Locating and quantifying gas emission sources using remotely obtained concentration data

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Seminar: Data Science of the Natural Environment (slides at *www.lancs.ac.uk/~jonathan*)



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Over 2 million wells in North America

Locating gas emissions

GWP values and lifetimes from 2013 IPCC AR5 p714	Lifetime (veere)	GWP	
(with climate-carbon feedbacks) ^[8]	Litetime (years)	20 years	100 years
Methane	12.4	86	34
HFC-134a (hydrofluorocarbon)	13.4	3790	1550
CFC-11 (chlorofluorocarbon)	45.0	7020	5350
Nitrous oxide (N ₂ O)	121.0	268	298
Carbon tetrafluoride (CF ₄)	50000	4950	7350

Global warming potentials (wiki: time-integrated energy released from instantaneous release of 1 kg of trace substance relative to that of 1 kg of CO_2)

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Thanks

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Outline

Outline

Motivation

- A method for detecting, locating and quantifying sources of gas emissions to the atmosphere
- From remotely obtained atmospheric gas concentration measurements

Issues

- Potentially **large** background gas concentrations ($\approx 1800 ppb$ for CH_4)
- Need to detect small signals ($\approx 5 35ppb$ for CH_4)
- Gas dispersion determined by prevailing wind conditions

Approach

- Plume model represents gas dispersion between source and measurement location
- Measured concentration is sum of contributions from sources and relatively smooth background
- Infer source locations, source emission rates, background level, plume biases and uncertainties

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Outline



Smoke plumes (Gaussian plume in far field)

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Survey aircraft ($\approx 50ms^{-1}$, $\approx 200m$ above ground)

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Motivating test applications

Synthetic problem

Known wind field, sources and background, 10 sources

Landfill

- 2 landfill regions, probable diffuse sources
- Wind field from UK met–office global circulation model

Flare stack

- Single elevated near–point source
- Wind field from UK met–office global circulation model
- Coastal location

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Introduction A

Applications





(a) two passes x-y (b) first pass in time (c) second pass in time

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Landfill from above

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Locating gas emissions

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Landfill measurements

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Flare stack

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Introduction A

Applications



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Model formulation

$$\mathbf{y} = \mathbf{A}\mathbf{s} + \mathbf{b} + \boldsymbol{\epsilon}$$

- **y**: measured concentrations
- A: assumed known from plume model
- **s**: sources to be estimated
- **b**: background to be estimated
- ϵ : measurement error (assumed Gaussian), variance to be estimated

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Model

Plume

Plume model



- Red: Source height H
- Blue: Source half–width *w*
- **•** Magenta: Downwind offset δ_R
- **C**yan: Horizontal offset δ_H
- Green: Vertical offset δ_V
- **ABL** height: *D*
- Horizontal extent: $\sigma_H = \delta_R \tan(\gamma_H) + w$
- Vertical extent: $\sigma_V = \delta_R \tan(\gamma_V)$

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Opening angles: γ_H , γ_V

$$a = \frac{1}{2\pi |\mathbf{U}|\sigma_H \sigma_V} \exp\left\{-\frac{\delta_H^2}{2\sigma_H^2}\right\} \times \left\{ \exp\left\{-\frac{(\delta_V - H)^2}{2\sigma_V^2}\right\} + \exp\left\{-\frac{(\delta_V + H)^2}{2\sigma_V^2}\right\} + \exp\left\{-\frac{(\mathbf{2D} - \delta_V - H)^2}{2\sigma_V^2}\right\} + \exp\left\{-\frac{(\mathbf{2D} - \delta_V - H)^2}{2\sigma_V^2}\right\} \right\}$$

Background model

Requirements

- Positive and smoothly-varying, spatially and temporally
- Basis function representation: $\mathbf{b} = \mathbf{P}\boldsymbol{\beta}$
- We use Gaussian Markov random field
- Explicit spatial dependence due to wind transport incorporated

Random field prior

$$f(\boldsymbol{\beta}) \propto \exp\{-\frac{\mu}{2}(\boldsymbol{\beta}-\boldsymbol{\beta}_0)^T \mathbf{J}_{\boldsymbol{\beta}}(\boldsymbol{\beta}-\boldsymbol{\beta}_0)\}$$

