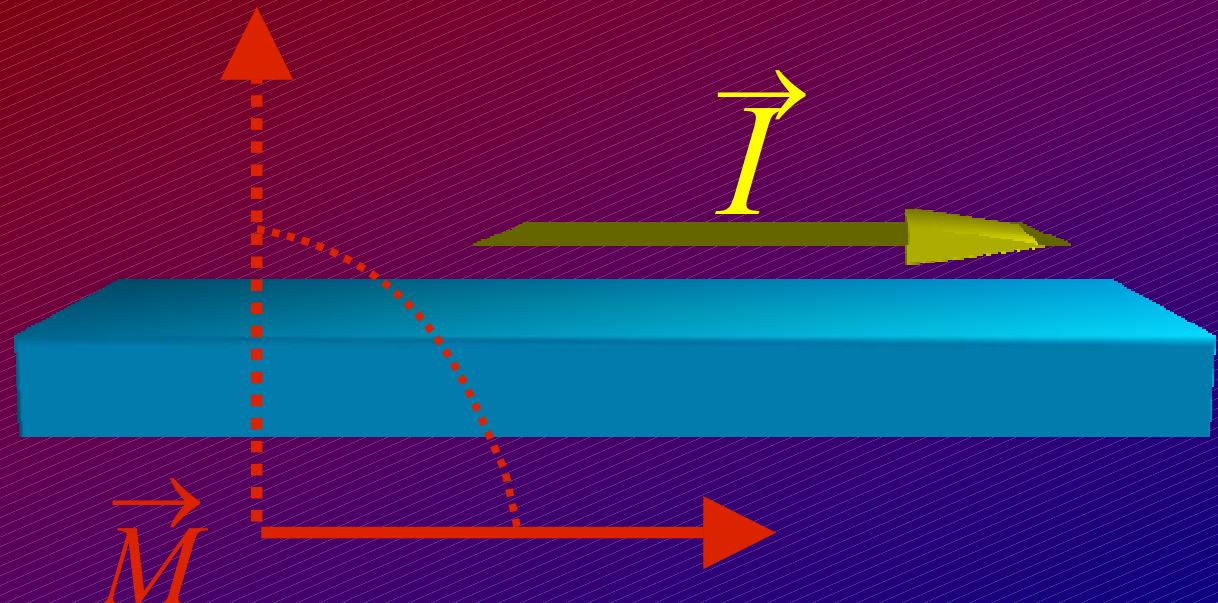
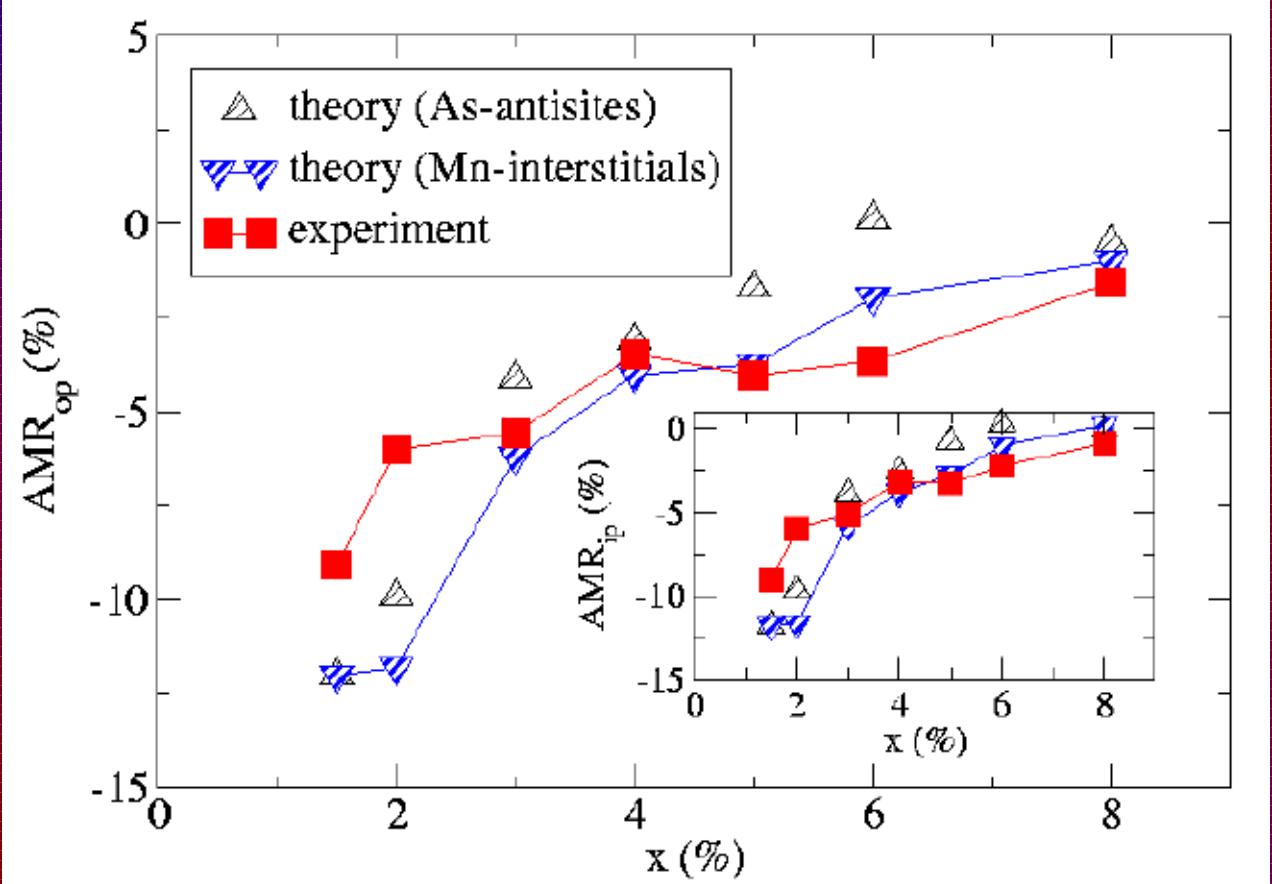
Interstitial Mn:  
 $Q=+2e$   
Coulomb potential

# Anisotropic magnetoresistance

Born approximation  
(finite quasiparticle lifetimes)

&

Linear-response theory



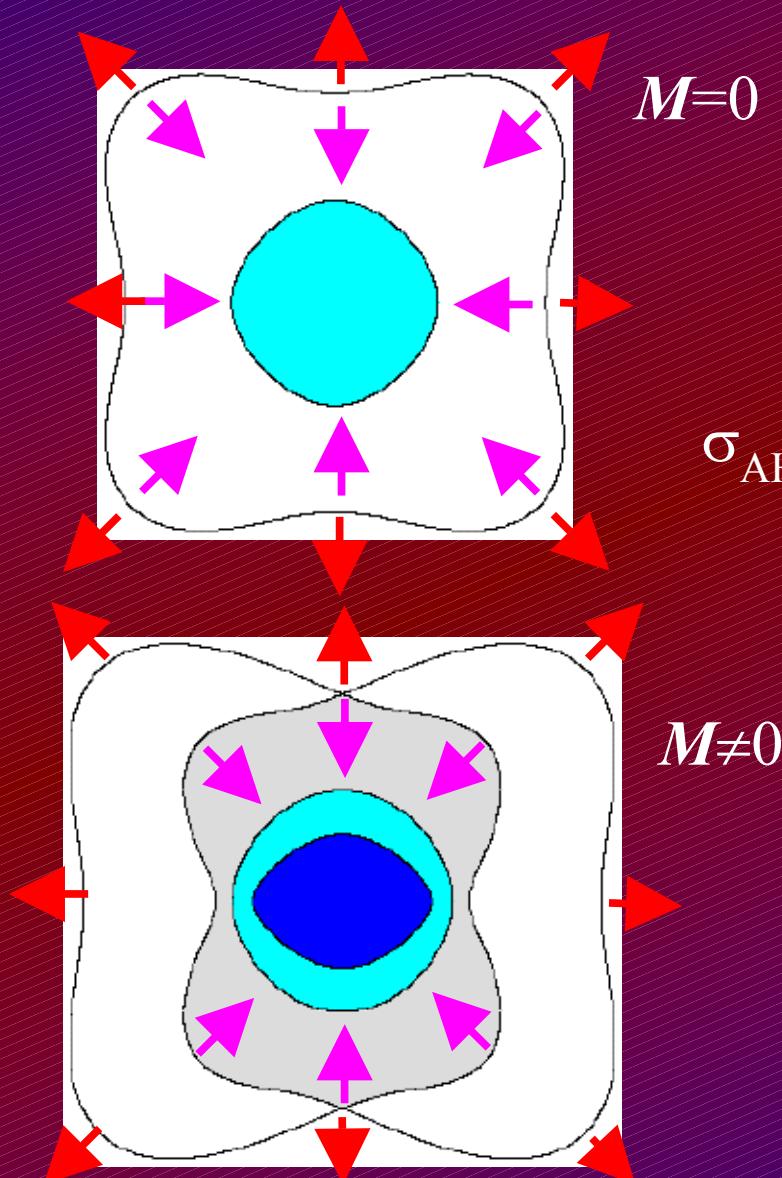
# Anomalous Hall effect

- Traditional approach: spin-orbit coupling in the scattering term  
skew scattering->  $\rho_{AH} \sim \rho$  and side-jump scattering->  $\rho_{AH} \sim \rho^2$   
(*L. Berger, Phys. Rev. B '70*)
- First and latest theories: band Hamiltonian with spin-orbit coupling  
non-zero *intrinsic*  $\sigma_{AH}$   
(*R. Karplus, J. Luttinger, Phys. Rev '54;*  
*M. Onoda, N. Nagaosa, J. Phys. Soc. Jpn. '02;*  
*T. Jungwirth, Q. Niu, A.H. MacDonald, PRL '02*)

- Semiclassical anomalous velocity

$$\mathbf{v} = \partial E_k / h \partial \mathbf{k} + (e/h) \mathbf{E} \times \mathbf{F}$$

Berry phase (F):  $\sigma_{\text{AH}} \sim \text{Im} \langle \partial \mathbf{u}_n / \partial k_x | \partial \mathbf{u}_n / \partial k_y \rangle$