J_β is sparse, P = I
Fast estimation

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Inference strategy

Initial point estimation

- Sources and background
- Source locations assumed on fixed grid
- **Fast** estimation of starting solution for Bayesian inference

Subsequent Bayesian inference

- Sources, background, measurement error, wind-field parameters, ...
- **Grid-free** sources modelled using Gaussian **mixture model**
- Reversible jump MCMC inference
- Quantified parameter uncertainties and dependencies

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Initial point estimation

Background prior

$$f(\boldsymbol{\beta}) \propto \exp\{-\frac{\mu}{2}(\boldsymbol{\beta}-\boldsymbol{\beta}_0)^T \mathbf{J}_{\boldsymbol{\beta}}(\boldsymbol{\beta}-\boldsymbol{\beta}_0)\}$$

Source prior (Laplace)

$$f(\mathbf{s}) \propto \exp\{-\lambda \|\mathbf{Q}\mathbf{s}\|_1\}$$

Likelihood

$$f(\mathbf{y}|\mathbf{s},\boldsymbol{\beta}) \propto \exp\{-\frac{1}{2\sigma_{\epsilon}^{2}}\|A\mathbf{s}+P\boldsymbol{\beta}-\mathbf{y}\|^{2}\},\$$

Posterior

$$f(\mathbf{s}, \boldsymbol{\beta}|\mathbf{y}) \propto f(\mathbf{y}|\mathbf{s}, \boldsymbol{\beta})f(\mathbf{s})f(\boldsymbol{\beta})$$

Maximum a-posteriori estimate

$$\operatorname{argmin}_{\mathbf{s},\boldsymbol{\beta}} \qquad \frac{1}{2\sigma_{\epsilon}^{2}} \|A\mathbf{s} + P\boldsymbol{\beta} - \mathbf{y}\|^{2} + \frac{\mu}{2}(\boldsymbol{\beta} - \boldsymbol{\beta}_{0})^{T} J(\boldsymbol{\beta} - \boldsymbol{\beta}_{0}) + \lambda \|Q\mathbf{s}\|_{1}$$

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Bayesian inference

Parameters

- Source locations **z**, "widths" **w** and emission rates **s** for mixture of *m* sources
- **\blacksquare** Random field background parameters β
- Measurement error standard deviation σ_{ϵ}
- Wind–direction correction δ_{ϕ}
- Others (e.g. plume opening angles)
- **Call these** θ which can be partitioned $\{\theta_{\kappa}, \theta_{\overline{\kappa}}\}$

Full conditional

```
f(\boldsymbol{\theta}_{\kappa}|\mathbf{y},\boldsymbol{\theta}_{\overline{\kappa}}) \propto f(\mathbf{y}|\boldsymbol{\theta}_{\kappa},\boldsymbol{\theta}_{\overline{\kappa}})f(\boldsymbol{\theta}_{\kappa}|\boldsymbol{\theta}_{\overline{\kappa}})
```

Inference tools

- Gibbs' sampling
- Reversible jump
- (Metropolis–Hastings)

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Synthetic



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Locating gas emissions

Landfill

Landfill



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Flare stack

Flare stack



(a) initial (b) median (c) 2.5% (d) 97.5%

Flare stack

Flare stack



(a) background in time (b) residual vs measured concentration initial (red); posterior median (black)

Wind direction correction of 18°

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Conclusions and on-going work

Conclusions

- Data structure and management
- Flexible inference using combination of standard methods
- Good performance on synthetic and field applications
- **Scalability** from iterative estimation

Extensions (on-going and potential)

- Multiple flights, multiple wind data sources
- Enhanced plume model
- Internal calibration
- Improved prior characterisation of sources, intermittent sources
- Simultaneous inference using multiple measurement types
- Optimal design
- Line-of-sight and satellite applications

Slides and articles at www.lancs.ac.uk/~jonathan

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Conclusions

Line-of-sight sensing



Line-of-sight laser

Locating gas emissions

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Satellite



Tropomi satellite and Google Earth

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Locating gas emissions

Satellite Service Dates



Potential to measure individual sources

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