- Quantum Kubo formula

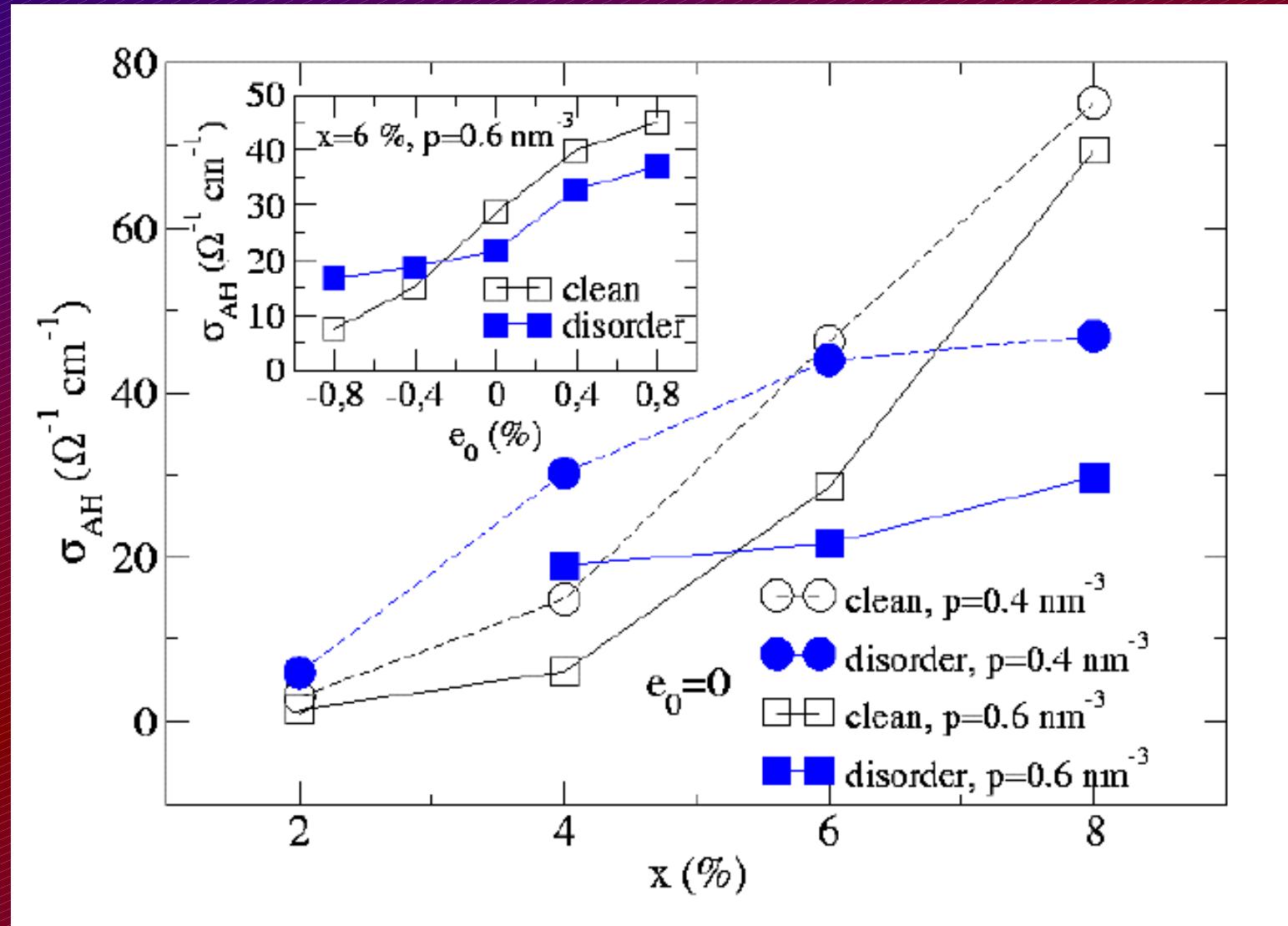
$$\sigma_{\text{AH}} \sim \text{Im} [\langle n', \mathbf{k} | p_x | n, \mathbf{k} \rangle \langle n, \mathbf{k} | p_y | n', \mathbf{k} \rangle] / (E_{n, \mathbf{k}} - E_{n', \mathbf{k}})^2$$



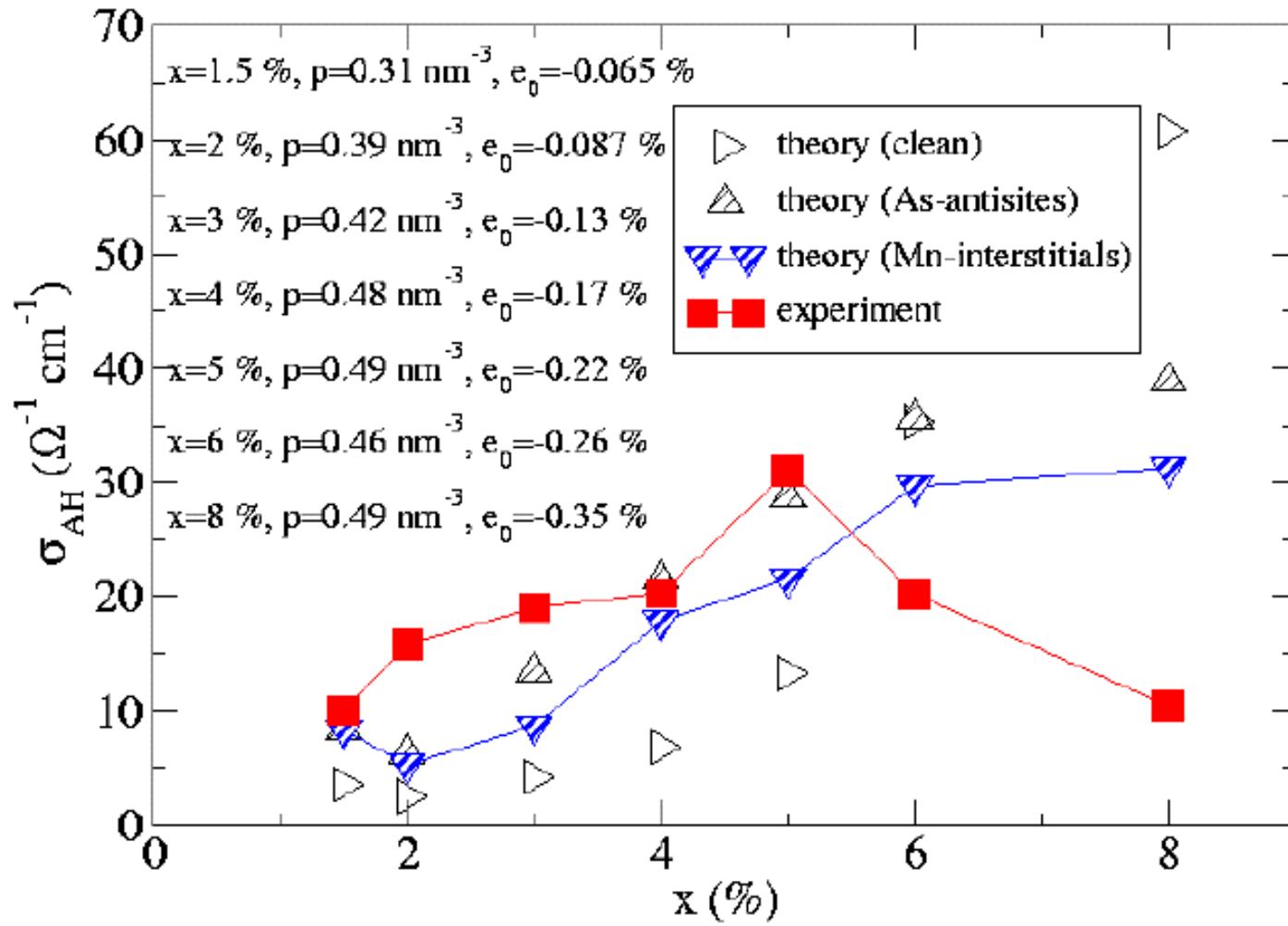
finite quasiparticle lifetimes

Analytic expression for the clean limit,  
small polarization, and strong spin-orbit  
coupling

# Doping and strain dependent AHE



## Theory vs. experiment



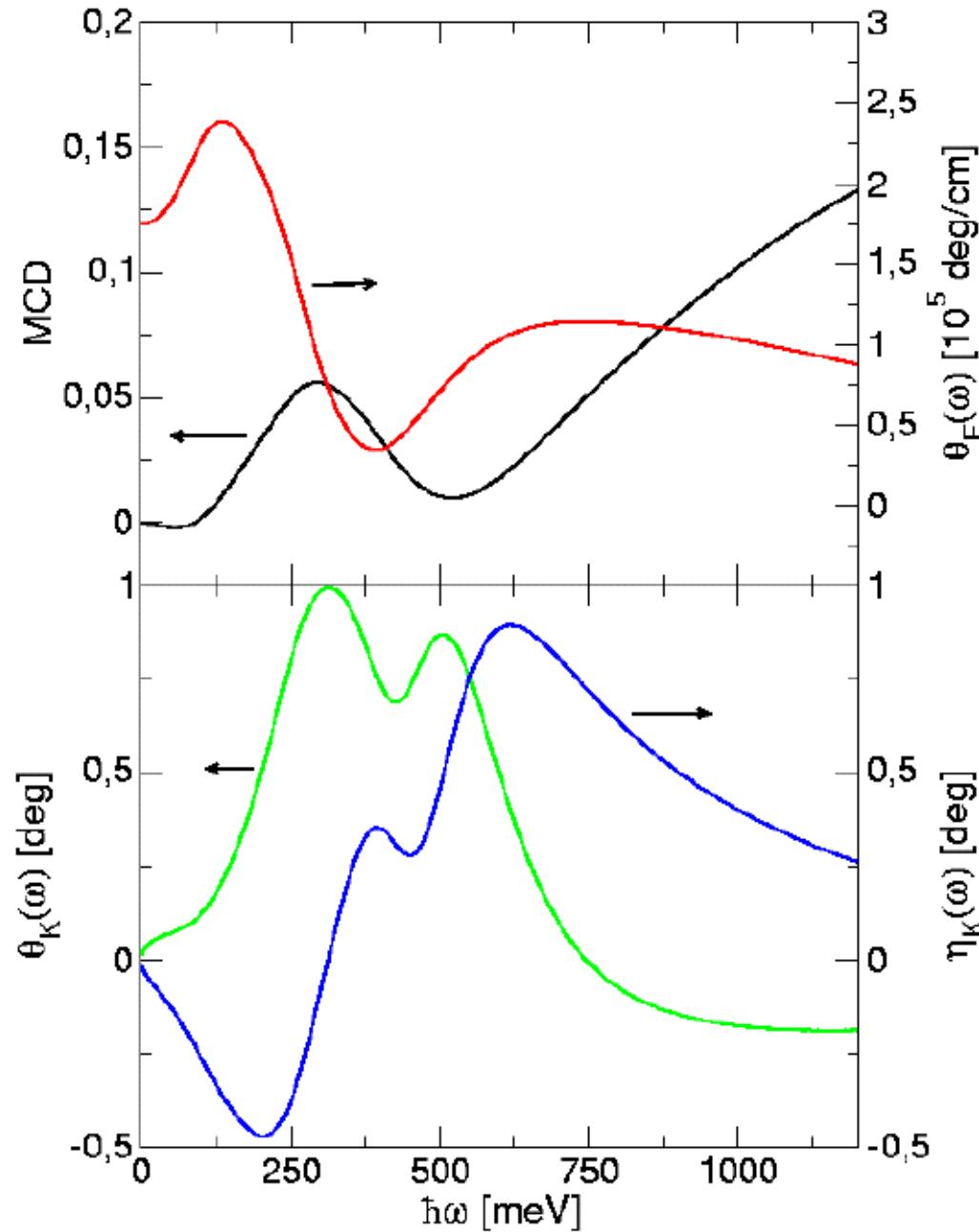
(T. Jungwirth, K.W. Edmonds, J. Sinova, B. L. Gallagher, A.H. MacDonald, unpublished)

# Infared magneto-optics

- Finite-frequency Kubo formula
- Born approximation quasiparticle lifetimes

Large MO effects

(*J. Sinova, B. T. Jungwirth,  
A.H. MacDonald, unpublished*)



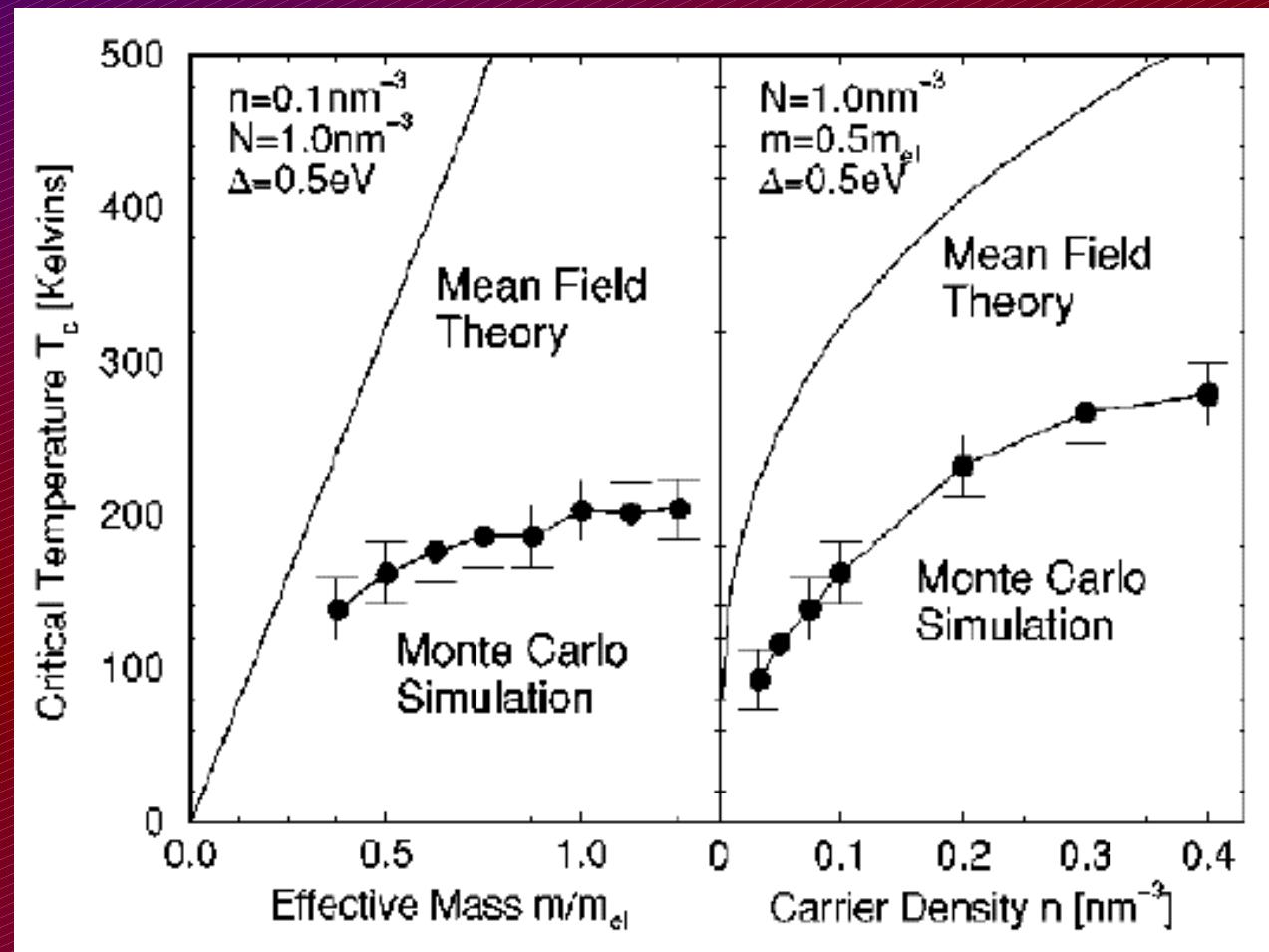
## Effective Hamiltonian (MF) and weak scattering theories (no free parameters)

- Ferromagnetic transition temperature ✓
- Magneto-crystalline anisotropy and coercivity ✓
- Domain structure ✓
- Anisotropic magnetoresistance ✓
- Anomalous Hall effect ✓
- MCD in the visible range ✓
- Non-Drude peak in longitudinal ac-conductivity ✓
- Infrared and visible range magneto-optics
- Ferromagnetic resonance
- Heterostructures and multilayers (spin-transfer, TMR, etc.)
- . . .

Extras ...

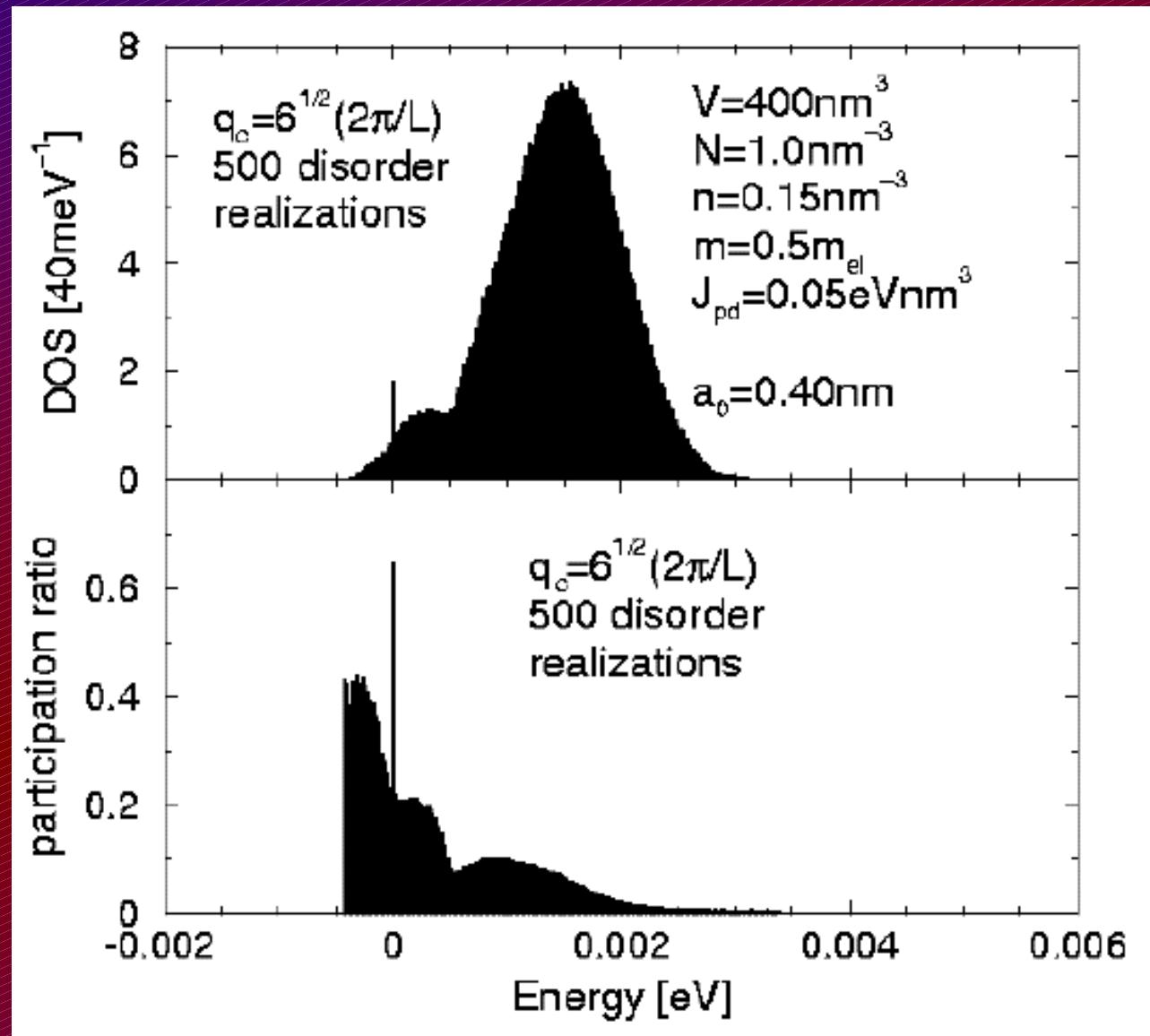
# Disorder effects beyond Born approximation

Suppresion of  $T_c$  due to spin fluctuations and disorder



(J. Schliemann, J. König, and A.H. MacDonald, PRB '01)

## Non-collinear ground states



(*J. Schliemann and A.H. MacDonald, PRL '02;*  
*also G. Zerand and B. Janko, PRL '02*)

# Metal-insulator transition at $\sim 1\%$ Mn

(*S.-R. Eric Young and A.H. MacDonald, cond-mat/0202021;  
C. Timm, F. Schäfer and F. von Oppen, PRL'02*)

*Enhanced  $T_c$  due to disorder in the insulating phase*

(*R.N. Bhatt, M. Berciu, M.P. Kennett, and X.Wan, Journal of Superconductivity '02*)